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# The effect of cosmic magnetic fields on the metagalactic ionization background inferred from the Lyman $\alpha$ forest

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## ABSTRACT

The sources which reionized the intergalactic medium by redshift  $\sim 6$  are still unknown. A severe constraint on the ionization process is the low emissivity required to maintain the ionization in the Ly $\alpha$  forest. Simulation-calibrated observations suggest a production rate of at most only a few photons per baryon. In this work, we present a new solution to this ‘photon-starvation’ problem using a weak background of cosmic magnetic fields, which may be present as a consequence of early-Universe physics and subsequent magneto-hydrodynamical amplification. If present, such magnetic fields can induce density perturbations which are dominant on scales comparable to those probed by measurements of hydrogen-absorption lines at redshifts  $z \sim 2\text{--}5$ . We show that a subnanoGauss magnetic field, coherent on scale  $\sim 1$  Mpc with an almost scale-invariant spectrum, is sufficient to produce significant impact on the effective optical depth, the appearance of the Ly $\alpha$  forest on quasar spectra, the pixel-flux statistics and the power spectrum of transmitted flux. We also show that such magnetic field signatures are effectively erased when the metagalactic photoionization rate is increased, hence relaxing the constraint on the cosmic photon budget available for reionization.

**Key words:** intergalactic medium – galaxies: magnetic fields.

## 1 INTRODUCTION

Measurements of anisotropies in the cosmic microwave background (CMB) and of spectra of quasi-stellar objects (QSO) suggest that as early as a few million years after the big bang, the primordial hydrogen in the Universe was largely ionized. The process of *cosmic reionization* is thought to have been initiated by high-energy photons produced during the formation of the first luminous objects before a redshift  $z \sim 11$ , with reionization completing as late as  $z \sim 6$  (Fan, Carilli & Keating 2006; Zahn et al. 2012; Hinshaw et al. 2013; Planck Collaboration 2013). The details of the reionization process are not yet understood. The galaxies widely believed to be the sources of the reionization are yet to be discovered.

The mystery of the reionization process is compounded by the low ionizing-photon emissivity inferred from the Ly $\alpha$  forest, the characteristic fluctuations detected in the spectra of high-redshift quasars arising from the scattering of photons at wavelength  $1216(1+z)$  Å by intervening clouds of neutral hydrogen (Meiksin 2009). The ionizing background required to match the measured mean Ly $\alpha$  flux, as calibrated by numerical simulations, corresponds to a source emissivity of only a few ionizing photons per baryon at  $z \lesssim 6$  (Miralda-Escudé 2003; Meiksin 2005; Bolton & Haehnelt 2007).

This suggests the sources that drove reionization had harder spectra than those maintaining the ionization of the intergalactic medium (IGM) at  $z < 6$ ; or, alternatively, the number of reionizing sources, or the escape fraction of the ionizing photons from the sources, declined sharply as the reionization of the IGM came to completion. Galaxy formation models show the reduction may arise naturally from the suppression of star formation towards the end of the reionization epoch (Kuhlen & Faucher-Giguère 2012; Paardekooper, Khochfar & Dalla Vecchia 2013), although this scenario still lacks direct observational support.

The constraint on the ionizing photon budget could be relaxed if the density fluctuations in the IGM were sourced by an additional mechanism. In this work, we suggest a solution using a weak background of *cosmic magnetic fields*. It has been widely recognized that a primordial magnetic field would enhance the density fluctuations in the baryonic component (Wasserman 1978; Subramanian & Barrow 1998a), including those giving rise to the Ly $\alpha$  forest (Pandey & Sethi 2013). The seeds for such fields may have been produced by early-Universe processes such as inflation or symmetry breaking during phase transitions. The seeds are expected to have been amplified by some cosmic dynamo processes (see Kandus, Kunze & Tsagas 2011; Yamazaki et al. 2012; Durrer & Neronov 2013, for recent reviews).

Magnetic fields have been observed to permeate the Universe on a range of physical scales at various magnitudes, from roughly

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a milliGauss on galactic scales (Beck et al. 1996; Widrow 2002) down to a microGauss on galaxy-cluster scales (Clarke, Kronberg & Böhringer 2001; Govoni & Feretti 2004). Recent measurements of CMB anisotropies from *Wilkinson Microwave Anisotropy Probe*, and most recently from *Planck*, place an upper limit on the magnitude of magnetic fields on cosmological scales ( $\sim 1$  Mpc) of a few nG (Paoletti & Finelli 2012; Planck Collaboration 2013). Future CMB-polarization measurements will provide additional constraints on the amplitude of cosmic magnetic fields, since the latter induce Faraday rotation of the plane of polarization of CMB photons (Giovannini & Kunze 2008; Kahnishvili, Maravin & Kosowsky 2009; Pogosian et al. 2011).

If cosmic magnetic fields are present, they can induce additional density perturbations which are dominant on scales comparable to those probed by measurements of hydrogen-absorption lines at redshifts  $z \sim 2-5$ . There have been only a few previous studies connecting cosmic magnetic fields to the Ly $\alpha$  forest. Shaw & Lewis (2012) used SDSS quasar data and a modified COSMOMC code to constrain the magnetic contribution to the matter power spectrum on scale  $k \sim 1$  Mpc $^{-1}$ . More recently, Pandey & Sethi (2013) used a semi-analytic approach to generate magnetic-field-induced density fluctuations along lines of sight and constrained the magnetic field amplitude by comparing with the observations of Faucher-Giguère et al. (2008).

We extend the previous work to investigate a broader range of signatures of cosmic magnetic fields in the Ly $\alpha$  forest. We find that magnetic-field-induced perturbations increase the fluctuations in the structure of the IGM, deepening and broadening the features while contributing to their longer wavelength spatial correlations. These features, however, are washed out for high metagalactic photoionization rates. Since the numerical simulations used to calibrate the photoionizing background from the measured mean intergalactic Ly $\alpha$  transmission do not include fluctuations from magnetic fields, they would underestimate the photoionization rate if magnetic field fluctuations were present. We use an approximate treatment of the structure of the IGM to quantify this effect.

