A Vector Quantized Variational Autoencoder (VQ-VAE) Autoregressive Neural \( F_0 \) Model for Statistical Parametric Speech Synthesis

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Abstract—Recurrent neural networks (RNNs) can predict fundamental frequency (\( F_0 \)) for statistical parametric speech synthesis systems, given linguistic features as input. However, these models assume conditional independence between consecutive \( F_0 \) values, given the RNN state. In a previous study, we proposed autoregressive (AR) neural \( F_0 \) models to capture the causal dependency of successive \( F_0 \) values. In subjective evaluations, a deep AR model (DAR) outperformed an RNN.

Here, we propose a Vector Quantized Variational Autoencoder (VQ-VAE) neural \( F_0 \) model that is both more efficient and more interpretable than the DAR. This model has two stages: one uses the VQ-VAE framework to learn a latent code for the \( F_0 \) contour of each linguistic unit, and other learns to map from linguistic features to latent codes. In contrast to the DAR and RNN, which process the input linguistic features frame-by-frame, the new model converts one linguistic feature vector into one latent code for each linguistic unit. The new model achieves better objective scores than the DAR, has a smaller memory footprint and is computationally faster. Visualization of the latent codes for phones and moras reveals that each latent code represents an \( F_0 \) shape for a linguistic unit.

Index Terms—fundamental frequency, speech synthesis, neural network, variational auto-encoder

I. INTRODUCTION

The fundamental frequency (\( F_0 \)) is the frequency of vibration of the vocal folds during voiced speech sounds. The perceptual consequence of the \( F_0 \) is pitch. The \( F_0 \) carries phonological information in tonal languages and suprasegmental information in all languages [1]. For example: in Japanese which is a pitch-accent language, the change of \( F_0 \) height at the lexical level differentiates ‘alcohol’ (/sake/) from ‘salmon’ (/sa’ke/) [2]; in English, the \( F_0 \) is used to make a particular word more prominent, or to differentiate a statement from a question. In text-to-speech synthesis (TTS), where the achievable segmental quality is now very high [3], the \( F_0 \) of the generated waveform is arguably the most important place to look for improvements in naturalness.

Although some recent TTS systems [4], [5] predict (Mel) spectrograms, in which the \( F_0 \) is implicit, many other systems still represent the \( F_0 \) explicitly as a separate acoustic feature [6], [7]. In most statistical parametric speech synthesis (SPSS) systems [8], [9], the \( F_0 \) contour is predicted from a sequence of linguistic features that have been extracted from input text using the front-end text processor. Given the predicted \( F_0 \) and spectral features, SPSS systems generate a speech waveform using a deterministic or neural vocoder [10], [11].

We focus on the task of \( F_0 \) prediction for SPSS. We assume a traditional SPSS approach as the baseline in which the input linguistic feature and output acoustic feature sequences are equal in length and aligned in time; each time step in these sequences is a speech frame. In such a framework, \( F_0 \) prediction can be achieved using a neural network (NN), such as a recurrent NN (RNN) with long-short-term memory (LSTM) units [12]. Although such a model is straightforward to use and performs reasonably well, conditional independence is assumed between the \( F_0 \) at different frames. To alleviate this incorrect assumption, we previously proposed autoregressive (AR) \( F_0 \) models that can capture the causal dependency of each value in the \( F_0 \) sequence (i.e., the \( F_0 \) contour). A subjective evaluation demonstrated that one of our AR \( F_0 \) models – the deep AR \( F_0 \) model (DAR) – outperformed an RNN [13].

Although the DAR models the probability distribution of \( F_0 \) contours better than an RNN, it still processes input linguistic features frame by frame. However, most values in a frame-rate linguistic feature vector sequence have a constant value from one frame to the next because they change only every segment, syllable, word, etc. When operating at the frame rate, the recurrent layer(s) must propagate information across many frames before it can be used to predict the \( F_0 \) of the next segment. If the model uses a convolutional layer, however, it has to use a large convolution receptive field.

In this paper, we improved both the efficiency and interpretability of the DAR and developed a two-stage Vector Quantized Variational Autoencoder (VQ-VAE)-based AR \( F_0 \) model. During \( F_0 \) generation in a TTS system, the proposed model uses a linguistic linker to convert the linguistic features of one linguistic unit into a latent code vector. The model then uses a DAR-based \( F_0 \) contour generator to output an \( F_0 \) contour conditioned on the latent vector and duration of
the unit. In contrast to the DAR and to conventional RNN $F_0$ models, the linker in the proposed model operates at the segment rate rather than the frame rate. It processes only one input linguistic feature vector and produces one latent code for each segment, which reduces processing time and facilitates the use of wider context.

The training algorithm has two steps. We first use the VQ-VAE framework [14] and train the DAR-based $F_0$ contour generator (i.e., the VQ-VAE’s decoder) jointly with the VQ-VAE’s encoder and VQ codebook. We then use the trained VQ-VAE encoder and codebook to extract the quantized latent codes from the training data and train the linker to predict the latent codes from the input linguistic features. The trained model only uses the linker, VQ-VAE codebook, and decoder for $F_0$ generation, leaving the VQ-VAE encoder unused.

We conducted experiments in which the linguistic unit was defined as a phone, syllable, or word. We also combined latent codes from linguistic units at multiple levels. The experiments demonstrated that the model using the phone and syllable levels provided objective and subjective results no worse than the DAR, even though the proposed model is smaller. More interestingly, the learned latent codes encode the DAR, even though the proposed model is smaller. Many other models generate the $F_0$ for each frame, but they only use simple input features and limited network size due to the limitation of computation resources at that time.

