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Hierarchy of Scales in Language Dynamics

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Abstract. Methods and insights from statistical physics are finding an increasing variety of applications where one seeks to understand the emergent properties of a complex interacting system. One such area concerns the dynamics of language at a variety of levels of description, from the behaviour of individual agents learning simple artificial languages from each other, up to changes in the structure of languages shared by large groups of speakers over historical timescales. In this Colloquium, we survey a hierarchy of scales at which language and linguistic behaviour can be described, along with the main progress in understanding that has been made at each of them—much of which has come from the statistical physics community. We argue that future developments may arise by linking the different levels of the hierarchy together in a more coherent fashion, in particular where this allows more effective use of rich empirical data sets.

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1 Introduction

In 1972, Anderson famously articulated the idea that “more is different” [1]: that the emergent consequence of fundamental physical laws at one scale lead to new physical laws at a larger scale, and ones that are to be regarded as fundamental as those that apply at the smaller scale. In physics, statistical mechanics provides the conceptual and methodological framework to build the bridge between the dynamics at the larger scale and the interactions between the constituents at the smaller scale.

A good illustration of this procedure is provided by the two steps of coarse-graining that sit between the classical Hamiltonian dynamics of point particles and the Navier-Stokes equations for fluids. The first step is to shift from a description in terms of individual particles to one in terms of classes of particles, for example, all those at a similar point in space and with a similar velocity (see e.g. [2]). This trick, pioneered by Maxwell to determine the equilibrium distribution of particle velocities [3], reduces the dimensionality of the problem by a factor of $N$, the number of particles in the system. Since $N$ is extremely large (order $10^{23}$ or more) for macroscopic systems, this is an impressive reduction in complexity. However it comes at a cost: the full dynamics take the form of an infinite hierarchy of equations, each of which requires a solution for all of the others in order to be solved. To break this vicious circle, a physical insight is needed. Specifically, the molecular chaos assumption (employed by both Maxwell [3] and Boltzmann [4] with varying degrees of explicitness) amounts to a statement that the details of collisions between particles is less important than their overall effect, which is taken to eliminate correlations between pairs of particles. The Boltzmann equation that results is a non-linear equation that describes the population dynamics of particles and their movements between different classes. A further step of averaging yields coarse-grained density and velocity fields. Again, this step generates a hierarchy of equations which can be truncated by appealing to a physical insight, namely that the macroscopic fields of interest vary slowly on the length- and timescales of the microscopic particle dynamics [5]. We thus arrive at the Navier-Stokes equation, which is highly non-linear and can describe extremely rich physical states, such as turbulence, whose existence is unimaginable in the original Hamiltonian formulation.

The fact that Hamiltonian equations of motion lie at the bottom of this hierarchy is incidental to the statistical mechanical coarse-graining procedure. The crucial component is the physical insight that allows certain aspects of the dynamics at one level of the hierarchy to be replaced with an effective description that makes progress towards understanding the next level possible. There is no reason that such insights should be the preserve of condensed matter physics. Indeed, Anderson’s hierarchy extended from particle physics to the social sciences, passing through cell biology and psychology on the way. It should therefore come as no surprise—nor concern—that the reach of statistical physics has profitably expanded into the biological [6,7] and sociological [8] domains. Furthermore, in line with Anderson’s position, exploring these applications areas often raises new fundamental questions in nonequilibrium statistical mechanics.
One area that has received growing attention from statistical physicists over the past fifteen years or so is the quest for a quantitative understanding of language dynamics. Human language exhibits complexity at multiple scales in at least two dimensions. First, language itself exhibits complex structure at the level of sounds, words and sentences through *phonology* (which specifies how sounds may be combined), *morphology* (how meaningful combinations of sounds may be further combined to make words) and *syntax* (how sentences are formed) [9]. At each level, the specific set of valid combinations varies from one language to the next: for example, the order with which words with a specific function appear in a sentence is not the same in every language (as we will discuss further in Section 2 below). At the same time, variation is not completely arbitrary: for example, some word orders are more common across the world’s languages than others. Meanwhile, each language changes over time at all levels of organisation, leading on occasion to predictable phenomena like vowel shifts [10] and the unidirectional character of grammaticalisation [11], whereby words with more concrete meanings (like objects and actions, represented by nouns and verbs) take on more abstract grammatical functions (like relationships between objects, represented by prepositions) over time, whilst the reverse process is extremely rare [12].

2 Variation in language structure

As noted above, languages vary in their structure at all levels of organisation. A useful resource for studying similarities and differences between languages is the World Atlas of Language Structure (WALS [13]) which specifies up to 192 features (for example, the size of the consonant inventory or the number of genders) across over 1000 languages. This database reinforces the findings of typological research [14] that whilst considerable variation is evident in the structure of different languages, this variation is not unconstrained. An illustrative example is basic word order, which concerns the order that the subject (S), object (O) and verb (V) appear in a sentence. Although all six orderings would convey the same information, the two patterns that have the subject in the first position characterise around 90% of the languages in WALS. This highly non-uniform distribution over the possible states of a language is referred to as a *typological universal*. More sophisticated universals also exist [14], in particular *implicational universals*, whereby the presence of one structure in a language tends to imply another structure: for example, if adjectives precede nouns, it is very likely (around 90% probability) that demonstratives also precede nouns [13].

At the largest length and timescales we can think of each language as a single coherent unit, and defined in terms of some set of $F$ features. For simplicity, let each of these features be discrete such that feature $f$ takes one of $m_f$ distinct values, denoted $\sigma_f$. For example, in the case of basic word order, $\sigma_f$ takes one of six values. At this level of description, the state of a language is fully specified by the vector $\sigma = (\sigma_1, \sigma_2, \ldots, \sigma_F)$. The first type of typological universal then corresponds to a nonuniform distribution over the set of possible states $\{\sigma\}$, while implicational universals correspond to correlations between components of the vector $\sigma$. In this framework, one can postulate (at least) two possible explanations for these typological universals. The first is that some states $\sigma$ are more stable than others: for example, languages that place the subject first are less likely to change than those that have it in a different position. The second is to acknowledge that (like species) languages may have common ancestors (for example, French and Romanian are descendants of Latin), and hence correlations between the states of different languages can be attributed to a common historical period. The main method to discriminate such explanations is phylogenetic analysis (see e.g. [15] for a review in the context of cultural evolution).

The basic idea is to assume first of all that the historical evolution of languages can be modelled as a tree within which branches occur at points in time where an ancestor language splits into two daughters—see Figure 1. On top of this tree structure, a stochastic model for the changes in state that occur is superimposed. A natural choice is a time-homogeneous Poisson process wherein the probability that a language in state $\sigma$ changes to state $\sigma'$ in a time interval $dt$ is

$$P_d(\sigma' | \sigma; t) = \omega(\sigma' | \sigma) dt ,$$

(1)
i.e., that the rate of change from one state to another is constant in time across all branches of the tree. Sampling from this distribution gives a set of points at which changes in state occurred, shown as circles on the branches in Figure 1. From the stochastic model for changes in state, one can compute the likelihood of arriving at the current distribution of languages (given a common ancestor and specific tree structure). Then, using Bayesian statistics, one can infer a posterior distribution of the parameters in the model, which includes the tree structure and the transition rates between language states. It is also possible to incorporate further constraints where information is known, for example, points in history where a language split occurred.