Throughout this work, we assume in our fiducial model the following cosmological parameters: dimensionless Hubble parameter  $h = 0.68$ ; present density parameter for matter ( $\Omega_m = 0.31$ ), baryon ( $\Omega_b = 0.048$ ), radiation ( $\Omega_r = 2.47 \times 10^{-5}$ ), dark energy ( $\Omega_{DE} = 1 - \Omega_m - \Omega_r$ ); scalar spectral index,  $n_s = 0.96$ , normalization of matter power spectrum,  $\sigma_8 = 0.81$ , fraction of baryonic mass in helium  $Y = 0.247$  (Planck Collaboration 2013). All magnetic field amplitudes quoted are comoving:  $B(0) = B(z)/(1+z)^2$ .

In the next section, we present the formalism used to approximate the Ly $\alpha$  forest, followed by a discussion of the model used for generating the fluctuations induced by magnetic fields. The effects on the Ly $\alpha$  forest are presented in Section 4. We end with a discussion and our conclusions.

## 2 THE LOGNORMAL FORMALISM

Perturbations generated by primordial magnetic fields are dominant on scales on which linear perturbation theory starts to break down, making analytic progress difficult. Here, we describe a formalism, due to Bi & Davidsen (1997), which produces a distribution of mildly non-linear density perturbations at redshift  $2 \lesssim z \lesssim 5$  without the need for  $N$ -body simulations.

Consider the matter overdensity field  $\delta(\mathbf{x}, z) = (\rho_m(\mathbf{x}, z) - \bar{\rho}_m)/\bar{\rho}_m$ , where  $\bar{\rho}_m$  is the background matter density. Given a distribution of density perturbations in dark matter (generated, say, by inflation), Bi & Davidsen (1997) gave a formalism for calculat-

ing the corresponding distribution of *baryonic* matter perturbations based on the hypothesis that the baryonic density perturbations in the mildly non-linear regime follow a lognormal distribution. In this model, the baryon number density,  $n_b$ , is given by

$$n_b(\mathbf{x}, z) = n_0(z) \exp(\delta_b(\mathbf{x}, z) - \langle \delta_b^2(\mathbf{x}, z) \rangle / 2), \quad (1)$$

where the background baryon number density  $n_0(z) = \langle n_b(\mathbf{x}, z) \rangle = \Omega_b \rho_c (1+z)^3 / (\mu_b m_p)$ , and  $\mu_b m_p = 4m_p / (4-3Y)$  represents mass per baryonic particle. The baryon overdensity,  $\delta_b$ , is assumed to be a Gaussian random field. Bi & Davidsen showed that the lognormal approach reproduces the expected distribution of baryons at small and large scales and was shown to be a reasonable approximation when tested against hydrodynamical simulations.

Assuming that the IGM temperature evolves smoothly with redshift, the baryon and dark-matter density perturbations on scale  $k$  are simply related by the Fourier-space relation

$$\delta_b(\mathbf{k}, z) = \frac{\delta_m(\mathbf{k}, z)}{1 + x_b^2 k^2}, \quad (2)$$

where the comoving Jeans length,  $x_b$ , is given by (Fang et al. 1993)

$$x_b = H_0^{-1} \left( \frac{2\gamma k T_m(z)}{3\mu m_p \Omega_m (1+z)} \right)^{1/2}. \quad (3)$$

Here,  $T_m(z)$  is the density-averaged IGM temperature,  $\mu = 4/(8-5Y)$  is the mean molecular weight of the IGM, and  $\gamma$  is the polytropic index defined via the equation for the temperature,  $T(\mathbf{x}, z)$  of the IGM:

$$T(\mathbf{x}, z) = T_0(z) \left( \frac{n_b(\mathbf{x}, z)}{n_0(z)} \right)^{\gamma-1}, \quad (4)$$

where  $T_0(z)$  is the temperature at mean density, which we set equal to  $T_m(z)$ . In contrast with previous works in which  $\gamma$  is usually assumed to be constant, here we use the measurement of Becker et al. (2011) to infer the values of  $\gamma$  and  $T_0$  in the redshift range  $2 < z < 4.8$  as shown in Fig. 1. Their measurement is derived from 61 high-resolution QSO spectra, and shows  $T_0$  increasing from 8000 K at  $z = 4.4$  to around 12 000 K at  $z = 2.8$ . The authors interpreted this rise as coming from the photoheating of ionized helium (He II), consistent with He II reionization at  $z \sim 3$ .

Inflation and linear perturbation theory predict that the linear matter power spectrum is given by

$$P_m(k, z) \propto \mathcal{M}^2(k, z) k^{n_s-4}, \quad (5)$$

$$\mathcal{M}(k, z) \equiv \frac{2k^2 T(k) D(z)}{3H_0^2 \Omega_m}, \quad (6)$$

where the power spectrum is defined via the Fourier autocorrelation

$$\langle \delta_m(\mathbf{k}, z), \delta_m(\mathbf{k}', z) \rangle = (2\pi)^3 \delta(\mathbf{k} - \mathbf{k}') P_m(k, z), \quad (7)$$