### II. BRIEF REVIEW OF RELATED $F_0$ MODELS

We consider the $F_0$ modeling as a task to learn the mapping from the input linguistic features to the output $F_0$ sequence. At each time step, the target $F_0$ datum encodes the voicing status and the $F_0$ value if the frame is voiced.

#### A. Classical models

For SPSS-based TTS systems, hidden Markov models (HMMs) plus decision-trees have been widely used to model the $F_0$ and other spectral features. Specifically, multi-space probability distribution HMMs directly model the raw $F_0$ contours that may contain unvoiced frames [15], whereas HMM-based continuous $F_0$ models use interpolated $F_0$ contours and the voicing status as the target [16]. Based on these two models, many other models or methods have been proposed. For example, some $F_0$ models generate the $F_0$ contour by adding $F_0$ components at different linguistic levels [17], [18], [19]; some other models use an alternative $F_0$ representation rather than the raw or interpolated $F_0$ contour [20], [21].

Recently, researchers have used NNs as alternatives to HMMs to jointly model the $F_0$ and other spectral features [22], [23], [24]. Some researchers use NNs exclusively for $F_0$ modeling [25], [12], which may be reasonable because it was recently found that NNs may prioritize the spectral features over the $F_0$ [26]. In fact, many NN-based $F_0$ models have been proposed before the advent of SPSS-based TTS systems [27], [28], [29]. Some of the NN-based models may only predict $F_0$s for a few target points per linguistic unit [30].

### B. Autoregressive neural $F_0$ models

We focused on recent NN-based $F_0$ models because they are straightforward to use and perform well. The goal of an NN-based $F_0$ model is to convert a linguistic feature sequence of $T$ frames $x_{1:T} = \{x_1, \cdots, x_T\}$ into an $F_0$ sequence $c_{1:T} = \{c_1, \cdots, c_T\}$, where $c_t \in \mathbb{R}$ is the $F_0$ value at the $t$-th frame of an interpolated continuous-valued $F_0$ contour (i$F_0$) [7]. For an RNN-based $F_0$ model, its output at the $t$-th frame can be written as $\hat{c}_t = \mathcal{H}_\theta(x_{1:t}, \theta)$, where $\mathcal{H}_\theta(\cdot)$ and $\Theta$ denote the non-linear transformation conducted by the network and the network’s weights, respectively. Usually, $\Theta$ can be learned by minimizing a mean square error (MSE) $E = \sum_{t=1}^T \| \mathcal{H}_\theta(x_{1:t}, \theta) - c_t \|^2$ over a training data set. After training, the RNN can produce $\hat{c}_{1:T}$ for a new input sequence $x_{1:T}$ by generating $\hat{c}_t = \mathcal{H}_\theta(\hat{x}_{1:t}, \theta)$, $\forall t \in \{1, \cdots, T\}$.

The above method implicitly treats the RNN as a probabilistic model [31] with a distribution of $c_{1:T}$ at $\Theta$:

$$p(c_{1:T} | x_{1:T}; \Theta) = \prod_{t=1}^{T} p(c_t | x_{1:t}; \Theta) = \prod_{t=1}^{T} \mathcal{N}(c_t; \mathcal{H}_\theta(x_{1:t}, \beta I), \beta I),$$

(1)

where $\mathcal{N}(\cdot)$ is the Gaussian distribution, $I$ is an identity matrix, and $\beta$ is a variance parameter. Training the RNN using the MSE criterion is equivalent to a maximum-likelihood training on the probabilistic model; using $\mathcal{H}_\theta(\hat{x}_{1:t}, \theta)$ as the generated $F_0$ is equivalent to taking the mean of the Gaussian distribution as the output. This probabilistic interpretation also allows the RNN to be extended as a recurrent mixture density network (RMDN) [32], [33] where the Gaussian distribution is replaced with a Gaussian mixture model (GMM).

An RNN-based $F_0$ model has been demonstrated to be better than those based on feedforward NNs [12]. However, as Equation (1) shows, a conditional independence between $c_{t1}$ and $c_{t2}$, $\forall t_2 \neq t_1$ is assumed with an RNN (and RMDN),

\footnote{The interpolated $F_0$ contour is modeled jointly with a sequence of voicing statuses [16]. The voicing status is omitted here for the purpose of explanation.}

\footnote{In this paper, we use $p(\cdot)$ and $F(\cdot)$ to denote the probability density function for a continuous random variable and probability mass function for a discrete random variable, respectively.}
which is incompatible with the fact that \( F_0 \) values in neighboring frames may be highly correlated. We recently proposed AR neural \( F_0 \) models that learn the causal temporal dependency of \( F_0 \) contours \cite{13}. One of these models, the shallow AR model (SAR), defines the distribution of \( c_{1:T} \) as

\[
p(c_{1:T}|x_{1:T}; \Theta, \Psi) = \prod_{t=1}^{T} p(c_t|c_{1:t-1}, x_{1:T}; \Theta, \Psi)
\]

\[
= \prod_{t=1}^{T} N(c_t; H_{\Theta}(x_{1:T}, t) + \sum_{k=1}^{K} a_k c_{t-k} + b, \beta I)
\]

where \( \Psi = \{a_1, \ldots, a_K, b\} \). In contrast to an RNN, the distribution of \( c_t \) is assumed with SAR to be dependent not only on \( x_{1:T} \) but also on the observations \( c_{t-K:t-1} \) in the previous \( K \) frames. Note that the SAR can also be defined on the basis of the RMDN \cite{13}.

