On the sensitivity of generic porous optical sensors

Citation for published version:

Digital Object Identifier (DOI):
10.1364/AO.51.002752

Link:
Link to publication record in Edinburgh Research Explorer

Document Version:
Publisher's PDF, also known as Version of record

Published In:
Applied optics

Publisher Rights Statement:
This paper was published in Applied Optics (Vol. 51, Issue 14, pp. 2752-2758, 2012) and is made available as an electronic reprint with the permission of OSA. The paper can be found at the following URL on the OSA website: http://www.opticsinfobase.org/ao/abstract.cfm?uri=ao-51-14-2752. Systematic or multiple reproduction or distribution to multiple locations via electronic or other means is prohibited and is subject to penalties under law.

General rights
Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy
The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.
On the sensitivity of generic porous optical sensors

Tom G. Mackay

School of Mathematics and Maxwell Institute for Mathematical Sciences, University of Edinburgh, Edinburgh EH9 3JZ, UK
Nanoengineered Metamaterials Group, Department of Engineering Science and Mechanics, Pennsylvania State University, University Park, Pennsylvania 16802, USA
(T.Mackay@ed.ac.uk)

Received 12 January 2012; revised 15 February 2012; accepted 20 February 2012; posted 22 February 2012 (Doc. ID 161371); published 10 May 2012

A porous material was considered as a platform for optical sensing. It was envisaged that the porous material was infiltrated by a fluid that contains an agent to be sensed. Changes in the optical properties of the infiltrated porous material provide the basis for detection of the agent to be sensed. Using a homogenization approach based on the Bruggeman formalism, wherein the infiltrated porous material was regarded as a homogenized composite material, the sensitivity of such a sensor was investigated. For the case of an isotropic dielectric porous material of relative permittivity $\epsilon_a$ and an isotropic dielectric fluid of relative permittivity $\epsilon_b$, it was found that the sensitivity was maximized when there was a large contrast between $\epsilon_a$ and $\epsilon_b$; the maximum sensitivity was achieved at midrange values of porosity. Especially high sensitivities may be achieved for $\epsilon_b$ close to unity when $\epsilon_a \gg 1$, for example. Furthermore, higher sensitivities may be achieved by incorporating pores that have elongated spheroidal shapes. © 2012 Optical Society of America

OCIS codes: 280.4788, 260.2065, 160.1245.

1. Introduction

A simple generic optical sensor may be envisaged as porous material (labeled $a$, say), which is infiltrated by a fluid (labeled $b$, say). An agent to be sensed is contained within the fluid. It assumed that the fluid and the agent to be sensed have quite different optical properties. Thus, the concentration of the agent within the fluid may be gauged by the optical properties of the infiltrated porous material [1-3]. The optical properties used to detect the presence of the agent may be the reflectances or transmittances of the infiltrated porous material. Alternatively, if one surface of the porous material were coated with a thin metallic film, measurements could be based on the excitation of surface-plasmon-polariton (SPP) waves at the interface of the porous material and metal film [4-6].

For example, sculptured thin films (STFs) represent rather promising porous materials for such optical sensors [7-9]. These constitute parallel arrays of nanowires that are grown on substrates by physical vapor deposition [10-11]. By controlled manipulation of the substrate during the deposition process, a range of nanowire shapes can be achieved. Thereby, the multiscale porosity of such STFs can be tailored to order, to a considerable degree. Additionally, since STFs can be fabricated from a wide range of organic and inorganic materials, a wide range of optical properties for the porous material can be delivered [12,13]. Chiral STFs are especially interesting for optical sensing applications, as these support the circular Bragg phenomenon, courtesy of the helical nature of their nanowires [10]; furthermore, they also support more than one mode of SPP wave [14-16], which may be usefully exploited for sensing [17].