Since sampling the full parameter space to obtain posterior distributions is computationally demanding, it is only recently that these methods have become widely-used. Prior to this, other methods—such as maximum parsimony methods—were used to infer the relationships between different languages [16]. In this context, maximum parsimony corresponds to the sequence of events with the smallest number of changes in state. Initial studies [16,17] focussed on the lexicon (i.e., the set of words available to speakers to express meanings). The idea is the closely-related languages have more words in common than distantly-related languages. More formally, one can define cognate sets that comprise words from different languages that are judged to have the same form for the same meaning [9]. In this context, each feature \( f \) corresponds to one of the cognate sets, and \( \sigma_f = 0 \) or 1 depending on whether the language in question appears in cognate set \( f \). A change in state then corresponds to a language entering or leaving a cognate set.

One obvious question is whether it is reasonable to assume that relationships between languages form a tree-like structure, as in Figure 1. Evidence in favour of this assumption was provided by Gray et al [16]: the most parsimonious tree was more consistent with an ‘express-train’ hypothesis where languages were established during a rapid process of colonisation of successive ‘stations’ in the Pacific by Austronesian-speaking populations, as opposed to an ‘entangled bank’ hypothesis characterised by a high degree of contact between the different languages.

This work thus opened the door to a wide range of quantitative inferences about the history of languages. Key findings include support for the theory that Indo-European languages originated in Anatolia around 8,000–9,500 years ago [17,18] and that inferences based on the structure of the sound system, word order and other grammatical features allows reconstruction to greater time depths than is possible with the lexicon, and specifically that Papuan languages diverged over 10,000 years ago [19]. These findings continue with a number of studies on the rate of language change. The rate of lexical change has been found to vary by up to two orders of magnitude, and to be correlated with the frequency of word use [20] and population size [21]. In both cases the data are suggestive of a power-law dependence of the rate on the explanatory variable. A power law relationship between the rate of verb regularisation and verb frequency was also found from a corpus of English texts [22]. Here, however, the statistical physicist will likely be disappointed that the exponents of the power laws relating the rate of language change to the frequencies of different linguistic units are not the same: this suggests that the underlying mechanisms generating these mechanisms may not be universal—at least in a strict statistical physics sense.

Most relevant to questions about the origin of typological universals, and in particular the question of whether more common structures are also more stable, are two studies of word-order universals [23,24]. Of these two studies, that of Maurits and Griffiths [24] is conceptually more straightforward. Here, the authors find that despite SOV word order being slightly more common than SVO order in the contemporary distribution of languages (at 48% and 41% respectively [13]), the historical rates of change between the two orders are indistinguishable, suggesting that they are in fact of equal stability. Dunn et al [23] meanwhile investigate the more subtle question of implicational universals. Here, the hypothesis is that if the orders of two word classes (say adjective-noun and demonstrative-noun) are found to be correlated in the contemporary distribution, one would expect to see a similar correlation in the historical rates of change of these two structures. Only two of the correlations expected from the contemporary distribution were observed in the historical dynamics of more than one language family. Furthermore, most of the dynamical correlations that were identified were present in a single language family.

This latter result suggests that factors specific to individual cultures contribute to the dynamics that give rise to typological universals. However, at this level of description, it does not pinpoint what these factors might be. Some clues are provided by investigations of correlations between language structures and quantities that vary between cultures: of these, two studies [25,26] have been particularly prominent—in part due to a degree of controversy. Dediu and Ladd [25] presented evidence that two genes related to brain structure potentially contribute towards a cognitive bias that disfavours linguistic tone.
(the use of pitch to distinguish words) in the process of language acquisition. Meanwhile, Lupyan and Dale [26] demonstrated an inverse relationship between language size (as measured number of speakers or geographical area) and structural complexity across 28 distinct features (e.g., the number of cases): in other words, that more widely-spoken languages tend to be less complex. Further clues might emerge by appealing to the dynamics of language at a lower level of description.

3 Languages competing for speech communities

The model of language in the previous section made explicit reference only to its structure (as defined by a set of features). Any influence of the underlying population of speakers was incorporated at best implicitly, for example, by allowing the transition rates between states to depend on culture-specific factors like its size (as was done in [21]). In all of these studies, interactions between distinct languages, other than the possibility that they share an ancestor, were ignored. By descending a level into the hierarchy, we can investigate interactions between languages mediated by the groups of speakers using them. Note that in order to distinguish from any other social groups (e.g., populations of a country) we shall use the term speech community (borrowed from linguistics) to describe a social group with a common language.

The obvious example of an interaction between two or more languages is where they are spoken in the same geographical area, and thereby compete for a common pool of speakers. The Celtic languages (Welsh, Scottish and Irish Gaelic, Cornish and Manx) that spoken alongside English within the British Isles provide an example of such a set [27]. The increasing dominance of English over the Celtic languages—to the extent of extinction in the case of Cornish and Manx—is evidence of competition between them that is independent of the population dynamics in the relevant regions, since neither region suffered a mass population extinction in the relevant historical period. Rather it is the process of language shift, whereby individual speakers switch from one language to another through a variety of mechanisms [28], that is believed to explain such declines.

A seminal model of language shift was proposed by Abrams and Strogatz [29]. It is couched in terms of the fractions \( x \) and \( y = 1 - x \) of a population speaking two languages \( X \) and \( Y \) respectively. The fraction of speakers who shift from \( Y \) to \( X \) per unit time is denoted \( P_{YX} \) and is taken to depend on the size, \( x \), of speech community of \( X \) and a quantity \( 0 \leq s \leq 1 \) that encodes the ‘status’ of \( X \). The status of \( Y \) is given implicitly by \( 1 - s \), so for \( s > \frac{1}{2} \), \( X \) has a higher status than \( Y \). Ignoring all fluctuations, one arrives at an ordinary differential equation for \( x \) of the form

\[
\frac{dx}{dt} = xP_{YX}(x, s) - xP_{XY}(x, s).
\]

The transition rates \( P_{XY}(x, s) \) and \( P_{YX}(x, s) \) are not independent. If the size and status of a language are the only factors that affect the competition between them, we must obtain the same dynamics under relabelling of \( X \) and \( Y \). This implies that \( P_{XY}(x, s) = P_{X}(1-x, 1-s) \). Under the further mild assumptions that \( P \) languages with no speakers are not spontaneously re-invented; (ii) that a language with zero status is never shifted towards; and (iii) that \( P_X(x, s) \) increases monotonically in both arguments, the fixed points of (2) can be determined. One finds that there are always two stable fixed points at \( x = 0 \) and \( x = 1 \), corresponding to extinction of \( X \) and \( Y \) respectively, and a third fixed point that corresponds to coexistence of both languages. This latter fixed point is always unstable, implying that one of the two languages is doomed to extinction. Which of the two languages that is destined for this fate depends on the initial condition.