Although the SAR is theoretically better, it fails to outperform an RNN-based model for \( F_0 \) modeling because the SAR only models the local dependency \cite{13}. A more powerful of our previous models is the DAR \cite{13}, which defines:

\[
P(o_{1:T}|x_{1:T}; \Theta) = \prod_{t=1}^{T} P(o_t|o_{1:t-1}, x_{1:T}; \Theta)
\]

To avoid the impact of the interpolated \( F_0 \) curves, the DAR uses quantized \( F_0 \)s (qF0s) rather than interpolated continuous-valued \( F_0 \)s as the target. The quantized \( F_0 \) of the \( t \)-th frame is represented as a one-hot vector \( o_t = [o_{t,0}, o_{t,1}, \ldots, o_{t,N}] \), where \( N \) is the number of quantization levels. For example, \( o_t = [1, 0, \ldots, 0] \) denotes an unvoiced frame, while \( o_t = [0, 0, \ldots, o_{t,n} = 1, \ldots, 0] \) means an \( F_0 \) value at the \( n \)-th quantization level. The DAR then uses a hierarchical softmax layer to calculate a categorical distribution for each quantized \( F_0 \) datum. Suppose that the \( j \)-dimension of \( o_t \) is 1, the probability of \( o_t \) can then be written as:

\[
P(o_t|o_{1:t-1}, x_{1:T}; \Theta) \triangleq P_l(J = j)
\]

\[
P_l(J = j) = \begin{cases} 
\frac{e^{h_{t,0}}}{1 + e^{h_{t,0}}}, & j \in \{0\} \\
1, & j \in [1, N] \\
\frac{e^{h_{t,j}}}{1 + \sum_{k=1}^{N} e^{h_{t,k}}}, & j \in [1, N]
\end{cases}
\]

Here, \( h_{t,j} \) is the \( j \)-th dimension of the input vector \( h_t \) to the softmax layer. In implementation, the hierarchical softmax uses a sigmoid function to compute the probability of being unvoiced, i.e., \( P_l(\text{unvoiced}) \triangleq P_l(J = 0) = \frac{e^{h_{t,0}}}{1 + e^{h_{t,0}}}. \)

It then uses a normal softmax to compute the conditional probability of each quantized \( F_0 \) level as \( P_l(J = j|\text{voiced}) = \frac{e^{h_{t,j}}}{\sum_{k=1}^{N} e^{h_{t,k}}}, j \in [1, N]. \)

More importantly, the DAR introduces the links that feed the previous observation into a uni-directional recurrent layer, which is plotted in Figure 1. The feedback datum is transformed non-linearly and propagated to the rest of the utterances, which theoretically enables the distribution of \( o_t \) to depend on \( o_{1:t-1}. \) Compared with the SAR, the DAR theoretically models non-linear temporal dependency in a longer time-span. Our previous experiments demonstrated that

the DAR outperformed the SAR and an RNN-based model with a statistically significant difference for \( F_0 \) modeling \cite{13}.

III. PROPOSED VQ-VAE-BASED AR \( F_0 \) MODEL

A. Shortcomings of conventional NN-based \( F_0 \) models

The input linguistic features \( x_{1:T} \) to an \( F_0 \) model mainly contain the linguistic properties of phone, syllable, and other high-level segments. When a TTS front-end generates \( x_{1:T}, \) it simply replicates the features of the \( n \)-th segment to \( \{x_{tn}, x_{tn+1}, \ldots, x_{t(n+1)−1}\} \), where \( t_n \) and \( t(n+1)−1 \) denote the first and last frames of that segment. Although the frame index \( t \) may be added, most dimensions of the linguistic feature vectors remain the same within one segment. An example is illustrated on the left side of Figure 2.

It is inefficient for the DAR and other conventional NN-based \( F_0 \) models to convert \( x_{1:T} \) into the \( F_0 \) contour \( o_{1:T} \) frame by frame. First, the input layers spend much time processing replicated linguistic features in one segment. Furthermore, they cannot easily retrieve the features of neighboring segments. In a recurrent layer, the features of the surrounding segments may be attenuated when they are propagated across frames. If a convolutional layer is used, its receptive field must be sufficiently large to cover surrounding segments.

Another shortcoming is that the hidden features of conventional NN-based \( F_0 \) models cannot be easily interpreted. In some classical \( F_0 \) modeling frameworks, such as the combination of decision trees and the Tilt model \cite{34}, the linguistic features are converted into meaningful discretized \( F_0 \) events (e.g., Tilt events) then transformed into an \( F_0 \) contour. If an NN-based \( F_0 \) model provides meaningful hidden features, it would facilitate theoretical research on speech prosody.

B. Introducing latent variables to NN-based \( F_0 \) models

As the right side of Figure 2 illustrates, a more efficient and interpretable model may only need to process a short input sequence \( x_{1:N_p} \), where \( N_p \) is the number of segments such as phones in the utterance. To convert \( x_{1:N_p} \) into \( o_{1:T} \) (or \( c_{1:T} \)), the \( F_0 \) model may introduce an intermediate feature sequence \( e_{1:N_p} \) that satisfies the following three conditions:

- \( e_{1:N_p} \) can be easily predicted from \( x_{1:N_p} \);
- \( e_{1:N_p} \) can be easily converted to a frame-level \( e_{1:T} \) then \( o_{1:T} \), given the duration of each phone;
- \( e_{1:N_p} \) is interpretable.
One potential implementation for the above idea is to replace the hidden layer near the input side of the DAR with a clockwork recurrent layer [35], which extracts $e_{1:N_p}$ from $x_{1:N_p}$ and replicates $e_{1:N_p}$ into $e_{1:T}$ given the duration of each phone. However, such a clockwork DAR model did not outperform the normal DAR in our pilot experiments. Furthermore, the clockwork recurrent layer did not produce meaningful hidden features.