In the design of such an optical sensor, what values should one choose for the optical properties of the porous material and infiltrating fluid, in order to maximize sensitivity? What value should one choose for the porosity, and what shape should one choose for the pores, in order to maximize sensitivity? These
are the questions that we address here. We do so by considering the simplest scenario wherein the porous material and infiltrating fluid are both made from lossless, homogeneous, isotropic dielectric materials, characterized by relative permittivities \( \epsilon^a \) and \( \epsilon^b \), respectively \([18]\). The infiltrated porous material is regarded as a homogeneous composite material (HCM), which is a reasonable approximation provided that the linear dimensions of the pores are much smaller than the wavelength(s) involved. Thus, in the case of optical sensors operating at visible wavelengths, we have in mind pore linear dimensions \( \lesssim 38 \text{ nm} \) for the smallest values of \( \epsilon^a,b \) considered and \( \lesssim 10 \text{ nm} \) for the largest values of \( \epsilon^{a,b} \) considered. The infiltrated porous material may be either isotropic or anisotropic depending upon the shape of the pores. We use the well-established Bruggeman homogenization formalism to estimate the relative permittivity dyadic of the infiltrated porous material, namely, \( \epsilon^{Br} \) \([19-20]\). The Bruggeman formalism has recently been implemented to study the prospects of infiltrated STFs as optical sensors \([21]\), based on both changes in reflectance/transmittance \([22]\) and SPP wave excitation \([17,23]\).

Regardless of whether the sensor is based on changes in reflectance/transmittance or the excitation of SPP waves, the sensitivity of the sensor depends crucially on how much the optical properties of the infiltrated porous material change in response to changes in the optical properties of the infiltrating fluid. Thus, the dyadic derivative \( d\epsilon^{Br} / d\epsilon^b \) is a key indicator of sensitivity. In the following we explore how this derivative varies as a function of the porosity, the pore shape, and the relative permittivities of the infiltrating fluid and the porous material.

2. Homogenization Theory

Within our homogenization framework, the pores are all assumed to have the same shape, which is spheroidal in general. These spheroidal pores are randomly distributed but identically oriented. The surface of each spheroid relative to its centroid is prescribed by the vector \([20]\)

\[
r_s(\theta, \phi) = \eta \mathbf{U} \cdot \mathbf{r}(\theta, \phi),
\]

with \( \mathbf{r} \) being the radial unit vector originating from the spheroid’s centroid, specified by the spherical polar coordinates \( \theta \) and \( \phi \). The linear dimensions of the spheroid, as determined by the parameter \( \eta \), are assumed to be small relative to the electromagnetic wavelength(s). The spheroidal shape is captured by the dyadic

\[
\mathbf{U} = \mathbf{U}_\perp \mathbf{I} + (\mathbf{U}_\parallel - \mathbf{U}_\perp) \hat{\mathbf{c}} \hat{\mathbf{c}},
\]

where \( \mathbf{I} \) is the identity \( 3 \times 3 \) dyadic and the unit vector \( \hat{\mathbf{c}} \) is parallel to the spheroid’s axis of rotational symmetry. The linear dimension parallel to \( \hat{\mathbf{c}} \), relative to the equatorial radius of the spheroid, is provided by the shape parameter \( \rho = U_\parallel / U_\perp \).

A schematic illustration of such a spheroidal pore is provided in Fig. 1.

The form of the relative permittivity dyadic \( \epsilon^{Br} \), as estimated using the Bruggeman homogenization formalism, mirrors that of the shape dyadic \( \mathbf{U} \). That is, it has the uniaxial form

\[
\epsilon^{Br} = \epsilon^{Br}_\parallel + (\epsilon^{Br}_\parallel - \epsilon^{Br}_\perp) \hat{\mathbf{c}} \hat{\mathbf{c}}.
\]

It emerges as the solution of the dyadic Bruggeman equation \([24,25]\)

\[
f_a \epsilon^{a} + f_b \epsilon^{b} = 0,
\]

where \( 0 \) is the null \( 3 \times 3 \) dyadic. The scalars \( f_a \) and \( f_b = 1 - f_a \) denote the respective volume fractions of the porous material and infiltrating fluid. Thus, \( f_b \) represents the porosity of the optical sensor. The dyadics

\[
\epsilon^{\ell} = (\epsilon^{\ell}_\parallel - \epsilon^{Br}) \cdot [\mathbf{I} + D \cdot (\epsilon^{\ell}_\parallel - \epsilon^{Br})]^{-1} \quad (\ell = a,b),
\]

are the polarizability density dyadics of the spheroids in the HCM, while the depolarization dyadic \( \mathbf{D} \) in Eq. (5) is given by the double integral \([26,27,28]\)

\[
\mathbf{D} = \frac{1}{4\pi} \int_0^{2\pi} d\phi \int_0^{\pi} d\theta \sin \theta \left( \frac{1}{\mathbf{r} \cdot \mathbf{U}^{-1} \cdot \epsilon^{Br} \cdot \mathbf{U}^{-1} \cdot \mathbf{r}} \right) \times \mathbf{U}^{-1} \cdot \mathbf{r} \cdot \mathbf{U}^{-1}.
\]