Although extremely simple, this model provides a number of valuable insights. First, Abrams and Strogatz [29] showed that the model can be fit to time-series data for a variety of languages. To achieve this, they chose the form of the transition rate to be \( P_{XY}(x, s) = csx^a \), where \( a \), \( c \) and \( s \) are a set of parameters fit separately to each linguistic time series (along with \( x(0) \)). The value of the exponent \( a \approx 1.3 \) was reported to be fairly robust across the languages, although little was said about the remaining parameters. Nevertheless, this appears to allow confident prediction of the fate of a minority language, and in particular the timescale over which extinction may be expected. From a theoretical perspective, the most interesting parameter in this model is \( s \), the social status of language \( X \). The thinking here is that speakers have some awareness of the opportunities afforded to them by their choice of language, for example, to improve their own personal wealth. At this level of description, however, the precise mechanism by which this awareness is gained is left unspecified.

The main value of Abrams and Strogatz’ model is the limited range of outcomes it predicts under broad but reasonable assumptions. In particular, the fact that coexistence of two languages of different social status is impossible in this framework has motivated many extensions of the basic model, a number of which are reviewed in greater detail elsewhere, e.g. [30,31]. There are at least two ways in which two languages of unequal status can coexist. The first is to assume that initially the languages are spoken in different regions and only then mediate contact between them by diffusion of speakers of one language into the geographical region in which the other was originally spoken [32]. This mechanism works because Eq. (2) has stable fixed points at \( x = 0 \) and \( x = 1 \), i.e., when either of the two languages is the only one being spoken. This stability implies a small incursion of speakers of the other language can be tolerated. What is interesting about this result is that demonstrates the possibility for a globally disfavoured language (the one with the lower status) to survive alongside the high-status language.

Is there any way in which two languages of different status might coexist at the same point in space? This was
shown to be possible if one combines the process of language shift in the Abrams-Strogatz model with a process of reproduction that causes both the population size to grow and for the offspring to inherit the language of its parents [33]. In common with many other models of population growth, this model featured a carrying capacity which limits the maximum size of the population [34]. However, in [33] a separate carrying capacity was assigned to each speech community, meaning that when the region is saturated by speakers of language X, it can nevertheless continue to accommodate speakers of language Y. It turns out that it is this assumption that facilitates coexistence. If one instead assumes that the overall size of the combined population, comprising both speech communities, is limited by a carrying capacity, which is reasonable if they compete for the same set of resources to sustain their population, the possibility of coexistence is removed [35]. It is however possible to engineer coexistence if the relative social status of the two languages is different in different parts of space, which could plausibly arise because ultimately the status is a subjective judgement made by individual speakers, and consequently different groups of speakers could reach different judgements. Taking the results from this body of research together, it seems that the usual outcome of language competition is for a dominant language to drive others to extinction, unless there is some spatial symmetry-breaking present, either in the initial condition or through variation of an external factor like social status. This generalisation also applies in the presence of noise, which can be seen from individual-based models that incorporate the same mechanisms as the Abrams-Strogatz model [104]. The main departure from this generalisation is found under external interventions that are explicitly designed to prevent extinction of declining languages, such as embedding them in the school curriculum [36].

4 Emergence of a common language

In the discussion so far, a language has been defined at the speech community level, for example, as a set of structural features that are characteristic of the language as a whole, and help to differentiate it from languages spoken by different groups of people. Nevertheless, there is considerable variation in the way language both between different members of a speech community and within the set of utterances produced by a single individual [9, 37, 38]. In common with structural variation between languages, this variation exists at all levels of linguistic complexity: speakers can differ in the way they pronounce the same word or a syllable that appears in a class of words, in the word they use to convey a given meaning, or in the way they construct sentences. This variation may arise in a number of different ways [37]. For example, one property of language is its open-endedness which confers on speakers the ability to express propositions that they have never articulated or heard before. This entails producing new words or recombining words in a new way. At the same time, speakers may adjust their set of grammatical rules, perhaps to achieve greater internal consistency of the system (e.g., by regularising an irregular verb). Alternatively, words and phrases may enter one language by borrowing from another (see, for example, the German word *ansatz* that is widely used by physicists, and whose precise meaning is hard to convey efficiently in English).

These innovations explain why some unconventional forms may coexist alongside the conventional forms that characterise a language at the speech community level. However, these conventions also change over time, as we have seen in Section 2. An important question relates to the mechanism by which these innovations, which are created in interactions between small numbers of agents, are propagated and result in a change in a language’s macroscopic state. By now, this is a very well-studied problem in statistical physics, with progress having been very comprehensively reviewed fairly recently [8]. It is also worth noting that the field of sociolinguistics is devoted to understanding variability in language use, the factors that result in one variant form being used over another, and how these factors contribute to language change [38].

In order to discuss this large body of work in a consistent fashion, we shall adopt Croft’s evolutionary framework for language change initially set out in [37]. This identifies three distinct dynamical processes that contribute. The first is replication, which is the reproduction of structures (e.g., sounds, words or a particular ordering of word classes in a sentence). The second is innovation, which may take the form of a completely novel utterance or (more likely) some small change to a structure as it is replicated (e.g., putting words in a different order in order to suggest a novel meaning to the listener). The third process is selection, which is the preferential replication of one structure over another. Later works [39,40] introduce a distinction between two types of selection: *interactor selection*, whereby certain individual members of the speech community have a greater influence on a speaker’s behaviour than others, and *replicator selection*, whereby one structure is systematically replicated in preference to another by a speaker or a group of speakers.

Given pre-existing variation, replication acting without any further innovation or selection taking place leads to random changes in the frequencies of different structures that is mathematically equivalent to the process of genetic drift [41]. We review one of the paradigmatic models of replication, the Moran model, in the next section below. We then discuss how the dynamics are affected by the addition of biases which include selection and frequency-dependent effects. We then complete this section with a discussion of innovation.

4.1 The Moran model of replication dynamics

For simplicity, we consider the case where some linguistic structure takes one of two variant forms, A and B. As noted previously, A and B might refer to two different pronunciations of the same sound, two different words for an object, or two different grammatical rules with the same function (e.g., marking the past tense). Initially we shall
also assume that every member of the speech community uses either A or B categorically (and not some variable mixture of the two, although we will find that these two cases are in fact closely related). We now define the Moran model of replication [42] as it applies to a speech community of \( N \) speakers with no spatial structure—see also Figure 2. In each elementary timestep, a pair of individuals is chosen at random from the speech community to interact. One of these individuals is designated as the speaker and the other as the listener. The speaker produces an utterance that allows the listener to identify whether the speaker is a user of variant A or variant B. As a result of the interaction, the listener adopts the same variant as that used by the speaker. The Moran model thus serves as a simple mathematical description of accommodation, a process where interacting agents serve to align their linguistic behaviour [43].

A stochastic equation of motion for this model can be derived fairly straightforwardly [41]. First, let \( x \) be the fraction of the \( N \) agents in the speech community who use variant A. In order for \( x \) to change in one timestep, the speaker–listener pair must comprise one A and one B user. Then \( x \) increases or decreases by \( 1/N \) with equal probability. Consequently, the expected change in \( x \) is zero, and the stochastic process is purely diffusive. The rate of diffusion is obtained by examining the mean square change in \( x \) per timestep: this is \( 2x(1-x)/N^2 \). This allows one to write down the Fokker-Planck equation [44]

\[
\frac{\partial}{\partial t} P(x,t) = \frac{1}{A(N)} \frac{\partial^2}{\partial x^2} x(1-x) P(x,t),
\]

(3)

where \( P(x,t) \) is the probability that a fraction \( x \) of the speech community are users of A at time \( t \) given some initial condition, and the timescale \( A(N) = N^2 \) for the Moran model. Formally, this equation is exact in the limit \( N \to \infty \) under rescaling of time \( \tau = t/A(N) \).