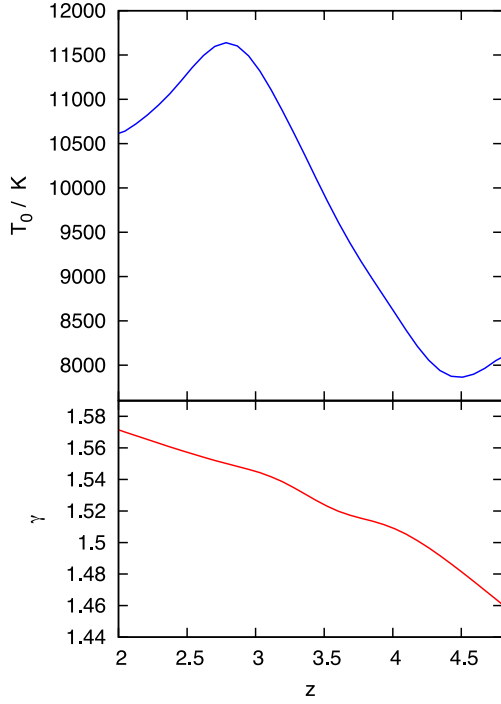
$T(k)$  is the transfer function and  $D(z)$  the growth factor of density fluctuations. We normalize  $P_m(k, z=0)$  so that  $\sigma_8$  (square root of the variance of fluctuations on scale  $8 h^{-1}$  Mpc) equals 0.81.

From (2), we see that the 3D baryon power spectrum is given by

$$P_b(k, z) = \frac{P_m(k, z)}{(1 + x_b^2 k^2)^2}. \quad (8)$$

However, observations of the Ly $\alpha$  forest probe only the one-dimensional baryonic power spectrum along lines of sight. Let

$$\mathcal{I}_n(k, z) = \frac{1}{2\pi} \int_k^\infty dk' (k')^n P_b(k', z).$$



**Figure 1.** The IGM temperature at mean density,  $T_0(z)$ , with varying polytropic index  $\gamma$ , calibrated using the measurement of Becker et al. (2011).

The 1D power spectra for the baryon overdensity,  $\delta_b(k)$ , and velocity perturbations,  $v_b(k)$  and their cross-correlation can be expressed as

$$P_b^{1D}(k, z) = \mathcal{I}_1, \quad (9)$$

$$P_v^{1D}(k, z) = E^2(z)k^2\mathcal{I}_{-3}, \quad (10)$$

$$P_{bv}^{1D}(k, z) = iE(z)k\mathcal{I}_{-1}, \quad (11)$$

where  $E(z)$  determines the growth rate of velocity perturbations and is defined as

$$E(z) \equiv \frac{d \ln D}{d \ln a} \frac{H(z)}{1+z}.$$

Bi & Davidsen's formalism allows the Fourier-space density and velocity fields to be generated, given information about their power spectra. To do this,  $\delta_b$  and  $v_b$  are first decomposed into combinations of uncorrelated Gaussian fields,  $u(\mathbf{x})$  and  $w(\mathbf{x})$ , using the projection method outlined in Bi (1993). The expressions for the independent power spectra  $P_u(k, z)$  and  $P_w(k, z)$  are

$$P_w(k, z) = \mathcal{I}_{-1}^2 / \mathcal{I}_{-3}, \quad (12)$$

$$P_u(k, z) = \mathcal{I}_1 - P_w(k, z). \quad (13)$$

To obtain the Fourier modes  $u(k, z)$  and  $w(k, z)$ , from their power spectra, we use the polar decomposition

$$u(k, z) = |u|e^{i\phi}, \quad (14)$$

where  $\phi$  is drawn from a uniform distribution  $U[0, 2\pi]$  and  $|u|$  is drawn from the Rayleigh distribution

$$R(|u|) = \frac{|u|}{\alpha^2} e^{-|u|^2/2\alpha^2}, \quad \alpha^2 \equiv P_u(k)/2. \quad (15)$$

It can be shown that  $|u| = \alpha\sqrt{-2 \ln \mathcal{X}}$ , where  $\mathcal{X}$  is drawn from another uniform distribution  $U[0, 1]$ . Similarly,  $w(k, z)$  can be obtained using independent draws since  $u$  and  $w$  are uncorrelated Gaussian

fields. Finally, the density and velocity perturbations of baryons can be written as

$$\delta_b^{\text{Inf}}(k, z) = u(k, z) + w(k, z), \quad (16)$$

$$v_b^{\text{Inf}}(k, z) = iE(z)kw(k, z) \frac{\mathcal{I}_{-3}}{\mathcal{I}_{-1}}. \quad (17)$$

We use the superscript 'Inf' to distinguish the inflation-generated perturbations from the magnetic-field induced perturbations, which we now describe.

### 3 PERTURBATIONS FROM MAGNETIC FIELDS

We now consider the baryonic matter perturbations induced by cosmic magnetic fields. The coherent length of such magnetic fields is so large that they may be treated as a stochastic field with homogeneous energy density. The effect of helicity is neglected in this work.

Let  $B(\mathbf{x}, t)$  be the local amplitude of a homogeneous, non-helical background magnetic field. After recombination, free baryons and magnetic field can be treated as a fluid which can be described by a set of coupled magneto-hydrodynamical equations as shown the pioneering work of Wasserman (1978). Given a certain amplitude of the magnetic field component in this fluid, we are interested in the amplitude of the induced density fluctuations in the baryonic component.

The magnetic field amplitude scales with the cosmic scale factor,  $a(t)$ , as  $B(\mathbf{x}, t) = B(\mathbf{x})/a^2(t)$ . This means that the average energy density in magnetic field,  $\rho_B \equiv \langle B^2(\mathbf{x}, t) \rangle / 8\pi$ , scales like radiation:

$$\rho_B(t) = \frac{\langle B^2(\mathbf{x}) \rangle}{8\pi a^4(t)} = \frac{\rho_{B,0}}{a^4(t)}. \quad (18)$$