It may be expressed in the uniaxial form

\[
\mathbf{D} = D_\parallel \mathbf{I} + (D_\parallel - D_\perp) \hat{\mathbf{c}} \hat{\mathbf{c}},
\]

with components

\[
D_\parallel = \frac{\gamma}{\epsilon^{Br}_\parallel} \Gamma_\parallel(\gamma),
\]

10 May 2012 / Vol. 51, No. 14 / APPLIED OPTICS 2753
\[ D_\perp = \frac{1}{e^\perp} \Gamma_\perp(\gamma), \]  

(9)

wherein the terms

\[ \Gamma_\parallel(\gamma) = \frac{1}{4\pi} \int_0^{2\pi} d\phi \int_0^\pi d\theta \frac{\cos^2 \phi \sin^3 \theta}{\cos^2 \theta + \sin^2 \theta (\gamma \cos^2 \phi + \sin^2 \phi)}, \]  

(10)

\[ \Gamma_\perp(\gamma) = \frac{1}{4\pi} \int_0^{2\pi} d\phi \int_0^\pi d\theta \frac{\sin^2 \phi \sin^3 \theta}{\cos^2 \theta + \sin^2 \theta (\gamma \cos^2 \phi + \sin^2 \phi)}, \]  

are functions of the scalar parameter

\[ \gamma = \frac{U_\perp^2 e^\perp}{U_\parallel^2 e^\parallel}. \]  

(12)

The double integrals on the right sides of Eqs. (10) and (11) may be evaluated as

\[ \Gamma_\parallel(\gamma) = \begin{cases} \frac{\sinh^{-1} \sqrt{\frac{\gamma}{(1-\gamma)^2}}} {1-\gamma} - \frac{1}{1-\gamma} & \text{for } 0 < \gamma < 1, \\ \frac{1}{1} & \text{for } \gamma > 1. \end{cases} \]  

(13)

\[ \Gamma_\perp(\gamma) = \begin{cases} \frac{1}{2} \left( \frac{1}{1-\gamma} \sinh^{-1} \sqrt{\frac{\gamma}{(1-\gamma)^2}} \right) & \text{for } 0 < \gamma < 1, \\ \frac{1}{2} \left( \frac{1}{1-\gamma} \sinh^{-1} \sqrt{\frac{\gamma}{(1-\gamma)^2}} \right) & \text{for } \gamma > 1. \end{cases} \]  

(14)

Notice that the anomalous case \( \gamma < 0 \), which represents a hyperbolic HCM [29], is excluded from our consideration.

The dyadic Bruggeman equation [Eq. (4)] yields the two nonlinear scalar equations

\[ \frac{\epsilon^a - \epsilon^\parallel^b}{1 + D_\parallel(\epsilon^a - \epsilon^\parallel^b) f^a} + \frac{\epsilon^b - \epsilon^\parallel^b}{1 + D_\parallel(\epsilon^b - \epsilon^\parallel^b) f^b} = 0, \]  

(15)

\[ \frac{\epsilon^a - \epsilon^\perp^b}{1 + D_\perp(\epsilon^a - \epsilon^\perp^b) f^a} + \frac{\epsilon^b - \epsilon^\perp^b}{1 + D_\perp(\epsilon^b - \epsilon^\perp^b) f^b} = 0. \]  

(16)

which are coupled via \( D_\perp \). Using standard numerical techniques, this pair can be solved for \( \epsilon^\parallel^b \) and \( \epsilon^\perp^b \).

Let us turn to the dyadic derivative that provides a measure of the sensitivity of the porous optical sensor under consideration, namely,

\[ \frac{d\epsilon^\parallel^b}{d\epsilon^b} = \frac{d\epsilon^\parallel^b}{d\epsilon^b} I + \left( \frac{d\epsilon^\parallel^b}{d\epsilon^b} - \frac{d\epsilon^\parallel^b}{d\epsilon^b} \right) \hat{c} \hat{c}. \]  

(17)

Before proceeding further, we observe that the corresponding derivatives of the depolarization dyadic components may be expressed as

\[ \frac{dd^\parallel}{d\epsilon^b} = \nu_{11} \frac{d\epsilon^\parallel^b}{d\epsilon^b} + \nu_{12} \frac{d\epsilon^\parallel^b}{d\epsilon^b}, \]  