There are many related models of replication which are described by (3) for an appropriate definition of the variant frequency \( x \) and characteristic timescale \( A(N) \).

The earliest such model, introduced independently by Fisher [45] and Wright [46], pre-dates the Moran model by around 20 years, and describes changes in gene frequencies for species where generations do not overlap. Since in this case \( N \) replication events occur concurrently, the characteristic timescale is \( A(N) = 2N \) (i.e., order \( N \) shorter than in the Moran model, where replication events occur one-by-one). When individuals are placed on the sites of a square lattice, and speaker–listener pairs are restricted to neighbouring sites of the lattice, we obtain the voter model [47] (although it was not actually referred to as such until a later work [48]). When the number of spatial dimensions exceeds two, the Fokker-Planck equation adequately describes the dynamics of the total fraction of sites \( x \) in state A, and the characteristic timescale \( A(N) \) is proportional to the number of sites. In two dimensions, we also have (3), but where now \( A(N) \) is proportional to \( N \ln(N) \). On small-diameter networks, one yet again obtains (3), but here the characteristic timescale \( A(N) \) may scale sublinearly (or indeed superlinearly) with \( N \) depending on the network’s degree distribution and the procedure for choosing a speaker and listener in each interaction [49–53]. In this case, it is also necessary to replace \( x \) with a weighted average of a variant’s frequency over the nodes of the network. Finally, the Fokker-Planck equation (3) also applies in the case where agents are variable users of the variants A and B, and \( x \) gives the probability that an agent uses variant A in an interaction; this yields the utterance selection model [54]. In this model, the set of \( N \) variable units comprises a memory of stored tokens of these units (e.g., realisations of a sound, or words with a common meaning). A speech event comprises \( T \) independent draws from the stored memory. Both speaker and listener may replace items in their store with copies of the variants produced in the interaction, with different probabilities depending on who produced the utterance—see Figure 2. The feedback of a speaker’s own behaviour into their store means that a speaker’s usage frequencies fluctuate even in the absence of any listeners: in this case, one...
reverses the Moran model and (3) applies for the speaker’s usage frequency \( x \). In the generalisation to multiple speakers, the form (3) applies at long timescales, again under a suitable choice \( A(N) \) and averaging of the individual agents’ variant frequencies to form a collective frequency \( x \) [51,52].

Having established that the Moran model, as described by the Fokker-Planck equation (3), can model linguistic variation at different levels of linguistic structure within and between speakers in different spatial geometries, we now ask what it predicts. The equation (3) is exactly solved for arbitrary initial condition [55], and therefore its dynamics are well understood. In particular it is known that eventually one of the two variants that are initially present will go extinct in a finite time. This is reminiscent of the Abrams and Strogatz’ result for language competition, which showed that one of the competing languages is destined for extinction. Even without solving the equation (3), it is clear that any timescale—including that of extinction—will be proportional to \( A(N) \). Typically this timescale increases with the speech community size, although on highly heterogeneous social networks it can remain finite even in the limit of an infinite speech community [49,51]. The relationship between fixation time and the speech community size has proven crucial in evaluating descriptive theories of language change. For example, it was argued that a process of accommodation—whereby speakers seek to align their behaviour to each other in order to be better understood [43]—was sufficient to explain the structure of new English language dialects [56].

Whilst this is true of the final state of the language that is reached in the Moran model, the slow diffusion towards fixation is difficult to reconcile with the rapid rate at which such dialects are seen to form [39].

### 4.2 Biased replication

We now turn to the case where replication of pre-existing variant structures is biased. We consider two paradigms, both related to the Moran model, in which biases naturally arise. The first is the utterance selection model, defined above, in which individual speakers may exhibit variability. The second is the iterated learning model, and will be introduced below. In the case of the utterance selection model, recall that the frequency \( x \) in the model specifies the frequency with which a single speaker uses variant A. As described above (see also Figure 2), utterances are produced by sampling from the set of \( N \) tokens stored in a speaker’s memory.

One way that replication may be biased is if the frequency that a speaker uses a variant differs from its frequency among the tokens stored in memory. For example, a speaker may apply a bias in favour of the variant with the highest frequency in the store (see Section 5 below for reasons why this might be the case for real human language behaviour). If the stored frequency is \( x \), we can define the production frequency \( f(x) \) as \( f(x) = x + \alpha \beta(x) \), where \( \beta(x) \) is the bias and \( \alpha \) is the strength of that bias.

If we continue to work within a framework where a variant is not spontaneously re-created once it has gone extinct, this means that \( \beta(0) = \beta(1) = 0 \). Moreover, if we assume that there is no systematic preference towards one of the two variants (i.e., replicator selection), we must also have \( \beta(x) = -\beta(1-x) \). The lowest order polynomial with these properties is \( \beta(x) = x(1-x)(2x-1) \). In the regime where the bias is small, it contributes a drift term to the Fokker-Planck equation (3) but leaves the diffusion term unchanged. The resulting Fokker-Planck equation can be written as a Langevin equation

\[
\dot{x}(t) = \alpha \beta(x) + \sqrt{x(1-x)} \eta(t)
\]

where \( \eta(t) \) is a Gaussian white noise with zero mean and variance \( 1/A(N) \), and the multiplicative noise is interpreted in the Ito sense [44,57]. The generalisation to multiple speakers on a square lattice takes the form

\[
\dot{x}(t) = \sum_j \eta_j (x_j - x_i) + \alpha \beta(\alpha) + \sqrt{x_i(1-x_i)} \eta_i (t)
\]

where \( x_i \) is the frequency of variant A in speaker \( i \)’s memory, \( \eta_j \) specifies the extent to which speaker \( i \)’s memory is affected by the tokens produced by their neighbours \( j \) (see Figure 2), and \( \{ \eta_i (t) \} \) is a set of independent Gaussian white noise terms. We can recognise the first term as a discretised Laplacian operator, and hence this term describes a spatial diffusion.