In Fourier space, the magnetic field power spectrum,  $P_B(k)$ , is defined by the autocorrelation

$$\langle B_i(\mathbf{k})B_j^*(\mathbf{k}') \rangle = (2\pi)^3 \delta(\mathbf{k} - \mathbf{k}') \frac{\mathcal{P}_{ij}(\hat{\mathbf{k}})}{2} P_B(k), \quad (19)$$

where  $\mathcal{P}_{ij} = \delta_{ij} - \hat{k}_i \hat{k}_j$  is a projection tensor. The power spectrum is commonly parametrized as a power-law with a small-scale cut-off

$$P_B(k) = \begin{cases} Ak^{n_B}, & k \leq k_D \\ 0, & k > k_D, \end{cases} \quad (20)$$

where  $n_B$  is the magnetic spectral index and  $k_D$  is the cutoff scale, below which the energy in the magnetic fields is dissipated by Alfvén-wave damping (Jedamzik, Katalinić & Olinto 1998; Subramanian & Barrow 1998b). This form of the spectrum leads to the expression for the expected magnetic field amplitude

$$\langle B^2 \rangle = \frac{Ak_D^{n_B+3}}{2\pi^2(n_B+3)}, \quad (21)$$

valid for  $n_B > -3$ . When smoothed using a Gaussian window function,  $\exp(-x^2/\lambda^2)$ , we obtain the smoothed amplitude  $\langle B^2 \rangle_\lambda$ , which is related to the spectral amplitude by

$$A = \frac{(2\pi)^{n_B+5} \langle B^2 \rangle_\lambda}{2\Gamma\left(\frac{n_B+3}{2}\right) k_\lambda^{n_B+3}}, \quad (22)$$

where  $k_\lambda = 2\pi/\lambda$ . We choose  $\lambda = 1 \text{ Mpc}$  in this work, and for convenience, we denote the *rms* amplitude as

$$B_1 \equiv \sqrt{\langle B^2 \rangle_{\lambda=1 \text{ Mpc}}}. \quad (23)$$

This choice of  $\lambda$  leads to the expression for  $k_D$  (Kahniashvili et al. 2012)

$$k_D = \left[ 140\sqrt{h} (2\pi)^{(n_B+3)/2} \left( \frac{1 \text{ nG}}{B_1} \right) \right]^{2/(n_B+5)} \text{Mpc}^{-1}, \quad (24)$$

where it is assumed that the Alfvén wave velocity is proportional to the magnetic field amplitude. The damping scale is typically small: using  $B_1 = 1 \text{ nG}$  and  $n_B = -2.99$ ,  $k_D \approx 114 \text{ Mpc}^{-1}$ .

The linear magnetic field contribution to the matter power spectrum has been derived analytically in Kim, Olinto & Rosner (1996) and Gopal & Sethi (2005). The expression for the magnetic-field-induced matter power spectrum, in unit of  $h^{-3} \text{ Mpc}^3$ , is

$$P_m^{\text{MF}}(k) = \frac{t_{\text{rec}}^4 k^3}{(4\pi\rho_b a^3(t_{\text{rec}}))^2} \int_0^{k_D} dq \int_{-1}^1 d\mu \frac{P_B(q)P_B(\alpha)}{\alpha^2} \mathcal{K}(k, q, \mu),$$

$$\mathcal{K} = q^3 (2k^2\mu + kq(1 - 5\mu^2) + 2q^2\mu^3),$$

$$\alpha = \sqrt{k^2 + q^2 - 2kq\mu}, \quad (25)$$

where  $\rho_b$  is the present baryon density and  $t_{\text{rec}} \approx 0.371 \text{ Myr}$  is the cosmic time at recombination (see also Paoletti, Finelli & Paci 2009; Shaw & Lewis 2012, for alternative treatments).

Letting  $u = q/k$  brings equation (25) to a more manageable form

$$P_m^{\text{MF}}(k) = C(k) \int_0^{k_D/k} du \int_{-1}^1 d\mu \mathcal{I}(u, \mu),$$

$$C(k) = k^7 [P_B(k)]^2 \frac{t_{\text{rec}}^4}{(4\pi\rho_b a^3(t_{\text{rec}}))^2},$$

$$\mathcal{I}(u, \mu) = u^{n_B+3} (1 + u^2 - 2u\mu)^{n_B/2-1}$$

$$\times (2\mu + u(1 - 5\mu^2) + 2u^2\mu^3). \quad (26)$$

In this form, we find that  $C(k) \sim k^{2n_B+7}$  dominates the behaviour of  $P_m^{\text{MF}}(k)$ , with small deviation represented by the remaining integrals. The latter must be carefully evaluated across the pole at  $(u, \mu) = (1, 1)$ . Finally, we insert the time dependence using another result of Kim et al. (1996)

$$P_m^{\text{MF}}(k, t) = \mathcal{T}^2(t) P_m^{\text{MF}}(k), \quad (27)$$

$$\mathcal{T}(t) = \frac{9}{10} \left( \frac{t}{t_{\text{rec}}} \right)^{2/3} + \frac{3}{5} \left( \frac{t}{t_{\text{rec}}} \right) - \frac{3}{2}. \quad (28)$$

In summary, the magnetic-field-induced matter perturbations are determined mainly by two parameters: the magnetic spectral index,  $n_B$ , and the *rms* amplitude smoothed at 1 Mpc,  $B_1$ .

To calculate the magnetic field contribution to the baryon perturbations, we replace the  $P_m(k, z)$  in equation (8) by  $P_m^{\text{MF}}(k, z)$ , and again apply the lognormal formalism. This gives the magnetic-field-induced perturbations,  $\delta_b^{\text{MF}}(k, z)$  and  $v_b^{\text{MF}}(k, z)$ .

At each point along the line of sight, we evaluate the Fourier-space density and velocity perturbations  $\delta_b^{\text{Inf}}$ ,  $\delta_b^{\text{MF}}$ ,  $v_b^{\text{Inf}}$ ,  $v_b^{\text{MF}}$ . An inverse Fourier transform produces the real-space perturbations. The condition  $\delta_b(-k) = \delta_b(k)$  (and similar for  $v_b$ ) is applied to ensure that the real-space perturbations are indeed real. We take the inflationary and magnetic-field-induced perturbations to be correlated, i.e. the amplitudes and phases of both types Fourier modes are drawn from the same distributions. Removing this correlation was shown by Pandey & Sethi (2013) to have little impact on observables.