(18)

\[ \frac{dd^\perp}{d\epsilon^b} = \nu_{21} \frac{d\epsilon^\perp^b}{d\epsilon^b} + \nu_{22} \frac{d\epsilon^\perp^b}{d\epsilon^b}, \]  

(19)

with the scalars

\[ \nu_{11} = \frac{U_\perp^2}{U_\parallel^2 e^\parallel} \left( \Gamma_\parallel + \gamma \frac{d\Gamma_\parallel}{d\gamma} \right) - \frac{\gamma \Gamma_\parallel}{(e^\parallel)^2}, \]  

(20)

\[ \nu_{12} = -\frac{U_\perp^2}{U_\parallel^2 (e^\parallel)^2} \left( \Gamma_\parallel + \gamma \frac{d\Gamma_\parallel}{d\gamma} \right), \]  

(21)

\[ \nu_{21} = \left( \frac{U_\perp^2}{U_\parallel^2 (e^\parallel)^3} \right) \frac{d\Gamma_\perp}{d\gamma} - \frac{\Gamma_\perp}{(e^\parallel)^2}, \]  

(22)

\[ \nu_{22} = -\left( \frac{U_\perp^2}{U_\parallel^2 (e^\parallel)^3} \right) \frac{d\Gamma_\perp}{d\gamma} - \frac{\Gamma_\perp}{(e^\parallel)^2}. \]  

(23)

and derivatives

\[ \frac{d\Gamma_\parallel}{d\gamma} = \begin{cases} \frac{1}{2} \left[ \frac{3\sinh^{-1} \sqrt{\frac{\gamma}{(1-\gamma)^2}} - 1}{(1-\gamma)^2} \right] & \text{for } 0 < \gamma < 1, \\ \frac{1}{2} \left[ \frac{1+2\gamma - 3\sec^{-1} \sqrt{\frac{\gamma}{(1-\gamma)^2}}}{(1-\gamma)^2} \right] & \text{for } \gamma > 1. \end{cases} \]  

(24)

\[ \frac{d\Gamma_\perp}{d\gamma} = \begin{cases} \frac{1}{2} \left[ \frac{3}{(1-\gamma)^2} - \frac{1}{2(1+2\gamma) - 3\sec^{-1} \sqrt{\frac{\gamma}{(1-\gamma)^2}}} \right] & \text{for } 0 < \gamma < 1, \\ \frac{1}{2} \left[ \frac{3}{(1-\gamma)^2} - \frac{1}{2(1+y) - 3\sec^{-1} \sqrt{\frac{\gamma}{(1-\gamma)^2}}} \right] & \text{for } \gamma > 1. \end{cases} \]  

(25)

Next we exploit the scalar Bruggeman equations [Eqs. (15) and (16)]. Their derivatives with respect to \( \epsilon^b \) may be written as

\[ \beta_{11} \frac{d\epsilon^\parallel^b}{d\epsilon^b} + \beta_{12} \frac{d\epsilon^\perp^b}{d\epsilon^b} + \beta_{13} = 0, \]  

(26)

\[ \beta_{21} \frac{d\epsilon^\parallel^b}{d\epsilon^b} + \beta_{22} \frac{d\epsilon^\perp^b}{d\epsilon^b} + \beta_{23} = 0, \]  

(27)

with

\[ \beta_{11} = \nu_{11} \left( \epsilon^a - \epsilon^\parallel^b \right) \left( \epsilon^b - \epsilon^\parallel^b \right) + D_\parallel \left( 2\epsilon^\parallel^b - \epsilon^a - \epsilon^b \right) - 1, \]  

(28)

\[ \beta_{12} = \nu_{12} \left( \epsilon^a - \epsilon^\parallel^b \right) \left( \epsilon^b - \epsilon^\parallel^b \right), \]  

(29)
\[
\beta_{13} = f_b + D_\parallel (e^a - e^{Br}) , \tag{30}
\]

\[
\beta_{21} = \nu_{21} (e^a - e^{Br}) (c^b - e^{Br}) , \tag{31}
\]

\[
\beta_{22} = \nu_{22} (e^a - e^{Br}) (c^b - e^{Br}) + D_\perp (2e^{Br} - e^a - e^{Br}) - 1 . \tag{32}
\]

\[
\beta_{23} = f_b + D_\perp (e^a - e^{Br}) . \tag{33}
\]