It turns out that there is a rather subtle interaction between the three terms in (5). The first term seeks to make speakers more similar to each other (in the spirit of accommodation theory). The second and third terms both serve to eliminate variability, either systematically (by biasing in favour of the more frequent variant in memory) or stochastically (by sampling the tokens in the finite memory story for production). The strength of the Gaussian noise decreases as \( N \) is increased. Thus for large \( N \), one expects the noise to act as a weak perturbation on the deterministic part of the dynamics, which in turn is closely related to the Ginzburg-Landau model of coarsening in the Ising model with non-conserved order parameter. Indeed, Ising-like coarsening is observed at low noise strengths (at least on square lattices [58]). However, for small \( N \), the multiplicative nature of the noise acts as a strong perturbation on the dynamics to the extent that it in fact changes the universal properties of the coarsening dynamics from that of the Ising model to that of the voter model [58]. In more concrete terms, this means that when memory is short, speakers tend to exhibit categorical behaviour (because the strong noise tends to cause extinction at the level of individual speakers), and regions where speakers exhibit similar behaviour grow logarithmically in time. On the other hand, when memory is long, speakers exhibit variable behaviour and regions of similar behaviour grow as a power-law in time. It is worth noting that one would not necessarily expect the same coarsening behaviour to apply to every aspect of linguistic behaviour, as the strength of the coupling between speakers, the bias and memory lifetime may vary on a case-by-case basis.
Based on this result, we might speculate that for
generic biases we expect there to be two regimes, one in
which the noise serves to eliminate the bias and the phe-
nomenology of the voter model is recovered, and one in
which the noise is sufficiently weak that the deterministic
limit of (5) can be used to gain insights into the fate of
variation under different types of bias. This latter regime
was investigated systematically in [40] by appealing to the
different symmetry principles the biases may have. Asym-
metry may arise separately in the coupling between speak-
ers in (5), that is when the parameters $h_{ij}$ in (5) satisfy
$h_{ij} \neq h_{ji}$, or in the form of the bias function $b(x)$, for ex-
ample by taking $b(x) = x(1-x)$ which consistently favours
variant $A$. These correspond to implementing interactor
selection and replicator selection separately. It is found
that only the latter asymmetry provides a robust mecha-
nism for reproducing the widely-observed S-curve pattern
of language change, whereby the overall frequency of an
innovation in the speech community tends to track a sig-
noidal shape (such as a logistic function) as it propagates
and establishes itself as a new convention [40]. It is this
kind of bias that can transform variation at the level of
individual speakers, and translate it into a change in the
macroscopic state of the language which was the funda-
mental dynamical process modelled at the topmost level
of the hierarchy (see Section 2). However, this model of
language change remains incomplete. For the propagation
mechanism to work, the majority of speakers in the speech
community must consistently favour one of the variants
(e.g., $A$) over the other. Why this should be the case is
difficult to explain without more detailed understanding of
the origin and the nature of biases on linguistic behaviour,
which we discuss in more detail in Section 5 below.

Another—perhaps more fundamental—puzzle with a
model like that defined by (5) is how to achieve stabil-
ity of multiple dialects within a single speech community.
This is related to the problem of obtaining stable coexis-
tence between two languages discussed in Section 3, and
the reasons are in fact somewhat similar. Suppose that
the bias in (5) is such that for some group of neighbour-
lying individuals, the state of consensus (where all $x_i = 1$
or all $x_i = 0$ within this group) is stable. Then, if bi-
ases are uniform across the speech community, the state
of global consensus will be stable. On way to achieve (at
least metastable) coexistence of both variants across dif-
ferent members of the speech community is if the biases
vary from one place to another, i.e., if one subset of indi-
viduals systematically boosts the frequency of one variant
while another subset systematically boosts the frequency
of the other variant. This is analogous to one of the pro-
posed mechanisms for achieving coexistence of different
languages. However, it is problematic, because in order to
explain how behaviour (like language) that is visible to
other agents may spatially separate, we need to explain
how biases towards a specific linguistic behaviour, that
may be somewhat less visible, to other agents themselves
separate. Iterating this argument, one may arrive at an in-
finitely hierarchy of increasingly obscure ‘meta-biases’, each
of which will have needed to have spatially separated in
order to permit separation at the more visible levels. Stud-
ies in the related area of opinion dynamics [8] suggest one
possible way to close this hierarchy, which is to incorpo-
rate a feedback whereby agents preferentially interact with
those agents who behave in a similar way to themselves.
Separation into groups that exhibit their own distinctive
behaviour is seen in three classes of model that implement
this idea, namely Brownian agents that diffuse towards
regions of similar opinion [59], Deffuant-type models of
bounded confidence [60] where agents whose opinions dif-
er by more than a certain amount have no effect on each
other and the Axelrod model [61] and derivatives where
agents exhibit multiple variable traits and the probability
a pair of agents interacts depends on how many traits they
have in common. In the language of Croft et al [37,39,40],
this corresponds to a feedback between two type different
types of selection they identified, namely replicator and
interactor selection.

We now turn to the second paradigmatic class of mod-
els that relate to the Moran model of replication: the itera-
ted learning model. These have mainly been researched
within the linguistics community: see [62,63] for reviews
from that perspective. Each individual in a group of agents
is characterised in terms of a grammar—a set of rules that
governs their linguistic productions. Where there are two
possible grammars, we can denote them $A$ and $B$, as in the
Moran model defined above in Section 4.1. The dynamics
of the iterated learning model are usually formulated as
follows. A naïve agent is exposed to the utterances gener-
ated by an experienced agent’s grammar. The task of this
naïve agent is to infer a suitable grammar ($A$ or $B$ in the
case of two grammars), at which point they become an ex-
perienced agent. This agent may then serve as a model for
one (or more) naïve agents to learn from. We can think of
this as a replication process, in that grammars are repli-
cated from one generation to the next: however, changes
may occur in replication due to the fact that more than
one grammar may be compatible with the set of utterances
that the learner was exposed to. Biases may be present in
production or learning that result in certain grammars
being favoured over others as they are replicated: these
thus mirror the biases discussed above in the context of
language use and the utterance selection model. Indeed,
a more formal connection between the iterated learning
model and the utterance selection model was made in the
case where a grammar specifies the frequency with which
two variant forms should be used. Here it was shown that if
agents employ a Bayesian learning algorithm after hearing
$N$ tokens of a variable structure, the estimated frequency
$x$ is governed by the Langevin equation (4) with a bias
that can act either in favour or against categorical use of
a single variant, depending on the prior expectations of
the language learner and the number of tokens heard [64].

The main purpose of iterated learning models is to
understand processes by which an initially unstructured
language may acquire structure after many generations of
learning. Of particular interest are properties that are
thought to transcend all languages. These design features
[65] include the fact language is productive (i.e., the ability
to articulate a novel thought and be understood by a listener) and compositional (i.e., that the meaning of an utterance can be understood from the meanings of the component parts). It seems likely that these two features are related: for example, compositionality provides a means by which language can be productive. What is less obvious is that a pressure on speakers to be productive can promote the emergence of compositional structure.

This effect was demonstrated within an iterated learning model with the space of grammars defined in such a way that agents could express a set of structured meanings (e.g., objects that have a shape and a colour) in either a holistic way (i.e., with no relation between the structure of the signal and meaning) or a compositional way (where the component parts of the meaning can be understood from the component parts of the signal) [66]. The bias responsible for the emergence of structure lies in the production part of the interaction. The experienced agents have no control over which meanings they are required to express when providing training data to naïve agents: thus if the amount of data that is presented at each generation is small, agents may be confronted with meanings for which they have never heard a signal. Under these conditions, it is found that grammars that allow components of signals to be recombined are favoured by iterated learning. In more abstract terms, one might think of this as a competition between minimising the number of distinct signals in the grammar and maximising the ability to convey arbitrarily complex meanings. Such a competition may perhaps be related to guiding principles, such as the principle of least effort [67] and the principle of uniform information density [68], which could potentially be investigated within this modelling framework.