Finally, the total real-space density perturbations at each point is

$$\delta_b(x, z) = \delta_b^{\text{Inf}}(x, z) + \delta_b^{\text{MF}}(x, z), \quad (29)$$

and similarly for the velocity perturbations  $v_b(x, z)$ . The corresponding baryon number density,  $n_b(x, z)$ , can then be determined using the lognormal ansatz (equation 1) and the relation

$$\langle \delta_b^2(x, z) \rangle = \frac{1}{2\pi^2} \int_0^\infty d \ln k k^3 P_b(k, z). \quad (30)$$

## 4 EFFECTS ON THE LY $\alpha$ FOREST

### 4.1 Ly $\alpha$ optical depth

The optical depth,  $\tau(z)$ , quantifies the amount of absorption of light emitted at redshift  $z$ . The intensity of radiation emitted by a QSO is attenuated by a factor of  $e^{-\tau(z)}$ . Assuming an approximate Doppler profile for each absorption by the IGM, the optical depth is given by

$$\tau(z) \approx \frac{cI_\alpha}{\sqrt{\pi}(1+z)} \int_{\text{LOS}} \frac{n_{\text{H}_1}(x)}{b(x)} \exp(-(\Delta v/b(x))^2) dx, \quad (31)$$

where the integration is performed with respect to the comoving distance,  $x$ , measured towards a point along the line of sight. The Ly $\alpha$  cross-section  $I_\alpha = 4.45 \times 10^{-18} \text{ cm}^2$ , the Doppler parameter  $b = (2k_B T(x, z)/m_p)^{1/2}$  and  $\Delta v = v_b + c(z' - z)/(1+z)$  represents the local velocity of the point with redshift  $z'$ . Averaging the optical depth  $\tau(z)$  over the realizations generated by the lognormal approach gives us the *effective* optical depth,

$$\tau_{\text{eff}}(z) = -\ln(e^{-\tau(z)}), \quad (32)$$

which is an observable quantity.

In ionization equilibrium, the number density of neutral hydrogen  $n_{\text{H}_1}$  is largely determined by the rate of recombination  $\alpha_{\text{H}_1}(T)$  (see e.g. Verner & Ferland 1996), and the photoionization rate,  $\Gamma_{\text{H}_1}(z) \equiv \Gamma_{-12}(z) \times 10^{-12} \text{ s}^{-1}$ :

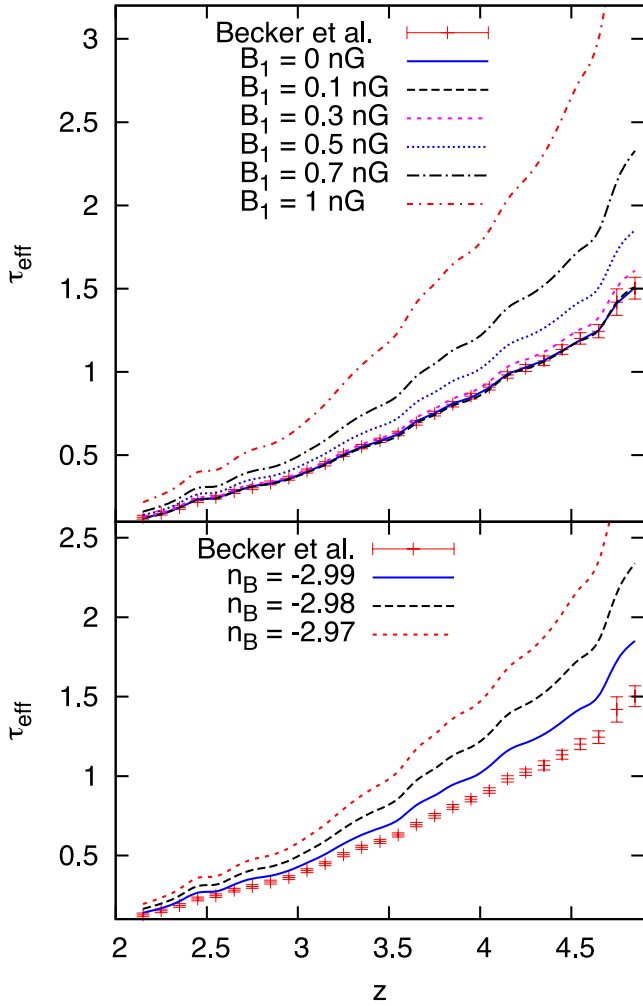
$$n_{\text{H}_1} = \frac{n_b \alpha_{\text{H}_1}}{\alpha_{\text{H}_1} + \Gamma_{\text{H}_1}(z)/n_e}, \quad (33)$$

where  $n_e$  is the electron number density. We neglect the effect of collisional ionization, which is only significant at temperature  $T \gtrsim 10^5 \text{ K}$  (Black 1981).

Fig. 2 shows the effective optical depth calculated in the redshift range  $2.2 \leq z \leq 4.8$  using the lognormal approach, with values of  $T_0(z)$  and  $\gamma(z)$  shown in Fig. 1. The data points and error bars are from Becker et al. (2013) based on 6065 SDSS quasars. We adjust the values of  $\Gamma_{-12}$  in each bin so that  $\tau_{\text{eff}}$  matches these data points. The upper panel shows  $\tau_{\text{eff}}$  when the magnetic field magnitude  $B_1$  is increased from 0 to 1 nG (with magnetic spectral index  $n_B$  fixed at  $-2.99$ ). We observe significant increase beyond the error bars for  $B_1 \gtrsim 0.3 \text{ nG}$  with most deviation occurring at higher redshifts. This increase stems from the fact that magnetic fields increase small-scale density fluctuations  $\delta_b$ , which in turn increase the baryon and the neutral-hydrogen number densities.