Another approach is to treat $e_{1:N_p}$ as latent variables and formulate a two-staged $F_0$ model as

$$P(o_{1:T} | x_{1:N_p}; \Theta) = \int_{e_{1:N_p}} P(o_{1:T} | e_{1:N_p}; \Phi) p(e_{1:N_p} | x_{1:N_p}; \Omega) de_{1:N_p}, \quad (5)$$

where $p(e_{1:N_p} | x_{1:N_p}; \Omega)$ converts $x_{1:N_p}$ into $e_{1:N_p}$, $P(o_{1:T} | e_{1:N_p}; \Phi)$ generates the $F_0$ contour given $e_{1:N_p}$, and $\Theta = \{ \Phi, \Omega \}$. Such a model can be trained under the framework of a conditional variational autoencoder (VAE) by maximizing an evidence lower bound (ELBO) [37]

$$\log P(o_{1:T} | x_{1:N_p}) \geq E_{q(e_{1:N_p}|o_{1:T}, x_{1:N_p}, \Gamma)} \log P(o_{1:T}|e_{1:N_p}; \Phi) - \text{KLD}[q(e_{1:N_p}|o_{1:T}, x_{1:N_p}, \Gamma)||p(e_{1:N_p}|x_{1:N_p}; \Omega)], \quad (6)$$

where $P(o|e; \Phi)$, $q(o|e; \phi; \Gamma)$, and $p(e|x; \Omega)$ denote the decoder, encoder, and prior distribution of the latent variables, respectively, and KLD is the Kullback-Leibler divergence.

As an implementation, the encoder $q(o|e; \phi; \Gamma)$ may use a linguistic-boundary-based pooling strategy to summarize the $F_0$ features from $o_{1:T}$ for each of the $N_p$ phones (see Section II-C1) and generate the latent variables $e_{1:N_p}$. The decoder $P(o|e; \Phi)$ can be a DAR that receives the replicated latent variables $e_{1:T}$ as input.

However, our pilot experiments showed that the KLD decreased to zero after only two training epochs, and the decoder ignored the latent variables. The resulting model became similar to the DAR and the latent variables became useless.

The above phenomenon has been reported in VAE-based text and image generation models under the name of ‘posterior collapse’ [35], [39]. One possible reason is that, without using latent variables, the DAR-based decoder has found sufficient information from the feedback data $o_{1:t-1}$ to predict $o_t$.

### C. Proposed model and implementation

To avoid ‘posterior collapse’, we define the proposed $F_0$ model on the basis of the VQ-VAE framework [14]

$$P(o_{1:T}|x_{1:N_p}; \Theta) = \sum_{e_{1:N_p} \in \Phi_2} P(o_{1:T}|e_{1:N_p}; \Phi_1) P(e_{1:N_p}|x_{1:N_p}; \Omega), \quad (7)$$

where the latent vectors $e_{1:N_p}$ are assumed to be selected from a codebook $\Phi_2$ using a vector quantization process.

Although other frameworks, such as the annealing trick [38], may also alleviate the ‘posterior collapse’, we chose the VQ-VAE framework because the quantized latent codes are more compatible with the linguistic assumption that $F_0$ can be abstracted as discretized prosodic events [40], [41]. Another motivation is that the VQ-VAE framework has not been used for $F_0$ modeling. A probabilistic interpretation on the VQ-VAE and its relationship with a conventional VAE are reported in another of our studies [36].

We list the steps to train and use the proposed VQ-VAE-based $F_0$ model based on the definition in Equation (7):

1. Train the decoder $P(o_{1:T}|e_{1:N_p}; \Phi_1)$ with the codebook $\Phi_2$ and an encoder $q(e_{1:N_p}|o_{1:T}; \Phi_3)$ using the standard VQ-VAE training method;
2. Use the trained encoder and codebook to extract the quantized codes $e_{1:N_p}$ from the $F_0$ training data and train a model $P(l_{1:N_p}|x_{1:N_p}; \Omega)$ to predict the indices $l_{1:N_p}$ of the quantized codes $e_{1:N_p}$ from the input linguistic features $x_{1:N_p}$. Because $P(l_{1:N_p}|x_{1:N_p}; \Omega)$ links the latent $F_0$ space with the linguistic feature space, it is referred to as a linguistic linker.
3. Combine the linker, VQ-VAE codebook, and decoder as a full-fledged model for $F_0$ generation, leaving the VQ-VAE encoder unused.
These three steps are illustrated in Figure 3. Details of the three steps are explained in the following sections. Note that, because $e_{1:N_p}$ are quantized, the combination of the codebook and linker is equivalent to $P(e_{1:N_p}|z_{1:N_p}; \Omega)$ in Equation (7). The VQ-VAE part is trained in an almost-unsupervised manner since it only requires the $F_0$ and linguistic boundary of linguistic segments.

1) VQ-VAE: The first step is to use the VQ-VAE framework and learn the parameter of $p(o_{1:T}|e_{1:N_p}; \Phi_1)$ together with the codebook and encoder. The three components are trained by minimizing

$$L(\Phi) = -\log p(o_{1:T}|e_{1:N_p}; \Phi_1) + \|e_{1:N_p} - \text{sg}[z_{1:N_p}]\|^2_2 + \beta \|z_{1:N_p} - \text{sg}[e_{1:N_p}]\|^2_2,$$

where the quantized code vectors $e_{1:N_p}$ (i.e., centroid of code cell) and raw latent vectors $z_{1:N_p}$ are given by

$$e_{1:N_p} = \text{Vector-quantization}_{\Phi_2}(z_{1:N_p}), \quad z_{1:N_p} = \text{Encoder}_{\Phi_3}(o_{1:T}),$$

and $\Phi = \{\Phi_1, \Phi_2, \Phi_3\}$. The first term in Equation (8) measures the reconstruction loss; the second term drives the quantized vectors towards the raw latent vectors; the third term is a ‘commitment loss’ that prevents the output of the encoder from growing arbitrarily large [14]. The hyper-parameter $\beta$ scales the commitment loss and is set to 0.25 as in the original paper [14]. The operator $\text{sg}[]$ zeros out the gradient back propagated to the argument.

