Increasing the dimensionality of cryogenic molecular coolers: Gd-based polymers and metal-organic frameworks**

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Supporting information:
†Electronic Supplementary Information (ESI) available: [selected bond distance and angles for 1, crystallographic data in CIF format, isothermal magnetizations for 1 and 2]. See http://dx.doi.org/10.1039/C2CC33485B
Abstract

The magnetothermal properties of a coordination polymer and a metal-organic framework (MOF) based on Gd$^{3+}$ ions are reported. An equally large cryogenic magnetocaloric effect (MCE) is found, irrespective of the dimensionality. This combined with their robustness makes them appealing for widespread magnetic refrigeration applications.

Introduction

Gadolinium-based molecular magnetism and cryogenic magnetic refrigeration are closely interrelated topics that have received a rejuvenated$^1$ and increased interest in the recent literature.$^2$ The driving force stems from the experimental observation that the magnetocaloric effect (MCE) of this class of materials can outperform that of well-established magnetic refrigerants at liquid-helium temperatures. MCE describes the changes of magnetic entropy and adiabatic temperature, following a change of the applied magnetic field, and can be exploited for magnetic refrigeration in a process known as adiabatic demagnetization.$^8$ Gd$^{3+}$ is a common constituent element for molecular refrigerant materials, because large MCE can be favoured by: $^2$ (a) its $^8S_{7/2}$ ground state, which provides the largest entropy per single ion, (b) its quenched orbital momentum, which implies that crystal field effects are extremely small, and (c) its weak superexchange interactions, which result in low-lying excited spin states. For Gd-metal and most high-$T$ solid-state refrigerant materials, the MCE is driven by the mechanism of magnetic ordering.$^8$ For Gd-based molecular refrigerants, thermal fluctuations are typically stronger than that of magnetic origin between molecules, unless experiments are carried out deep in the sub-kelvin regime.$^7$ Therefore for such materials, one would expect the magnetic dimensionality to play no dominant role in the MCE. So far, MCE investigations have focused on high-spin 0D Gd clusters,$^{1,4,7}$ with rare exceptions.$^{5,6}$ Here, we report the MCE of two extended networks of Gd$^{3+}$ ions with 2D and 3D topologies, respectively the novel [Gd(HCOO)(OAc)$_2$(H$_2$O)$_2$] (1) and the MOF [Gd$_2$(N-BDC)$_3$(dmf)$_4$] (2, N-BDC = 2-amino-1,4-benzenedicarboxylic acid).$^9$ Their MCE are indeed found qualitatively similar to that of the best Gd-based clusters.$^5$ Providing a more robust, 3D framework structure to molecular coolers could facilitate their widespread applications through synthetic and technological strategies already developed in MOF science. Our MCE results for 2 nicely complement those already reported for other MOF materials, viz. Prussian blue analogues, investigated for magnetic refrigeration at high temperatures.$^{10}$

Compound 1 [Gd(HCOO)(OAc)$_2$(H$_2$O)$_2$]$^4$ crystallizes in the monoclinic $P2_1/m$ space group,$^4$ the asymmetric unit containing a a distorted square antiprismatic eight coordinate Gd$^{3+}$ ion coordinated by two chelating terminal acetate, two aqua ligands, both in cis-position, and a bridging $\mu$-O,O’ formato ion. The structure of 1 thus builds on 1D Gd$^{3+}$ coordination chains propagating along the $b$ axis through a single formato anti-anti bridge (Fig. 1a). Adjacent chains are rotated by 180° with respect to $b$, so that the water molecules and acetato groups form a dense network of hydrogen bonds that results in thick sheets in the $bc$ plane (Fig. 1b). The
corresponding Gd···Gd separations are respectively 6.584 Å through the –O–C–O– formate bridges and 5.920 Å through the –O–H···O– interchain H-bonds. The sheets are separated by the acetate methyl groups (Fig. 1c), without any significant interactions, resulting in a inter-plane Gd···Gd separation of 7.997 Å. The true topology of 1 is therefore likely better described as 2D. On the other hand, the structure of compound 2 is built from an edge-sharing [Gd$_2$] unit (Fig. 1d) connected through six N-BDC ligands in three dimensions to form a cubic porous framework with a 4$^{12}$-6$^3$ topology (Fig. 1e), with Gd···Gd separations in the 10.488-11.455 Å range. Within the dinuclear secondary building unit, the tricapped trigonal-pyramidal Gd$^{3+}$ ions are 4.073 Å apart, bridged through two $\mu$-O,O'-carboxylato and two $\mu$-O,O,O'-carboxylato groups.