### 4.3 Innovation

The modelling of replication dynamics is greatly simplified if one knows in advance all possible variants of linguistic structure that may come into existence as the system evolves. Then, the state space is of fixed dimension, and one can (for example) extend the Moran model and its relatives to a larger number variants. Indeed, the multivariant generalisation of (3) is exactly solvable if the rate at which an agent spontaneously innovates a given variant $A_i$ is independent of the state of the system [69]. Technically, this is because there is no current in the steady state: at some level, the dynamics is in the same class as that for physical systems at thermal equilibrium. All other models of innovation generate non-equilibrium steady states, and we are not aware of any exact solutions for the multivariant Moran model in this case.

The situation is even more complex when arbitrarily many variants can be created, as is the case for language, given its design feature of productivity. For the case where replication of existing variants is unbiased, and where new variants (each of which has never been seen before) are innovated at a constant rate, one arrives at the infinite-alleles model in population genetics for which some exact results are available [70,71]. A more straightforward approach—and one that allows easier connection to human behaviour—is Monte Carlo simulation. A large body of such work centres on the problem of a speech community reaching consensus on a name for a novel object. Here the paradigmatic model is the naming game [72], in which agents each maintain a lexicon of words that they recognise as a possible label for an object. Initially, this lexicon is empty for all agents. The dynamics proceeds by repeatedly choosing a speaker-listener pair at random from the speech community. The speaker presents a name for the object to the listener: in the case where the speaker’s lexicon is empty, a completely new name is invented on the spot; otherwise the speaker chooses a name at random from their existing lexicon. If the listener also has this name in their lexicon, the interaction is deemed a success, and both speaker and listener delete all other names (if any) from their lexica. Otherwise the interaction is a failure, and the listener adds the name uttered by the speaker to their lexicon. At the level of the speech community, the dynamics proceeds in three stages: initially, interactions typically require the invention of a new name, and so the total number of different names grows in time. In the second stage, these names spread across multiple lexica, thereby increasing the chance that both speaker and listener will have a common name for the object. This precipitates the final stage of the dynamics where consensus on a single name for the object is achieved across the entire speech community. The timescale on which this consensus is reached is found from simulation to be $\Lambda(N) \sim N^{3/2}$, which is faster than the diffusive process of fixation in the Moran model. Moreover, on this timescale, the transition to the state of consensus becomes sharper (suggestive of something like a first-order dynamical phase transition). The origin of the short timescale for consensus formation relative to the Moran model can be understood by considering just the late-time regime where only two names remain and a direct comparison is possible [73,74]. Here one finds two distinct biases serve to favour the variant that is in the majority in the speech community. First, when communication is a success, the listener’s deletion of alternative names from their lexicon in itself favours the majority variant. Second, the listener feeds back to the speaker that communication was a success, and the speaker also applies the deletion step, further boosting the majority variant. Consequently, one would expect similar dynamics even without the explicit feedback step that is included in the original naming game dynamics.

From an empirical perspective, the most interesting application of a model of this type is to understand universal properties of colour terms. Languages differ in the number of basic colour terms (like ‘red’ or ‘green’ in English) that exist, and also in the shades that are regarded prototypical of a specific colour term [75]. Nevertheless, the division of the continuous colour space into discrete categories is not completely arbitrary: in particular, the prototypes for each category (eg red, blue and green) form clusters in colour space that do not strongly overlap [75, 76], Baronchelli et al [77] used an extension to the naming game to explain this phenomenon. The basic idea is that
speakers are presented with multiple colours in a single scene, and seek to refer to a specific target colour. If the speaker’s categorisation of the (one-dimensional) colour space is such that the target is the sole member of its category in the scene, a word associated with this category is presented to the listener. Otherwise, the speaker creates a new category (and a new word for it) that is sufficient to disambiguate the target from the other colours present. The interaction is successful if the listener recognises the word, and manages to correctly infer the target meaning (either because it is unambiguous according to the listener’s categorisation, or because they guessed correctly among equally plausible alternatives). Addition and deletion of words than proceeds as in the naming game: in the case of failed communication, the speaker indicates the target meaning and the listener adds the uttered word to the category containing that meaning. Naïvely one might expect these dynamics to lead to a very fine partitioning of colour space so that any combination of stimuli can be disambiguated. However, this is not the case for two reasons. First, only a small number of colours are typically shown in a scene, so the distance between them will typically be large. Second, speakers and listeners need to have well-aligned category boundaries for communication to be successful. Such alignment is hard to achieve with a large number of boundaries, and the failed interactions will tend to lead to words spreading between categories. Consequently, there is a trade-off between the ability to express distinctions between different colours and the difficulty of aligning a highly complex category system, reminiscent of the trade-offs seen in iterated learning models discussed above. The question of how category prototypes (which can be defined as the midpoints between two category boundaries) cluster around universal points was investigated by incorporating the psychological notion of a just noticeable difference (JND) into the model. In the context of colour, these means that any two stimuli presented in the same scene different in wavelength by some small value. Empirical research shows that the JND varies with wavelength: some nearby colours are easier for humans in all cultures to distinguish than others [78]. Consequently, this breaks the translational symmetry in colour space, and generates clustering that is argued to be consistent with that found empirically [77].

5 Individual linguistic interactions

In all the models of consensus formation and related processes discussed in the previous section, it is only the last [77] that made explicit use of empirically-determined quantitative data for individual human behaviour. Further opportunities to align models more closer to such data may arise from a considerable growth in experimental research on human communicative and linguistic interactions over the past few years (see [79] for a recent review). In addition to providing data relevant to language modelling, these experiments also illustrate some of the considerable complexity that is evident in human communication.

First, it is worth considering how a communicative act would appear to alien with limited communicative capabilities (or perhaps a domestic cat). What they would observe is people using their lungs and mouths to create pressure waves in the air, perhaps also moving their arms around at the same time, along with other movements like blinking, scratching of heads and so on. What would it take for the alien to realise that these actions have a communicative intent? This question has been addressed through experiments involving robots [80] and humans [81] that demonstrate processes by which communication channels are created on-the-fly through interactions without pre-specifying that communication is desirable or providing an obvious way to do so. In the case of humans, the crucial step that the agents make is to perform behaviour that is unexpected from other agents’ perspectives. This allows these agents to infer that the behaviour may be communicative [81]. This process requires complex cognitive abilities—for example the ability to predict how another agent will respond to an action—and as such is argued to be specific to humans [82].

Given this understanding of how agents are able to identify certain behaviours as potential signals, the question now arises as to how they would associate a signal with a specific meaning. Here it is worth remarking that in almost all models discussed above in Section 4, the meaning of a signal was always assumed to be known to both agents in a communicative interaction. For example, in the case of the colour terms study [77], any ambiguity in the meaning of a word was always resolved after an interaction as the speaker “unveils the topic [target meaning] via pointing” [77, SI:p2]. If it is always possible to communicate a word’s meaning by nonlinguistic means, then language is surely redundant. This suggests that there is likely always to be some some ambiguity in any utterance, particularly in the process of language acquisition where children somehow infer the meanings of words (and more generally grammatical constructions) from experienced language users.