Thus, the sought after derivatives of \(e^{Br}\) and \(e^{Br}\) finally emerge as

\[
\frac{de^{Br}}{de^b} = \frac{\beta_{12}\beta_{23} - \beta_{22}\beta_{13}}{\beta_{11}\beta_{22} - \beta_{12}\beta_{21}} , \tag{34}
\]

\[
\frac{de^{Br}}{de^b} = \frac{\beta_{23} - \beta_{11}\beta_{22} - \beta_{12}\beta_{21}}{\beta_{11}\beta_{22} - \beta_{12}\beta_{21}} . \tag{35}
\]

3. Numerical Investigations

The consequences of the theory presented in the previous section are illustrated here by means of some numerical examples. We begin with the simplest case in Subsection 3.A, wherein the pores are spherical and the infiltrated porous material is accordingly considered to be an isotropic HCM. Then the effects of anisotropy are considered in Subsection 3.B, wherein the pores are taken to be spheroidal in shape. For the purposes of these numerical calculations, our attention is restricted to relative permittivity values which, at optical frequencies, are attainable either using naturally occurring materials or currently available engineered materials. In Section 4, the results of implementing relative permittivity values that lie beyond the reach of present-day technology are commented upon.

A. Spherical Pores

If the pores are spherical (i.e., \(\rho = 1\)), then the relative permittivity dyadic characterizing the infiltrated porous material reduces the scalar form \(e^{Br} = e^{Br}\parallel\) with \(e^{Br} = e^{Br}\parallel = e^{Br}\). For \(e^a\in\{1.5, 5, 15\}\), the Bruggeman estimate \(e^{Br}\parallel\) and its derivative \(de^{Br}/de^b\) are plotted versus \(e^b\in\{1, 3\}\) and \(f_b\in\{0, 1\}\) in Fig. 2. We see that, when \(e^a = 1.5\), the Bruggeman estimate \(e^{Br}\parallel\) varies approximately linearly with \(e^b\) for all \(f_b\in\{0, 1\}\). However, the relationship between \(e^{Br}\parallel\) and \(e^b\) becomes increasingly nonlinear as \(e^a\) increases. For \(e^a = 1.5\), the derivative \(de^{Br}/de^b\) increases in an approximately linear fashion as the porosity \(f_b\) increases, regardless of the value of \(e^b\). However, for \(e^a = 5\), the trend is rather different: here the values of \(de^{Br}/de^b\) peak at \(f_b = 0.7\) and the height of this peak rises as \(e^b\) decreases. This peak in the value of \(de^{Br}/de^b\) becomes more pronounced as the value of \(e^a\) increases. Indeed, at \(e^a = 15\), this peak can be clearly observed even when \(e^b = 3\).

B. Spheroidal Pores

Let us now explore what happens when the pores are taken to be spheroidal. Accordingly, the HCM representing the infiltrated porous material is a uniaxial dielectric material. Following our findings in Subsection 3.A, we fix \(e^a = 15\) in order that the effects of pore shape are more clearly appreciated. The Bruggeman estimates \(e^{Br}\parallel\) and their derivatives \(de^{Br}/de^b\) are plotted versus \(e^b\in\{1, 3\}\) and \(f_b\in\{0, 1\}\) in Fig. 3 for \(\rho = 10\). Both \(e^{Br}\parallel\) and \(e^{Br}\perp\) vary relatively little as \(e^b\) increases, but both decrease—\(e^{Br}\parallel\) approximately linearly and \(e^{Br}\perp\) more nonlinearly—as \(f_b\) increases. The derivative \(de^{Br}/de^b\) increases approximately uniformly as \(f_b\) increases, for \(e^b \geq 1.5\). However, the values of \(de^{Br}/de^b\) for \(e^b \lesssim 1.5\) are slightly peaked around \(f_b \approx 0.9\). The plot of \(de^{Br}/de^b\) is similarly peaked, but, in this case, the peak occurs at \(f_b \approx 0.5\); it is larger in height than the \(de^{Br}/de^b\) peak, and it extends further into the \(e^b \geq 1.5\) region. Also, the height of this \(de^{Br}/de^b\) peak is substantially larger than the corresponding peak in \(de^{Br}/de^b\) observed in Fig. 2 for \(e^a = 15\).