Training the VQ-VAE is not straightforward because the gradients of $z_{1:N_p}$ w.r.t the reconstruction loss is undefined due to the undifferentiable VQ process in Equation (9). Following the original paper [14], we use the straight-through estimator (ST) to copy the gradients from $e_{1:N_p}$ to $z_{1:N_p}$ during the backpropagation on Equation (9). Accordingly, the encoder $\Phi_3$ is trained by minimizing the first and third terms of Equation (8), while the codebook $\Phi_2$ and decoder $\Phi_1$ are updated based on the second and first terms, respectively.

Remember that we only use a single code $e_{n_p}$ to encode the $F_0$ curve for the $n$-th segment. This is implemented using a linguistic-boundary-based pooling strategy. As step 1 in Figure 3 shows, the encoder uses a bi-directional recurrent layer to process $o_{1:T}$ and extracts $z_{n_p}$ for the $n$-th phone by concatenating the hidden features of the first and last frames of that phone. After that, the centroid vector $e_{n_p}$ closest to $z_{n_p}$ is retrieved from the codebook. Given the quantized code sequence $\{e_1, \ldots, e_{N_p}\}$, the decoder simply replicates each code to all the frames in the corresponding phone and reconstructs $o_{1:T}$ frame by frame. Note that the decoder uses a similar structure to the DAR.

The explanation above only concerns the latent codes for the phone. However, it is straightforward to extract latent codes of other linguistic units using additional encoders. In Figure 4, for example, the mora encoder is added to extract the mora latent codes $\Phi_2$. This mora encoder has a similar structure to the phone encoder except that it outputs one code per mora. Each mora code is replicated to every phone within that mora, and the sum of the phone and mora codes is used as the latent representation for the phone. Note that the latent codes of different linguistic layers are equal in dimension. The latent vectors can also be concatenated. However, summing the latent vectors was found to be slightly better in our pilot experiments.

Encoders of multiple linguistic levels should be trained in a top-down manner. For the case in Figure 5 the mora encoder and codebook are first trained, after which the phone part is updated with the mora encoder and codebook fixed. The single decoder, however, is always updated. Such a training approach prevents the VQ-VAE from ignoring the latent codes provided by a high-level encoder.

2) Linguistic linker: After the VQ-VAE is trained and the latent codes are extracted from the training $F_0$ data, the linguistic linker learns to map the linguistic features into the latent codes. Because the latent codes are codewords in a codebook, the task of the linker is equivalent to a sequential classification task, in which case the input is the sequence of

A Japanese mora is a phonological unit that determines the timing of speech. For example, the word ‘Japan’ in Japanese has two pronunciations: Ni-ho-n (3 moras) and Ni-p-po-n (4 moras).
linguistic features \( x_{1:N} = \{ x_1, \cdots , x_N \} \) and the target is the code index sequence \( l_{1:N} = \{ l_1, \cdots , l_N \} \), where \( l_n \) is the index of the code \( e_n \) for the \( n \)-th segment. Such a linker can be implemented using an RMDN with a softmax output layer. Other techniques for classification models can also be applied, for example the skip-connection [43] and dropout [44].

When the VQ-VAE uses latent codes at multiple linguistic levels, the linker must predict multiple code index sequences. However, the index sequences may differ in length because the number of linguistic segments may differ at different levels. A naive implementation is to replicate the higher-level indices to the segments at the lowest level. In the example plotted at the top of Figure 5, the mora level indices \( \{ l_m^{1}, l_m^{2} \} \) are replicated to the phones, and the linker predicts the mora and phone code indices simultaneously for every phone. Note that the alignment between different linguistic levels can be easily retrieved from the linguistic features.

By replicating the mora code indices to the phones, the naive linker treats the replicated indices as the values of different random variables and may assign them different probabilities. This model assumption is against the fact that the different random variables and may assign them different naive linker treats the replicated indices as the values of the alignment between different linguistic levels can be easily retrieved from the linguistic features.

We then show the results of comparing the proposed model with other NN-based models. The data and model configuration in Sections IV-A and IV-B we describe the evaluation of the VQ-VAE part and linker of the proposed model in Sections IV-C and IV-D respectively. We then show the results of comparing the proposed model with other NN-based \( F_0 \) models in Section IV-E.

A. Corpus and data

The experiments were conducted using the same speech corpus and configuration as in our previous study on the DAR [13]. Among the speakers in the corpus [45], we used fifty hours of recordings from a female speaker (F009). This subset contained 30,016 news-reading utterances, among which 500 were randomly selected as the validation set and another 500 as the test set. The waveform sampling rate was 48 kHz.

Natural \( F_0 \) data were extracted using an ensemble of multiple \( F_0 \) trackers with a frame shift of 5 ms [46]. The raw \( F_0 \) data were transformed to the Mel scale using \( m = 1127 \log (1 + F_0 / 700) \). The interpolated continuous-valued \( F_0 \) values were obtained after interpolating the unvoiced frames. In the case of the quantized \( F_0 \) (qF0), the Mel-scale \( F_0 \) values were quantized into 255 levels between 66 and 529 on the Mel scale, the same recipe as in our previous study [13]. The quantized \( F_0 \) values and an unvoiced symbol were encoded as a one-hot vector \( o_t \in \{ 0, 1 \}^{256} \) for each frame. The \( F_0 \) delta and delta-delta components were not used.