There is a considerable body of experimental research that addresses this problem (see e.g. [83] for a review of early contributions in this area). Much of this work is conducted in an artificial language learning paradigm, whereby experimental participants are presented with a series of scenes containing a number of potential referents of a word (or set of words) and are asked questions that determine the inferences that participants have drawn about the meanings of words they have heard. The working hypothesis that has emerged is that a number of processes combine to deliver reliable word learning. First, on hearing an unfamiliar word, learners apply various heuristics to narrow down the (potentially infinite) set of possible meanings to a more manageable number of candidate meanings [83]. Experimentally attested heuristics include following the gaze of the speaker [84], an expectation that a word is more likely to relate to a whole object rather than one of its parts [85], or that no two words have the same meaning [86]. In some cases, these heuristics are able to eliminate all uncertainty and the word is learnt immedi-
between maximising the number of distinctions between 
experiment further provides evidence for a competition 
tional structure over multiple generations of learning. This 
compositions of the earlier computer simulations [66], namely that 
the communication system acquires a systematic composi-
tions can be applied to this problem. Reali and Griffiths 
A key question is what happens when two players who 
have established different symbols for the same meaning 
meet. Tamariz et al. [98] consider two biases that might af-
fect whether a participant keeps their existing symbol or 
switches to the other player’s symbol after an interaction. 
The first is a coordination bias, which is a bias towards or 
against adopting symbols produced by other players. The 
second is a content bias, which is a bias towards specific 
symbols (e.g., because they communicated the intended 
meaning more effectively than others). These two biases 
are instances of interactor and replicator selection in the 
language of [39, 40]. The main findings were that players 
tended to be biased in favour of keeping their existing sig-
als, but that evidence of content bias was present in most 
cases. It is interesting to note that these two effects are 
in conflict with each other: content bias promotes change, 
but agents are generally resistant to modifying their be-

Variations on this experimental approach have been used 
to explore other topics that were discussed in Sec-

A small but significant (and somewhat ingenious) ex-
tension to the artificial language learning paradigm al-

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atley. This effect is known as fast mapping [87]. However, 
it seems plausible that this is not always possible, and that 
language learners integrate information from multiple ex-
posures to resolve any ambiguity. For example, if a child 
first encounters the word “sheep” on a visit to a farm, 
they could assume from the context that this refers to a 
cow that is also physically present; it is only on a later en-
counter that the cow meaning is implausible, whereas the 
sheep meaning is highly plausible, and the child revises 
their internal lexicon accordingly.

The general practice of combining information from 
multiple exposures is referred to as cross-situational learn-
ing [88], and the separate process of hypothesising a (pos-
sibly incorrect) meaning and awaiting confirmation from 
later exposures is referred to variably as a guess-and-test 
[89] or propose-and-verify [90] heuristic. Both processes— 
along with a variety of others—been observed in arti-
ficial language learning experiments, which have been 
conducted variously with children and adults [89, 91, 90]. 
These results have inspired mathematical models of word 
learning which show that a lexicon of the size of that typ-
ically acquired by an adult human (60,000 words [83]) can 
be learnt on a realistic timescale under quite general con-
ditions [92, 93]. It is even in principle possible to learn 
the meaning of a word when an infinite set of alternative 
meanings can be inferred at any given exposure, as long 
as a learner can assign a plausibility ranking in such a way 
that the kth most plausible meaning decays as a power-law

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In the graphical communication experiment, agents are 
well characterised by usage of one particular signals for a 
given meaning. Since language users can be variable in 
language use, it is of interest to learn what happens to 
this variability when these users interact. In particular, 
this may provide some information as to the appropriate 
bias to include in an equation Eq. (4) which models vari-
able language behaviour. Again, iterated learning experi-
ments can be applied to this problem. Reali and Griffiths 
set up a language where each object has two names 
which appear with prescribed frequencies against their 
target meaning. After training, a participant is asked to 
name each object several times, which provides a set of fre-
quencies to use for the next generation of learning. In this 
approach, one can build up a transition matrix $T(x' | x)$,
which gives the probability that when word \( A \) is used with frequency \( x \) to name an object, that after learning an individual uses that word with frequency \( x' \). Real and Griffiths find that in one generation of learning, learners appear to probability match, i.e., that \( x' = \sum_{x'} T(x'|x) \approx x \). However, considerable variation is evident, and over multiple generations of learning the frequency distribution that results is consistent with a weak bias against variability (i.e., one that favours frequencies close to 0 or 1). This is consistent with sociolinguistic understanding of variation, which is that where variation exists, it is usually conditioned on a linguistic factor (e.g., the pronunciation of a sound may depend on the position in the word) or a social factor (e.g., the speaker’s age, level of education or other aspect of their identity) [9,38]. A further iterated learning experiment [100] bears this out, wherein the initial language had consistent names for each of the objects, but two different plural markers. Although initially one plural marker is more frequent than the other, there is no correlation between which plural marking is used for which object. Here it is found that iterated learning either eliminates one of the plural markers, or that the variation becomes predictable: that is, each object is typically pluralised by one or other of the markers, but not both.

A final application of the artificial language learning paradigm is to investigate whether the non-uniform distribution of a structural feature over the world’s languages (like word order, see Section 2) predicts the existence of a bias towards the more frequent structures in single instances of learning. One such study relates to affixes that change the meaning of the word. Where this occurs, it turns out that suffixes are more common than prefixes or infixes [101]. To investigate whether this is also true at the individual level, St Clair et al [102] trained participants on an artificial language in which words are divided into two categories, each with their own affix. When presented with unfamiliar sentences, participants could more reliably identify when the correct affix was used for a particular word stem, in correspondence with the observation that suffixes are more common than prefixes.

As noted in Section 2, correlations between two structural features of a language have been observed, and are formulated as implicational universals. Culbertson et al [103] set up an experiment to determine whether a correlation between the order of numerals and nouns and the order of adjectives and nouns is visible at the level of individual learning events. In particular, one of the four possible orderings is much less frequent than the other three. Participants were trained on four variant languages, and then asked to describe a set of scenes using the language they had learnt. Points were awarded for a valid description of the scene (i.e., the right words, but in any order) and additionally if the order matched that of a computer-generated ‘native’ speaker of the artificial language. The input languages were set up in such a way that participants would score maximum points by using one of the four possible orderings exclusively. The results of this experiment showed that this happened for all four input languages, apart from the one that corresponds to the order-

<table>
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Table 1. Hierarchy of scales in language dynamics covered in this article ordered by decreasing length- and timescales

6 Unifying the hierarchy

In this short Colloquium I have surveyed four levels in a hierarchy of scales that are relevant to language dynamics. Each level can be classified according to the main unit of variation at that level. This then determines the range of phenomena that are available for investigation: see Table 1. Here, we have taken individual episodes of language acquisition and production to sit at the base of the hierarchy. These episodes typically involve a small number of language users (often just two) interacting for a short period of time (typically minutes). These length- and timescales are sufficiently small that laboratory experiments involving human participants—and the full complexity of their cognitive apparatus—can be used to measure biases that govern how language learning and production affects the structure and variability of language (see Section 5). In principle, we could descend to a deeper level, where we take the structure of the internal cognitive apparatus as the unit of variation, but we have left this aside here in the interests of brevity. With knowledge of these biases, we can then build effective models of individual human behaviour, and embed these individuals in a speech community, as described in Section 4. Through repeated interactions, language structure may emerge, and one that can characterise an entire speech community. At higher levels of the hierarchy, both speech communities and languages are taken as coherent units. In the former case this leads to competition between languages, as described in Section 3, and in the latter, languages differentiate over time giving rise to a tree-like structure of relationships between them.