The pores represented in Fig. 3 are prolate spheroids. The corresponding case of oblate spheroids is represented in Fig. 4. The parameters for the plots in Fig. 4 are the same as those in Fig. 3, except that \(\rho = 0.1\). The plot of \(e^{Br}\parallel\) versus \(e^b\) and \(f_b\) in Fig. 4 is very similar to the corresponding plot of \(e^{Br}\parallel\) in Fig. 3, and likewise for the plots of \(e^{Br}\parallel\) in Fig. 4 and \(e^{Br}\parallel\) in Fig. 3. Also, the plots of the derivatives \(de^{Br}/de^b\) and \(de^{Br}/de^b\) versus \(e^b\) and \(f_b\) in Fig. 4 are similar to the corresponding plots of \(de^{Br}/de^b\) and \(de^{Br}/de^b\), respectively, in Fig. 3, albeit there are qualitative differences in the positions and shapes of the peaks in the derivative plots.

4. Discussion and Closing Remarks

An analysis based on the Bruggeman homogenization formalism has provided insights into the sensitivity of a generic porous optical sensor. Specifically, for a porous material of relative permittivity \(e^a\) infiltrated by a fluid of relative permittivity \(e^b\), we found that:

- the sensitivity is maximized when there is a large contrast between \(e^a\) and \(e^b\);
- if the contrast between \(e^a\) and \(e^b\) is large, maximum sensitivity is achieved at midrange values of porosity;
- higher sensitivities may be achieved for \(e^b\) close to unity when \(e^a \gg 1\), for example; and
- higher sensitivities may be achieved by incorporating elongated pores.

In Section 3 the relative permittivities of the porous material considered were \(e^a\in\{1.5, 5, 15\}\). These values correspond to many common dielectric materials at optical frequencies, with the largest value being close to the relative permittivity of silicon.
for example. The relative permittivities of the infiltrating fluid were taken to be in the range $1 < \epsilon_b < 3$. This range is physically realizable, with the largest values corresponding to nanocomposite fluids developed for immersion lithography [30], whereas values approaching unity may be attained by using water vapor [31], for example. We note that ongoing rapid developments in engineered materials are bringing relative permittivity parameter regimes, which were hitherto unattainable, into reach [32,33]. For example, relative permittivities in excess of 50 are now being reported for engineered materials in the terahertz frequency regime [34,35], while engineered materials with positive-valued relative permittivities less than unity also appear to be attainable [36–38]. Accordingly, it is of interest to consider how the sensitivities reported here would be affected if rather more exotic parameter regimes were incorporated. In further numerical studies (not presented in Section 3) it was observed that increasing $\epsilon_a$ beyond 15 results in a steady increase in sensitivity. Reducing the value of $\epsilon_b$ from unity results in a sharp increase in sensitivity. In this context, let us make a couple of parenthetical remarks. First, since the entire analysis presented herein is isomorphic to the corresponding scenario for magnetic materials (with relative permittivities replaced by relative permeabilities throughout), we note that relative

Fig. 2. (Color online) Bruggeman estimate of the relative permittivity of the infiltrated porous material $\epsilon^{Br}$ plotted versus the relative permittivity of the infiltrating fluid $\epsilon^b \in (1,3)$ and the porosity $f_b \in (0,1)$, for the relative permittivity of the porous material $\epsilon^a \in \{1.5,5,15\}$. Also plotted are the corresponding derivatives $d\epsilon^{Br}/d\epsilon^b$. 
the relative permittivity of the infiltrating fluid is a variable quantity (which varies according to concentration of the agent to be sensed), whereas the other design parameters remain fixed. Accordingly, the value of the relative permittivity of the fluid should be carefully chosen such that the sensitivity is maximized over the expected range of concentrations of the agent to be sensed.

While our attention here has been confined to infiltrated porous materials represented as uniaxial dielectric HCMs, a straightforward extension of the presented analysis could accommodate biaxial dielectric HCMs that represent certain STFs as optical sensors [17,22,23].

Finally, the study described herein provides a step toward a comprehensive study of porous platforms for optical sensing, which incorporates such matters as the absorption/desorption phenomena that dictate the response time and the reversibility of the sensors.

The author thanks two anonymous referees for their helpful comments and suggestions.

References and Notes


18. The entire analysis presented herein may also be applied to lossless, homogeneous, isotropic magnetic materials, by replacing relative permittivities by the corresponding relative permeabilities throughout.


