The complex chemical Langevin equation

Citation for published version:

Digital Object Identifier (DOI):
10.1063/1.4885345

Link:
Link to publication record in Edinburgh Research Explorer

Document Version:
Publisher's PDF, also known as Version of record

Published In:
Journal of Chemical Physics

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Rapid engineering of versatile molecular logic gates using heterologous genetic transcriptional modules

Volume 50 Number 79 11 October 2014 Pages 11601–11770
We designed and constructed versatile modular genetic logic gates in bacterial cells. These function as digital logic 1-input Buffer gate, 2-input and 3-input AND gates with one inverted input and integrate multiple chemical input signals in customised logic manners. Such rapidly engineered devices serve to achieve increased sensing signal selectivity.

Biomolecular computing is an emerging computing paradigm that has the potential of combining both the sensing and processing of biochemical signals to generate autonomous programmed output readout and action.\(^1,2\) Great progress has been seen in this area which typically applies enzymes,\(^3,4\) DNA\(^5,6\) or RNA\(^7\) in an in vitro biochemical system to execute complex logic computing tasks. For example, a DNA and restriction enzyme-based in vitro diagnostic automaton detected multiple biochemical disease indicators where the final positive state only forms under a predesigned logic combination of the inputs.\(^8\) More recently, live cells have hosted various in vivo logic computing tasks such as AND\(^9–11\) and XOR\(^12,13\) gates functionalities owing to the vast array of functions available to a living cell.\(^14\) However, the present capabilities for implementing complex logic computing functions in live cells are rather limited, since few well-characterised and versatile genetic building blocks are available.\(^14\) In addition, most of the devices constructed so far are designed to use specific inputs to drive specific outputs, which make them difficult to incorporate and reuse in other cellular circuit programs.

To address these bottlenecks, we present the rapid engineering of versatile modular molecular logic gates in model Escherichia coli bacteria via repurposing some heterologous genetic transcriptional modules. These modules exist in vast numbers amongst many different bacterial species, offering a largely untapped resource. As an example, we designed various modular logic devices using transcriptional modules from the hrp (hypersensitive response and pathogenicity) gene regulation system for Type III secretion in Pseudomonas syringae (Fig. 1).\(^15,16\) In the hrp gene regulatory architecture (Fig. 1), the activator proteins HrpR and HrpS form a high-order co-complex which binds the upstream activator sequence of the \(\sigma^{32}\)-dependent hrpL promoter to remodel the closed \(\sigma^{34}\)-RNA-P-hrpL transcription complex to an open one through ATP hydrolysis, while negative regulation by the HrpV occurs through its direct interaction with HrpS.\(^17\)

Since the hrp system comprises multiple components that interact and regulate each other in a defined logic manner, we considered that multiple-input combinational logic devices should be constructed based on their existing regulatory relationships. Accordingly three modular logic devices, including the digital logic 1-input Buffer gate, 2-input and 3-input AND with one inverted input gates, were designed using subsets of the hrp regulatory network (Fig. 1). The device inputs and

![Fig. 1. Versatile modular molecular logic gates (1-input Buffer, 2-input and 3-input AND) engineered in Escherichia coli using the heterologous hrp transcriptional modules from Pseudomonas syringae plant pathogen.](image-url)
outputs are promoters. The output promoter is only turned on when a specific logic combination of input promoters is active. One distinct advantage of the device design is the modularity (reusability), i.e. the inputs are exchangeable and can be connected to different environment-responsive promoters whilst the output may be wired to drive various other useful genes. Moreover, the genetic components used are heterologous to *E. coli* and thus less likely to interfere with the host endogenous genetic programs which will enable these logic devices to behave more robustly in their working contexts.

We first designed the single-input digital Buffer gate which functions as an amplifier for the input signal to achieve increased output expression capability for downstream connected logic modules. The Buffer gate does not change the logic relationship between the input and output, but instead acts as an isolator and enhancer that can transform the input signal to a higher amplitude signal to match the input requirement of the aligned output modules.

The Buffer gate was built to express from an operon the cooperative activator proteins HrpR and HrpS with *hrpL* as the output promoter (Fig. 2). The high order HrpRS assemblies synergistically activate the downstream tightly controlled σ54, dependent *hrpL* promoter, thus assisting amplification of the transcriptional input signal. To characterise the device, the input was connected to an arsenic responsive promoter and the output to a *gfp* (green fluorescent protein) reporter. The input promoter alone was first systematically characterised as its output, in the presence of arsenite and produced a mild output response (Fig. S1 and S2, ESI†). In contrast, when the Buffer gate was applied, the output significantly increased to a much higher level (~9 fold) under the same 2 μM NaAsO2 input induction (Fig. 2). The characterised responses under different arsenite levels help establish that the device behaves well as a digital logic Buffer gate (Fig. S1, ESI†). The Buffer gate can be used to increase the sensitivity of transcription-based biosensors (e.g. the arsenic sensor in this study) as well as to modulate the amplitude of an input signal to facilitate the coupling and matching of genetic modules with vastly different input–output strengths.

We next designed the double-input AND gate with one inverted input, a digital logic device that only produced an observable output when the 1st input is present and the 2nd input is absent (Fig. 3). The function is equivalent to the combination of connecting a NOT gate to one input of a canonical AND gate. The device can be used to improve the selectivity of biochemical sensors such that they will only generate a valid readout under the specific logic combination of the two chosen sensing chemicals.

The double-input AND gate above was built by expressing from an operon HrpR and HrpS, under the control of the non-inverted input and expressing separately the inhibitor HrpV under the inverted input (Fig. 1). To characterise the device, we connected the non-inverted input to the arsenic responsive promoter (Fig. S2, ESI†) and the inverted input to a mercury responsive promoter (Fig. S3, ESI†) whilst the final output was the *gfp* reporter. To achieve a close to zero off-state behaviour, we used a weak RBS (ribosome binding site, rbs32, Table S1, ESI†) ahead of the activator *hrpS* gene but a strong RBS (rbs30) ahead of the inhibitor *hrpV* gene. As a result, HrpV inhibitor will be expressed in excess over the activator HrpRS complex when both inputs are activated, leading to complete inhibition of the output *hrpL* promoter. The characterisation result shows that the device only produced an observable output when NaAsO2 (16 μM) is present and HgCl2 (4 μM) is absent among the four possible logic combinations of the two chemical inputs (Fig. 3). These outcomes establish the effectiveness of the digital logic AND gate having one inverted input function.

Extending from the double-input AND gate, we designed the triple-input AND gate with one inverted input, a combinational digital logic device that should only produce an output when the first two inputs are present and the third input is absent (Fig. 4). The predicted function is equivalent to that of connecting...
building blocks to expand the currently limited parts kit for gene circuit engineering.14

The genetic logic devices described here have particular advantages including the tight unactivated off state attributed to the underlying σ54-dependent strict transcriptional activation requirement.19 The high-order co-dependent HrpRS complexes employed in the system contribute to the sharp switching between the off and on states of the devices, resulting in digital-like response behaviour. Moreover, these devices are modular and can, potentially, be easily connected to other modules to construct larger and more complex systems with advanced functions.

This work was supported by a BBSRC project grant [BB/K016288/1] and a Royal Society research grant award [RG120527] to B.W.

Notes and references