Linguistic features were extracted from the text using a Japanese TTS front-end called OpenTalk [47]. The basic linguistic unit is the phone, above which there are mora, word, and phrase levels. A linguistic feature vector for a phone has 386 dimensions and encodes the quin-phone identity, word part-of-speech, phrase accent type, and so on [48]. To create the input linguistic feature sequences for conventional NN-based \( F_0 \) models, the linguistic features were replicated to each frame in the phone and augmented with three additional features: the frame position in the utterance (forward and backward) and the total number of frames.

Speech waveforms for listening tests were synthesized using the WORLD vocoder [49] given natural Mel-generalized cepstral coefficients [50] (60 coefficients per frame) and band aperiordicity features (25 dimensions per frame). Natural duration was used for both model training and testing.

B. Model configuration, training, and testing

We evaluated the proposed VQ-VAE-based \( F_0 \) model with different configurations on the VQ-VAE part and linker of the proposed model in Sections IV-C and IV-D respectively. We then show the results of comparing the proposed model with other NN-based \( F_0 \) models in Section IV-E.

All models were implemented using CURRENNT [51]. The toolkit and training recipes will be available online (https://ni-yamagishilab.github.io).

We chose the number of codes based on how frequently each code was used in the validation set. While the phone-level codebook used around 128 codes, high-level codebooks used fewer codes. However, it is harmless to leave unused codes in the codebook. We also tried to increase code dimensions from 64 to 128 but found that the performance of TTS \( F_0 \) modeling did not improve.
the top-down training strategy explained in Section III-C) and the Adam optimizer with default configuration (learning rate = 0.001, \( \beta_1 = 0.9, \beta_2 = 0.999, \epsilon = 10^{-8} \)) [52].

Figure 6 also plots some of the linker configurations. In all the configurations, each highway block contained five layers that converts the input vector \( x \) into \( y = (1 - g) \odot x + g \odot \text{ReLU}(Wx + b) \), where \( g = \text{sigmoid}(W_g x + b_g) \), and \( \odot \) is the element-wise product. The dropout rate in the feedback links was set to 25% based on a pilot test. The linker was trained using conventional gradient descent with early stopping (learning rate = 10^{-3}) and further tuned using AdaGrad (learning rate = 0.001) with early stopping.

Two baseline NN-based F0 models SAR and DAR were trained in our previous study [13]. The SAR used a GMM with two mixture components to model iF0 and a binomial distribution to model the voicing status. It was initialized using a trained RMDN and fine-tuned after adding the AR dependency of order \( K = 1 \). The DAR modeled qF0 and used a dropout rate of 50% in the feedback link. It was initialized using the layer-size-dependent strategy [53] and trained from scratch.

Because both SAR and DAR are based on RNNs, we included a convolution NN (CNN) as a reference system. Specifically, we used the WaveNet [3] to model the F0 (WaveNet-F0) since its dilated convolution architecture is reported to be able to cover contexts in a long range. This WaveNet-F0 uses a similar structure and training recipe to the WaveNet vocoder in another of our studies [54]. It contained 40 dilated CNN blocks with the dilation size of the \( n \)-th block as \( 2^\text{mod}(n-1,10), n \in [1,40] \). The sizes of the residual- and skip- channels were 64 and 256, respectively. Different from the WaveNet vocoder, the WaveNet-F0 used a hierarchical softmax output layer and modeled qF0 frame by frame.

Subjective and objective tests were conducted on the test set to evaluate model performance. For the objective test, several metrics were calculated on the generated \( F_0 \) given the natural duration information, including a root mean square error (RMSE), correlation coefficient (CORR), and unvoiced/voiced (UV) classification error rate (UV err). The RMSE and CORR were calculated on frames where both natural and generated \( F_0 \)s were voiced. The subjective test is discussed in Section IV-B.

C. Pilot test I: F0 encoding-decoding using VQ-VAE

This pilot test compared VQ-VAEs at the phone, mora, word, and phrase levels. Each VQ-VAE was trained on the training set and evaluated on the test set given the natural duration of linguistic units.

Table I lists the median duration of the linguistic units at each level, which can be used to compute the ‘bit rate’ of a VQ-VAE. For example, since 13 is the median duration of the phone in frames, a phone-level VQ-VAE extracts 1/13 code per frame on average. Because the codebook size is 128 = 2^7, the bit rate of this VQ-VAE is 7/13 = 0.538 bit/frame. For reference, the bit rate of the natural quantized \( F_0 \) is 8 bit/frame since each frame encodes 255 quantized \( F_0 \) levels and an unvoiced flag.

1) VQ-VAEs using single linguistic level: This test involved seven VQ-VAEs with a single linguistic level. The first four VQ-VAEs modeled the qF0 and operated on the phone,
Because the qF0 contains the voicing status, it may be inappropriate to model it at the linguistic levels above the phone. Therefore, three additional VQ-VAEs were added to model the interpolated quantized F0, especially ‘VQ-hwpmp’, ‘VQ-wmp’, and ‘VQ-mp’ use phrase (h) + word (w) + mora (m) + phone (p), word + mora + phone, and mora + phone levels, respectively.

The network structure of VQ-hwpmp, VQ-wmp, and VQ-mp used similar structures except the linguistic level to extract latent codes.