The lower panel of Fig. 2 shows the variation of  $\tau_{\text{eff}}$  when  $n_B$  increases from  $-2.99$  to  $-2.97$  (with  $B_1$  fixed at 0.5 nG). Clearly, there is a strong degeneracy between  $n_B$  and  $B_1$ , and constraints in this plane have been explored in Yamazaki et al. (2012) and Pandey & Sethi (2013). Comparing our results with the latter's, we find similar amplitude of magnetic fields which critically affects  $\tau_{\text{eff}}$ , but do not observe the decrease in  $\tau_{\text{eff}}$  for  $z > 3$  in the presence of





**Figure 2.** The effect of cosmic magnetic fields on the effective optical depth,  $\tau_{\text{eff}}$ , as a function of redshift. Data points and error bars are from Becker et al. (2013). *Upper panel:* the magnitude  $B_1$  varies, whilst the magnetic spectral index is fixed at  $n_B = -2.99$ . *Lower panel:*  $n_B$  varies, whilst  $B_1 = 0.5$  nG.

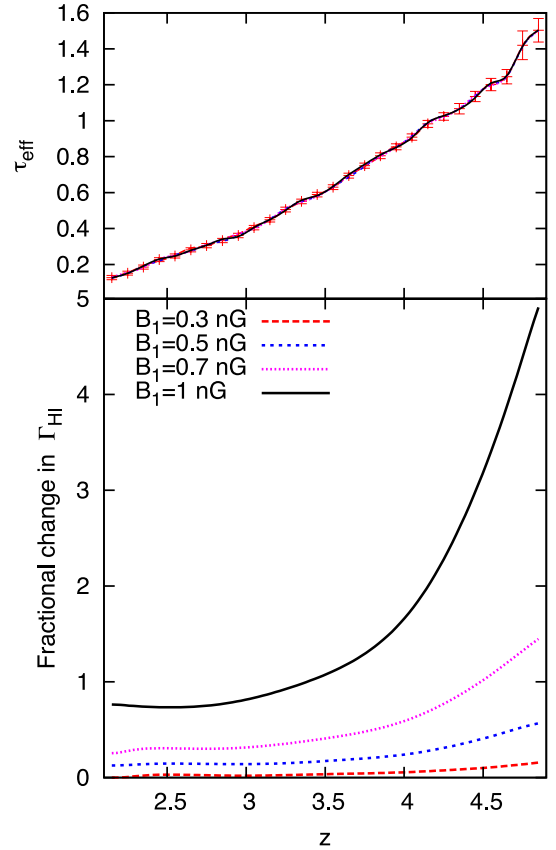
magnetic fields as they did. The reason for this is unclear, although it may be partially due to our different models of the IGM.<sup>1</sup>

Next, we examine the degeneracy between  $B_1$  and  $\Gamma_{\text{HI}}$  by readjusting  $\Gamma_{\text{HI}}$  in each redshift bin so that  $\tau_{\text{eff}}$  corresponds to the observed values (Fig. 3, upper panel). The lower panel shows the fractional increase in  $\Gamma_{\text{HI}}$  that would be inferred if magnetic fields with  $B_1 = 0.3$ – $1$  nG are assumed. The fractional increase is defined as

$$[\Gamma_{\text{HI}}(B_1 \neq 0) - \Gamma_{\text{HI}}(B_1 = 0)] / \Gamma_{\text{HI}}(B_1 = 0). \quad (34)$$

We see that the with  $B_1 = 0.5$  nG, for example, photoionization over redshift 3–5 can be roughly 20–50 percent more efficient when compared to the case without magnetic fields. With  $B_1 = 1$  nG, the increase is more extreme and the photoionization rate can be many times as large towards  $z \sim 5$ .

<sup>1</sup> Pandey & Sethi did not vary  $T_m$ ,  $\gamma$  and  $\Gamma_{-12}$  with redshift, in contrast with our approach.



**Figure 3.** The degenerate effects of cosmic magnetic fields and the photoionization rate can result in the same effective optical depth,  $\tau_{\text{eff}}$  (top panel – all four curves overlap). The lower panel shows the fractional increase in  $\Gamma_{\text{HI}}$  required to produce the upper panel, compared to the case with no magnetic fields.

## 4.2 Synthetic spectra

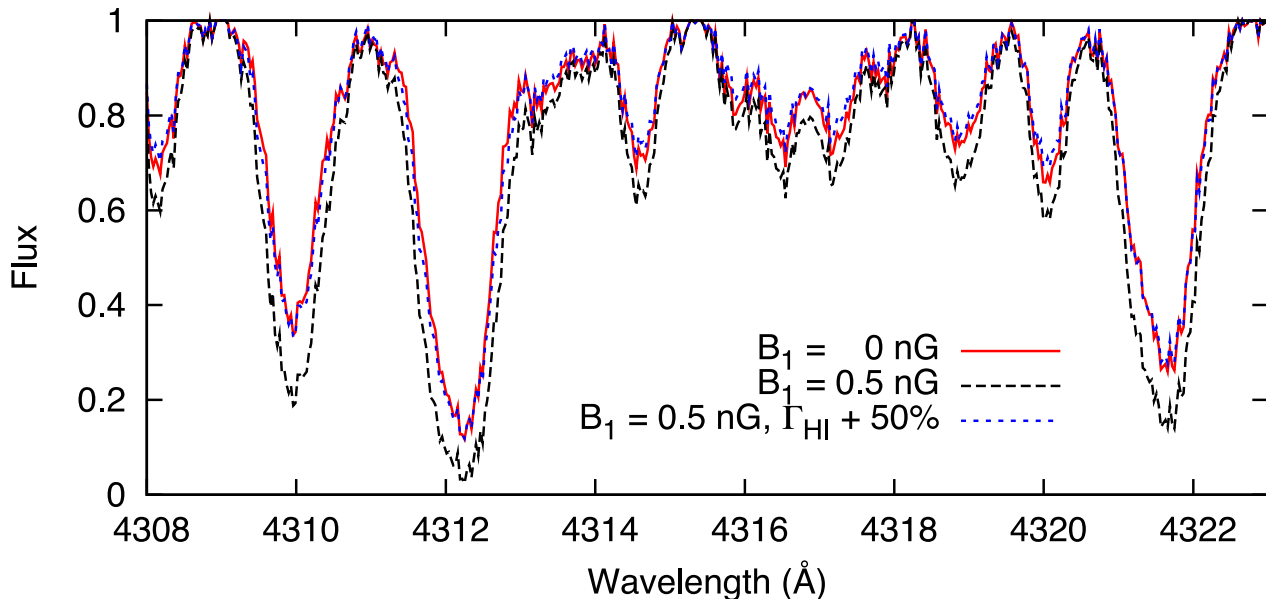
Next, we use the lognormal approach to produce synthetic QSO spectra and examine the effect of magnetic fields on the Ly $\alpha$  absorption lines in such spectra (see e.g. Bi 1993; Bi, Boerner & Chu 1992; Gallerani, Choudhury & Ferrara 2006 for previous work).