![Figure 1](image.png)

**Figure 1.** Top: views of the structure of 1: a) coordination chains propagating along the $b$ axis; b) chains H-bonded into sheets perpendicular to the $a$ axis; c) packing of these planes along the chain $b$ axis. Bottom: a) [Gd$_2$] building unit (only the first carbon of the benzene rings of N-BDC are depicted) and b) its connection into a 3D framework in the structure of 2. H are omitted except those on water molecules, formate in a) and acetate in c). Colour code: Gd, purple; O, red; N, blue, C, black, H, beige.
Figure 2 depicts the direct current (dc) susceptibilities normalized per Gd$^{3+}$ ion, which were collected for the 2–300 K temperature range in an applied field of 0.1 T. For both compounds, the room-temperature $\chi^{(\text{Gd})}T$ value is that expected for a spin-only $S = 7/2$ Gd$^{3+}$ ion (7.875 cm$^3$Kmol$^{-1}$). The value stays roughly constant as the temperature is decreased, and at approximately 20 K the $\chi^{(\text{Gd})}T$ decreases, reaching a minimum of approximately 7.1 cm$^3$Kmol$^{-1}$ (7.2 cm$^3$Kmol$^{-1}$) at 2 K, for 1 (2). In agreement with previous investigations,$^9$ this behaviour points to very weak antiferromagnetic exchange for both complexes, being slightly weaker in the case of 2. Isothermal magnetizations versus field are not particularly sensitive to slight differences in the exchange, therefore very similar plots (collected in the 2–10 K range and up to 5 T, see Figure S1 in the Supporting Information) were observed for both complexes.

![Figure 2](image)

**Figure 2.** Temperature-dependencies (2–300 K) of the dc molar susceptibility per Gd$^{3+}$ ion for 1 (empty markers) and 2 (filled markers) collected in an applied field of 0.1 T.

We next present the heat capacities $C^{(\text{Gd})}$ of 1 and 2, which were collected in the 0.3–30 K range and up to 7 T, and are depicted as normalized per Gd$^{3+}$ ion in Figure 3. Close similarities between the measurements on the two compounds are easily discerned. At high temperatures, the heat capacity is dominated by nonmagnetic contributions arising from thermal vibrations of the lattice. These can be modelled with a Debye function (dotted lines), obtaining the values for the Debye temperatures $\Theta_D = 80.4$ K and 45.4 K for 1 and 2, respectively, evidencing a stiffer structure for the former (see, e.g., Fig. 1). The low-temperature $C^{(\text{Gd})}$ for $B_0 > 0$ is characterized by a field-dependent broad feature, arising from the splitting of the $S = 7/2$ multiplet, which shifts to higher temperature by increasing $B_0$ (also calculated to provide the solid lines in Fig. 3). The zero-field $C^{(\text{Gd})}$ presents a markedly different behaviour depending on the compound examined, which we associate
with the differences in the magnetic exchange. The very weak values of the exchange couplings that characterize these materials make it impossible to distinguish between the several exchange pathways, and only an average $J$ can be found. The estimate is obtained by comparing the experimental $T^{-2}$ term, $C^{(\text{Gd})}T^{-2}/R = 0.53 \text{ K}^2$ and 0.36 K$^2$, for 1 and 2, respectively, to the theoretical expression for the high-temperature “tail” of the magnetic heat capacity for Heisenberg coupling, i.e., $C^{(\text{Gd})}T^{-2}/R = 6z[S(S+1)J/(3k_B)]^2$, where $z$ is the number of nearest magnetic neighbours.$^{11}$ This comparison provides $z^{1/2}J/k_B = -0.06 \text{ K}$ and $-0.05 \text{ K}$ for 1 and 2, respectively, that points to a weaker exchange for the latter in agreement with the susceptibility data (Fig. 2). From the heat capacity, the temperature-dependence of the magnetic entropy $S_m^{(\text{Gd})}$ is obtained by integration, using $S_m^{(\text{Gd})}(T) = \int C_m^{(\text{Gd})}/T dT$, where the magnetic heat capacity $C_m^{(\text{Gd})}$ is obtained from $C^{(\text{Gd})}$ upon subtracting the lattice contribution. The thus-obtained $S_m^{(\text{Gd})}(T)$, depicted in Fig. S2 for the corresponding applied fields, tend to the maximum entropy value at high temperatures, corresponding to a Gd$^{3+}$ $S = 7/2$ spin $(R\ln(2S+1) = 2.08R)$.