2) VQ-VAEs using multiple linguistic levels: Based on the above results, the second experiment involved three VQ-VAEs using multiple linguistic levels: phrase + word + mora + phone (VQ-hwpmp), word + mora + phone (VQ-wmp), and mora + phone (VQ-mp). The structure of VQ-mp is plotted in Figure 6 and VQ-hwpmp and VQ-wmp had similar structures. The three VQ-VAEs were trained in a top-down manner, as explained in Section III-C1. The encoders at the phrase, word, and mora levels took the iqF0 as input. The results in Table II indicate that the VQ-VAEs using multiple levels improved the objective performance compared with VQ-p-qF0, especially on the U/V. However, the improvement due to high-level latent codes seems to be limited because most of the variation was encoded by the phone-level latent codes.
D. Pilot test II: linguistic linkers

The second pilot test focused on the linguistic linker. With a trained VQ-VAE, the latent codes were extracted from the training and validation sets and used to train a linker. The trained linker was then combined with the VQ-VAE’s decoder and codebook into a full-fledged VQ-VAE-based F₀ model. The linker’s performance, or equivalently the performance of the proposed VQ-VAE-based F₀ model, was evaluated after generating F₀ contours from linguistics features on the test set.

1) Phone-level experiment: Given the phone-level VQ-VAE model VQ-p-qF₀, we compared three linguistic linkers (LK-p-1, LK-p-2, and LK-p-3) plotted in Figure 6. In the case of LK-p-1, the phone code indices p₁₁ₖ in the training set were replicated to the frame-level as p₁₁ₖ. LK-p-1 was then trained to convert the linguistic features x₁₁ₖ into p₁₁ₖ frame by frame in the same manner as conventional NN-based F₀ models. LK-p-2, however, directly converted x₁₁ₖ to p₁₁ₖ phone by phone. LK-p-3 was identical to LK-p-2 except that LK-p-3 replaced the second feedforward layer with a bi-directional LSTM. The objective results are listed in the first three rows of Table III.

First, LK-p-1 performed worse than LK-p-2 and required much more time in training (and of course generation). As argued in Section III-A, LK-p-1 is inefficient because it processes redundant linguistic features frame by frame. In contrast, LK-p-2 operates phone by phone and can easily access the linguistic features of multiple phones. This may be the main reason for the different performances of LK-p-1 and LK-p-2. As the median duration of the phone is around 13 frames (see Table I), the time LK-p-2 spends in both forward and backward computation is only \( \frac{1}{13} \) of LK-p-1. The LK-p-3 further improved the performance of LK-p-2 by replacing a feedforward layer with a recurrent layer. Since the length of the input/output sequence is short, a recurrent layer would not increase the training or generation time too much compared with a feedforward layer.

2) Multiple-level experiment: Three linkers (LK-mp-1, LK-mp-2, and LK-mp-3) were evaluated given the phone-mora VQ-VAE (VQ-mp). The three linkers operated phone by phone. While LK-mp-1 predicted the mora and phone code indices using the naïve implementation in Figure 5, LK-mp-2 and LK-mp-3 used the mora clock. Based on LK-mp-2, LK-mp-3 used dropout (rate 5%) in all the hidden layers.

The results are listed in the middle of Table III. First, LK-mp-2 performed better than LK-mp-1 in terms of RMSE and CORR. This result supports the use of the mora clock, even though this improvement was small since one mora in Japanese usually contains one or two phones. LK-mp-3 further improved in performance over LK-mp-2, especially regarding the U/V err. This result suggests the importance of dropout for the linker. Because the number of training samples for the linker was equal to that of phones, which was only 1/13 the number of frames in the corpus, dropout may regularize the network during training.

For more linguistic levels, LK-wmp and LK-hwmp were built for VQ-wmp and VQ-hwmp. Their network structures were the same as LK-mp-3 except additional branches to predict the word and phrase code indices. They also used dropout in hidden layers as LK-mp-3 did. However, the results in Table III indicate that using the phrase and word levels did not improve F₀ modeling performance. This result may be reasonable because the word and phrase latent codes were not informative, as suggested from pilot test I in Section IV-C.

E. Comparing proposed VQ-VAE-based F₀ model with baseline models

The results of the pilot tests indicate that VQ-mp with LK-mp-3 performed the best among different configurations. We refer to the proposed VQ-VAE-based model using this configuration as VQ-VAE (MP3) and compared it with the baseline NN-based F₀ models. As the results in Table IV indicate, VQ-VAE (MP3) achieved better RMSE and CORR scores even though the U/V err. increased. The improved RMSE and CORR scores may be the result of the unit-by-unit processing of linguistic features in the linker. The U/V err. increased because VQ-VAE (MP3) tended to treat a whole unit as either being voiced or unvoiced, which is shown in the analysis of latent codes in Section IV-D. This phone-level U/V classification caused more errors around the phone boundaries than the frame-level U/V classification conducted using conventional NN-based F₀ models.

A mean-opinion-score (MOS) test was conducted to compare the perceptual quality of the generated F₀. This test involved 109 paid native Japanese speakers. Each participant listened to the samples and evaluated their quality in terms of intonation using a score from 1 (unnatural) to 5 (natural). In each testing round, one vocoded speech sample and the synthetic samples from each model were played in a randomly shuffled order. In total, 1702 testing rounds were conducted. The results plotted in Figure 9 indicate that VQ-VAE (MP3) slightly outperformed the DAR, even
Fig. 9. Results of subjective evaluation. Numbers in table denote $p$-values calculated using two-sided Mann-Whitney U test.

Fig. 10. $F_0$ contours generated using baseline models and proposed VQ-VAE-based $F_0$ model given linguistic features of one test utterance.

though the difference is not statistically significant. The results also indicate that WaveNet-F0 and SAR performed worse than VQ-VAE (MP3). The performance of SAR was expected because it only modeled local $F_0$ dependency.