In principle, one could integrate the different levels of the hierarchy into a single whole, and the discussion we have given provides some detail as to how this might be
achieved in practice. First, from the experiments described in Section 5, we described how one can build up a transition matrix \(T(x’|x)\) that specifies how individuals modify the frequency \(x\) that they exhibit a specific behaviour in single interactions. This transition rate matrix could then be incorporated into the update rules of a Moran-type model (Section 4.1), which would lead to a set of stochastic equations of motion analogous to Eq. (5), where the biases \(b(x)\) that can be traced back to the experimentally-determined transition matrix \(T(x’|x)\). From here, one can predict the structures that become established as conventions in a speech community, and by further augmenting individuals in the model with their own birth-death dynamics we can study the competition between languages with different structures that occur at the level of the speech community (Section 3). If one coarse-grains over individual variability and looks for a deterministic limit, it seems likely that a description similar to that postulated by Abrams and Strogatz, Eq. (2), will result. If one further coarse-grains over the number of speakers, and looks at the conventions that are formed over longer timescales, then an effective dynamics for changes in these structures—for example, the Poisson process (1) that has been used in the phylogenetic analyses of Section 2—would result.

Although it is technically possible to connect the levels of the hierarchy in this way, is there any intellectual value in doing so? After all, when studying the relationships that emerge between languages at the largest length- and timescales, one may not be too interested in the precise process by which a new convention becomes established, just how this may be adequately described at the relevant timescales. A Poisson process could provide the adequacy that is desired. However, in addressing this question it is worth looking more deeply into the some of the underlying motivations for research questions that have been posed at opposite ends of the hierarchy. For example, in their study of word-order universals at the level of entire languages, Maurits and Griffiths [24] make reference to underlying psychological biases that act in favour of one word order (e.g., burdens on working memory) and how one would then expect these to be reflected in a preferred direction of change at the macroscopic level. Meanwhile, Culbertson et al. [103] in their experimental study of changes in word order that occur at the level of an individual refer to the hypothesis that “if a logically-possible grammatical system is not found, or is quite rate cross-linguistically, the explanation offered by [theories based on biases in learning] is that this system violates a learning bias” [103, p.306]. It is reassuring that the results of both investigations point in a similar direction, in that less common word orders appear to be less stable both at the level of individual learning and at the level of historical change. However, to demonstrate that these are manifestations of the same phenomenon requires us to connect the two descriptions via the intermediate levels of the hierarchy.

Two sources of complexity make such a demonstration challenging. First, many factors can affect language dynamics at each level of the hierarchy. By way of illustration, suppose that transmission matrices between linguistic states for single individuals have been established in an experimental setting, and are understood to characterise all human beings. On plugging these into speech-community-level models, it is clear from (4) that changes in state at the level of the common language that emerges can depend on specific (non-linguistic) features of those communities. For example, the characteristic timescale in the Moran model, the function \(A(N)\) in Eq. (3), can vary with the speech community size \(N\) in a way that depends on how the social network is connected, and the relative influence that different speakers can have on each other. At the same time, the propagation of a minority variant seems to require a positive disposition (replicator selection bias) towards it on the part of a majority of speakers. Such disposition towards a particular way of speaking presumably varies from one speech community to another and within a single community over time, for example due to its association with a particular well-regarded group of individuals [37]. Thus it would in fact be somewhat surprising if the transition rates that apply at the macroscopic level, as in Eq. (1), were universal for a given structural feature in space and time, unless perhaps all the changes that occur at the lower levels of the hierarchy on such a fast timescale that they give the appearance of being so. Indeed, some studies [26,23,21] provide evidence that language structure and the rate of language change co-vary with culture-specific factors. The second source of complexity is one that we have barely touched on in this work, namely that human language is a highly complex object, with many different components (sounds, words, grammar), which presumably interact with each other in acquisition and use. Almost all studies of language dynamics have considered a small number of variable units evolving in isolation from the rest of the linguistic system. It is not obvious whether such a simplification is reasonable, or whether some vital part of the description is missing.

To resolve these open questions, simultaneous progress is needed on at least three fronts. First, a more complete mathematical understanding of what specific models predict would be valuable. For example, the exact solutions of the simplest Moran models and their variants have provided a great deal of insight into evolutionary dynamics in general [70]; however, these solutions are known only for the case where currents vanish in the steady state. Thus, as in physics, the more general case of athermal (entropy-producing) dynamics is the one that is both of greater applicability, but presents a correspondingly more difficult mathematical challenge. Meanwhile, more complex dynamical processes are typically implemented as computational models. Again, it is typically difficult to access realistic degrees of complexity (e.g., in speech community size, or structure of the linguistic system) in cases where the stationary state is not an equilibrium (zero-current) case, as the most efficient simulation algorithms tend to rely on this property.

Second, as this and other reviews (e.g., [8,63]) attest, there is a profusion of models of language dynamics (and related processes like opinion formation). At the same time, many distinct models show broadly similar results,
for example, a tendency towards consensus unless there is a pre-existing spatial symmetry breaking or a feedback between agent behaviour and the propensity to interact; or that structure tends to emerge over repeated learning. The statistical physics community in particular is yet to converge on a core set of models that achieve the optimal balance between (analytical or computational) tractability and explanatory power. It is also important to consolidate the various modelling approaches that have been taken into a set of general principles. A number of works hint for example at principles that involve trade-offs between the expressive power and complexity of a language system, which are broadly reminiscent of the trade-offs between energy and entropy that provide a deep understanding of collective phenomena in physical systems.

Finally, it is a truth almost universally acknowledged that data for historical language behaviour is scarce. Although the World Atlas of Language Structures [13] is extensive in terms of the number of languages and structures that it covers, it does so at only one point in time. This allows historical changes to be inferred, but validating these inferences by comparing with the actual changes that have occurred is difficult. These difficulties are further confounded if it turns out that additional factors (such as the speech community size or social network structure) also affect historical language dynamics, since then these will need to be known as well. However, there may be approaches that will allow these gaps in the empirical data to be bridged. First, if one is specifically interested in how linguistic behaviour spreads and changes over short timescales, social media may provide a rich resource. In particular, it may be possible to determine whether models of the type described in Section 4 adequately describe how innovations propagate through an online community. Other large-scale sources of data with greater time depth also exist, such as Google’s corpus of scanned books [105]. Alongside providing snapshots of language use, the online world also offers the opportunity for mass behavioural experiments. Many of experimental designs outlined in Section 5 lend themselves to being set as tasks on platforms like the Amazon Mechanical Turk, and their results have been found to correlate well with traditional experiments (see e.g. [106]). Scientific progress is greatly accelerated when data is abundant, and with some creative thinking, data-driven advances in language modelling may pave the way to a more complete understanding of processes that lie beyond the grasp of empirical research.

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