We consider pixels along a line of sight within a box with mean redshift  $\bar{z}$ . Spectra are typically measured at pixels which are equally spaced in local-velocity intervals. The optical depth of a pixel with local velocity  $v$  is given by

$$\tau(v) = \frac{cI_\alpha}{\sqrt{\pi}H(\bar{z})} \int \frac{n_{\text{HI}}(v')}{b(v')} \exp(-[(v - v' - v_b)/b(v')]^2) dv', \quad (35)$$

where  $v_b$  is the peculiar velocity along the line of sight, and the integration spans all pixels. The flux associated with each pixel is simply  $F = e^{-\tau(v)}$ .

An example of such a synthetic flux is shown in Fig. 4 for a QSO at  $\bar{z} = 2.55$  (similar to Q1017–2046; see Penprase et al. 2008). The spectrum is drawn from a  $10 h^{-1}$  Mpc section along the line of sight. To mimic the instrumental profile, the spectrum is further convolved with a Gaussian function with full width at half-maximum of  $6.7 \text{ km s}^{-1}$  (roughly the resolution of HIRES spectrograph) and resampled at velocity interval of  $2.1 \text{ km s}^{-1}$ . Finally, we also add to the flux a Gaussian noise with zero mean and  $\sigma_{\text{noise}} = 0.02$ . The resulting spectrum is shown in solid line in Fig. 4.



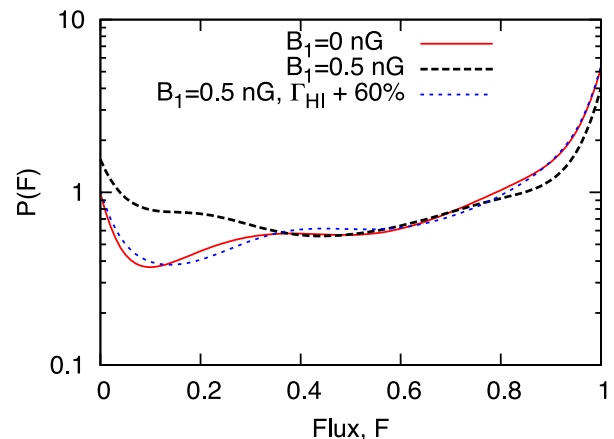
**Figure 4.** A synthetic spectrum from  $\bar{z} = 2.55$  illustrating the effect of cosmic magnetic fields ( $B_1 = 0.5$  nG,  $n_B = -2.99$ , long dashed line) on the Ly $\alpha$  forest. The solid line shows the spectrum without magnetic fields. The magnetic fields deepen and broaden the absorption troughs, as discussed in detail the text. These effects, however, can be offset by increasing the background ionization rate. In the figure, when  $\Gamma_{\text{HI}}$  is increased by 50 per cent (short dashed line), the spectrum for  $B_1 = 0.5$  nG is almost identical to the case without magnetic field.

Cosmic magnetic fields of strength  $B_1 = 0.5$  nG ( $n_B = -2.99$ ) is then added and the spectrum is recalculated. The result is shown in dashed line in Fig. 4. We clearly see the deepened and broadened absorption troughs which result from additional inhomogeneities from the magnetic fields, consistent with the findings in the previous section.

The degeneracy between  $B_1$  and  $\Gamma_{\text{HI}}$  is illustrated by the spectrum in short dashed line, where  $\Gamma_{\text{HI}}$  is increased by 50 per cent. The resulting spectrum is almost identical to the spectrum without magnetic fields, showing that increasing the photoionization rate can effectively erase the magnetic field imprints on the Ly $\alpha$  spectrum. This enhancement is slightly greater than that expected from Fig. 3, since the latter is calculated by averaging over multiple lines of sight without instrumental and noise considerations.

We further investigate if these degenerate effects on  $\tau_{\text{eff}}$  can be distinguished in the pixel flux statistics  $P(F)$ . We assume pixel bins of width  $\Delta F = 0.05$ , and normalize the flux probability density distribution,  $P(F)$ , so that  $\sum P(F)\Delta F = 1$ . Fig. 5 (solid line) shows such a flux pdf taken from synthetic spectra with  $\bar{z} = 3$ , exhibiting the usual double-peak feature (see e.g. Becker, Rauch & Sargent 2007; Kim et al. 2007). A magnetic field with  $B_1 = 0.5$  nG ( $n_B = -2.99$ ) is again added. This skews the PDF towards the region where  $F \approx 0$ , indicating deeper absorption troughs as expected. As before, we were able to mask the magnetic field imprints by enhancing the photoionization rate by 60 per cent in this case (short dashed line), producing an almost identical pdf to the case without magnetic field.