The reader may wonder whether VQ-VAE (MP3) performed well because of its large and deep network structures, particularly the linker. In fact, VQ-VAE (MP3) had a smaller number of model parameters (1.11M = VQ-VAE 0.44 + linker 0.67). Since the VQ-VAE encoder is not used during $F_0$ generation, the parameter of VQ-VAE (MP3) becomes smaller when it is used for $F_0$ generation (0.93M = VQ-VAE decoder&codebook 0.26 + linker 0.67). The results also suggest that the mapping between linguistic features and $F_0$ patterns may be more difficult than $F_0$ encoding-decoding. It may be better to assign more parameters to the linker.

Even though the linker is larger and deeper than the VQ-VAE part, it operates at the segment rate rather than frame rate. It is easier for the linker to cover a large linguistic context, as we argued before. Furthermore, the linker would not significantly increase the training and generation time because the number of segments in one utterance is much smaller than the number of frames. In our implementation, the linker part $L_k$=mp-3 only costs 0.019 ms out of the 0.147 ms that VQ-VAE (MP3) costs in generating one frame of $F_0$.

A conventional $F_0$ model such as DAR is less efficient because it spends extra time processing the redundant linguistic features frame by frame. Neither does it factorize the $F_0$ modeling task nor use a specific network structure to process the linguistic features. This may be the reason it used more parameters but did not outperform VQ-VAE (MP3).

$F$: Visualization of latent $F_0$ code space

Since the proposed VQ-VAE-based $F_0$ model has shown promising results, it is interesting to investigate the ‘meaning’ of the latent codes learned using the VQ-VAE. For this analysis, the codewords from the phone or mora codebooks of VQ-VAE (MP3) were compressed to two dimensions using t-SNE. Its VQ-VAE encoder was then used to extract the code indices from an $F_0$ contour in the test set. The results are plotted in Figure 11(a), where the top and bottom sub-figures show the results of the phone and mora codes, respectively.

At the mora level, the code indices assigned to the first part of the $F_0$ contour were {108, 119, 59, 13, 97, 20, 53}. The location of these codes generally reflects the average $F_0$ height of the corresponding linguistic unit. For example, the mora with the code 108 contained an $F_0$ peak, and the following moras contained a decreasing $F_0$ curve. Accordingly, the code sequence 108 $\rightarrow$ 59 $\rightarrow$ 13 $\rightarrow$ 20 $\rightarrow$ 53 formed a line starting from the right-bottom corner of the code space and ending at the left-top corner, except code 97 where the $F_0$ curve slightly increased. On the second part of the $F_0$ contour, we can observe that the $F_0$ curve increased at first, reached a plateau, and finally decreased. The corresponding code sequence {114, 110, 8, 40, 4, 123} started at the center of the code space, reached the right-bottom corner, and moved to the left-top corner.

Similar to the case at the mora level, the phone-level codes generally learned the average $F_0$ height of phones. More interestingly, some of the codes seemed to also encode the unvoiced status and were found in the right-hand side manifold in the phone-code space, e.g., the code indices {114, 46, 126, 119, 102} in the phone-code space of Figure 11.

The above results indicate that the VQ-VAE encoder at the phone or mora level mainly encodes the skeleton of the $F_0$ contour, e.g., average $F_0$ height and voicing status, while the decoder fills in the detailed $F_0$ variations. The average $F_0$ height may be a general representation to encode the $F_0$ contour at the phone or mora levels.

Analysis on the latent space at the word or higher levels did not show patterns as regular as those observed at the phone and mora levels. For example, Figure 11(b) plots the results for the word-level latent space in VQ-wmp, which is difficult to see meaningful patterns. One hypothesis is that the latent

\footnote{We also trained a smaller DAR with a number of parameters equal to 1.08 million. However, while the generation speed was still around 0.185 ms/frame, the RMSE and CORR degraded to 30.01 and 0.890, respectively.}
Our proposed model is by no means the only model to avoid the frame-by-frame processing of linguistic features. Sequence-to-sequence models [61], [62] may also be used for the \( F_0 \)-modeling task. Compared with a sequence-to-sequence \( F_0 \) model, however, our proposed model can explicitly use the linguistic boundaries rather than learning the alignment from scratch, which may ease the learning process. It is also interesting to introduce sequence-to-sequence models in the linker part of the proposed model.

VI. Conclusion

We investigated the issue of model efficiency for NN-based \( F_0 \) models in TTS systems. Although we previously proposed the DAR, which outperformed an RNN-based \( F_0 \) model, this DAR processes the linguistic features frame by frame in the same manner as the RNN-based model. Because frames within the same linguistic unit carry the same input linguistic features, the frame-by-frame processing of linguistic features is unnecessary. It also prevents the model from easily retrieving linguistic features of the neighboring units.

To improve model efficiency, we proposed a VQ-VAE-based \( F_0 \) model that consists of two components. The first component is an \( F_0 \) contour model that generates the \( F_0 \) contour based on sparse latent codes of linguistic units. To jointly learn this component and latent codes, we proposed to use the VQ-VAE framework and estimate the model parameter and codebooks together with additional encoders. Experiments showed that the meaningful latent codes can be learned at the phone and mora levels, and these codes can be used to encode and decode the \( F_0 \) contours quite accurately.
Given the latent codes extracted using the VQ-VAE encoder on the training set, the second component of the proposed model, which is referred to as the linker, can be easily trained as a sequential classification model. This linker only converts the linguistic features into a latent code for each linguistic unit. It operates much faster than the layers of a conventional NN-based \( F_0 \) model that processes the linguistic feature frame by frame. By combining a linker that predicts mora and phone latent codes and the corresponding VQ-VAE decoder and codebooks, the proposed VQ-VAE-based \( F_0 \) model outperformed the DAR in objective tests and performed equally well in subjective tests. The proposed VQ-VAE-based \( F_0 \) model is also smaller in model size and faster in training and \( F_0 \) contour generation.

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