![Graph](image.png)

**Figure 3.** Temperature-dependencies (0.3–30 K) of the heat capacity per Gd$^{3+}$ ion $C^{(\text{Gd})}$, normalized to the gas constant $R$ for 1 (empty markers) and 2 (filled markers) collected for $B_0 = 0, 1, 3$ and 7 T, as labelled. Plotted also is the zero-field magnetic heat capacity $C_m^{(\text{Gd})}$ (small markers) and lattice contribution (dotted lines) for both complexes.
Figure 4. Temperature-dependencies of the magnetic entropy change $\Delta S_m$, as obtained from magnetization ($M$) and heat capacity ($C$) data, for the indicated applied-field changes $\Delta B_0$, for 1 (top) and 2 (central). Bottom: entropy change per Gd$^{3+}$ ion and normalized to $R$, as obtained from $C$, for 1 (empty markers) and 2 (filled markers). Inset: magnification of the lowest-temperature region and $\Delta B_0 = 1$ T.

To evaluate the MCE, we obtain the isothermal magnetic entropy change $\Delta S_m$, following a change in the applied magnetic field $\Delta B_0$, from the measured magnetization (Fig. S1) and heat capacity (Fig. 3), using known data-processing procedures.$^{2,8}$ Both procedures provide identical results, depicted in Figure 4, proving the validity of our approach. It can be seen that $-\Delta S_m(T)$ reaches remarkable maxima, i.e., 45.9 Jkg$^{-1}$K$^{-1}$ for 1 and 29.0 Jkg$^{-1}$K$^{-1}$ for 2, both for $T = 1.8$ K and $\Delta B_0 = (7 - 0)$ T. The difference mostly stems from the normalized molar weight per Gd$^{3+}$ ion, i.e., 572.13 g for 1 and 366.38 g for 2. Indeed, both maximum values are close to the maximum available entropy per Gd$^{3+}$, i.e. $2.08R$. This is beautifully illustrated by the bottom panel of Fig. 4, showing the set of entropy data already depicted in the top panels, although now normalized.
per Gd\(^{3+}\) ion and gas constant \(R\). It is hardly possible to discern any difference between the behaviours of the two compounds, because the involved applied fields are largely overwhelming the effect due to the weak interactions present. Only for the lowest field change \(\Delta B_0 = 1\) T (inset of Fig. 4), one can notice that 1 achieves a lower MCE, while being slightly shifted towards higher \(T\), with respect to 2, in agreement with the relatively stronger \(J\) for 1, as it is well known that antiferromagnetic exchange does not favour the MCE.\(^{12}\)

In summary, we report that the cryogenic MCE for Gd-based molecular refrigerant materials can be spectacularly large, regardless of the magnetic dimensionality. At liquid-helium temperatures and for the applied fields typically involved, the MCE is chiefly determined by the Gd density, that is the metal:non-metal mass ratio. One can easily predict that this field will quickly move towards refrigerants with lighter ligands, because a larger MCE can be so achieved. We are still far from the ideal limit of an infinite ratio of non-interacting Gd\(^{3+}\) ions, for which the full entropy can be as large as \(2.08R/A_r\approx 110\) Jkg\(^{-1}\)K\(^{-1}\), where \(A_r\) is the relative Gd atomic mass.
Notes and references

[8] Synthesis of 1. Gd(OAc)$_3$∙6H$_2$O (442 mg, 1 mmol), HCOOH (40 µl, 1 mmol) and Et$_3$N (140 µl, 1 mmol) were dissolved in 25 ml of CH$_3$CN and stirred for two hours. The resulting white powder was filtered, washed with acetonitrile and dried. Recrystallisation from H$_2$O affords crystals of 1 in ~22% yield after ~40 days. Elemental analysis (%) calculated for C$_5$H$_{11}$O$_8$Gd: C 16.85, H 3.11; found: C 16.71, H 3.23.

[¶] Crystal data for 1: data were obtained on an Agilent XCalibur diffractometer at 100 K from Mo Kα (λ=0.71073) on a colourless plate, monoclinic, space group $P2_1/m$ (no. 11), with $a = 7.9966(4)$ Å, $b = 6.5839(2)$ Å, $c = 9.9447(4)$ Å, $β = 109.425(5)^o$, $V = 493.77(4)$ Å$^3$, $Z = 2$, $ρ_{\text{calcld}} = 2.397$ g/cm$^3$, $μ = 6.734$ mm$^{-1}$. 4816 reflections were measured, 1283 of which were independent. Refinement converged at final $wR_2 = 0.0758$, $R_1 = 0.0302$ and $S = 1.079$ (for 1095 reflections with $I > 2σ(I)$). CCDC 881702.

[£] Compound 2 was prepared as in ref. 9 and analyzed satisfactorily.