Adding a magnetic field with  $B_1 = 0.5$  nG ( $n_B = -2.99$ ) also substantially boosts the flux power spectrum, as shown in Fig. 6 (derived from the spectrum in Fig. 4). This is consistent with enhanced structure on small scales, as the flux power spectrum integrates along the lines of sight. It will in general also include the effects of larger wavelength modes. The boost is largely compensated for, however, by increasing the photoionization rate by 50 per cent, necessary to recover the mean observed transmission. As Shaw & Lewis (2012) appear not to have included the photoionizing background as a free



**Figure 5.** The normalized probability density distribution of the flux,  $P(F)$ , from synthetic spectra with  $\bar{z} = 3$ . The presence of magnetic fields with strength  $B_1 = 0.5$  nG (long dashed) skews the pdf towards  $F \approx 0$ , indicating deeper absorption troughs compared to the case without magnetic field (solid line). The magnetic signature can again be masked by enhancing the photoionization rate by 60 per cent (short dashed).

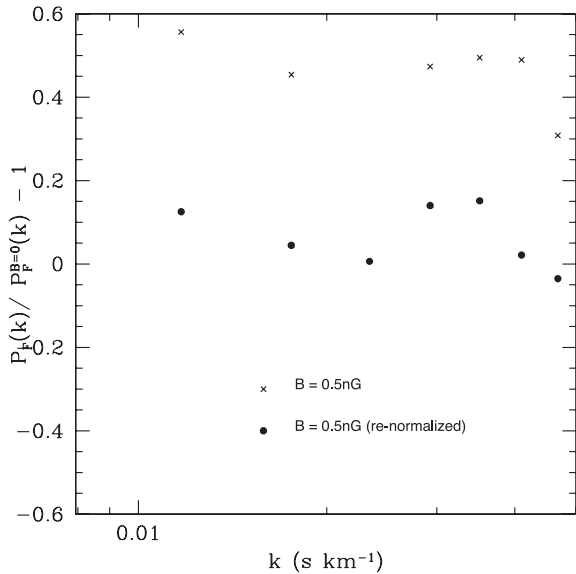
parameter, it is unclear how meaningful their Ly $\alpha$  forest constraint on a primordial magnetic field is.

In summary, this section illustrates that by introducing a sub-nanoGauss amplitude of cosmic magnetic fields, the metagalactic photoionization rate inferred from Ly $\alpha$  forest measurements can be significantly enhanced.

## 5 CONCLUSIONS AND DISCUSSION

We have shown how the ‘ionizing-photon budget’ problem can be alleviated by introducing a weak background of cosmic magnetic fields. Our main results are summarized below.

First, we showed quantitatively how cosmic magnetic fields induce baryonic density perturbations on top of the standard



**Figure 6.** The relative change in the flux power spectrum allowing for magnetic field fluctuations (derived from the spectrum in Fig. 4). The presence of magnetic fields with strength  $B_1 = 0.5$  nG (crosses) substantially boosts the power. The magnetic signature, however, is largely masked by enhancing the photoionization rate by 50 per cent (dots).

$\Lambda$ CDM perturbations, giving rise to an enhanced population of Ly $\alpha$  clouds. A weak magnetic field of order  $\sim 0.1$ – $1$  nG, coherent on scale  $\sim 1$  Mpc, with an almost scale-invariant spectrum was shown to be sufficient to produce significant impact on observables derived from high-redshift QSO spectra, including (i) the effective optical depth,  $\tau_{\text{eff}}$ , of photons to Ly $\alpha$  absorption, (ii) the spectra themselves, (iii) the pixel-flux statistics and (iv) the flux power spectrum. In all four observables, we found a consistent picture of magnetic fields creating deeper, broader absorption troughs along the lines of sight. The flux power spectrum in general will also include the effects of longer wavelength modes.

Furthermore, we examined the sensitivity of the magnetic field effects on the above observables to the assumed metagalactic photoionization rate,  $\Gamma_{\text{HI}}(z)$ . Decreasing the photoionization rate is degenerate with increasing the fluctuations in the density of neutral hydrogen induced by cosmic magnetic fields. The precise nature of this degeneracy could be explored using a likelihood analysis, but we leave this for future work.

The results in Figs 3–6 demonstrate that a subnanoGauss level of magnetic field from an almost scale-invariant spectrum is sufficient to significantly enhance the required value of  $\Gamma_{\text{HI}}(z)$ , with the amount increasing with redshift to a factor of several. This would substantially ease the tension between the number of ionizing photons per baryon required to reionize the IGM and the number required to maintain the IGM at its level of ionization afterwards, as inferred from the Ly $\alpha$  forest.

The thermal and radiative properties of the IGM are crucial in our calculations. In particular, we used values of the temperature at mean density,  $T_0(z)$ , and the polytropic index,  $\gamma(z)$ , inferred from the measurements of Becker et al. (2011). More realistically, the presence of large-scale magnetic fields would alter these parameters due to magnetic energy dissipation. The formation of the first ionized sources are also likely to be affected, meaning that  $\Gamma_{\text{HI}}$  will carry some dependence on the magnetic field strength. Some of these issues have been investigated in Schleicher et al. (2009) and Sur et al. (2010), although much larger hydrodynamical

simulations are needed to elucidate the precise relationship between cosmic magnetic fields and the IGM.

Finally, although neglected in this work, cosmic helicity may have played an important role in the amplification of seed fields through the so-called inverse cascade mechanism (Brandenburg, Enqvist & Olesen 1996) and could also leave novel imprints in the CMB (Kahniashvili & Ratra 2005). It will be interesting to investigate the imprints of helical magnetic fields on the IGM in future work.

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