Competition for space is ubiquitous in the ecology of both microorganisms and macro-organisms. We introduce a bacterial model system in which the factors influencing competition for space during colonization of an initially empty habitat can be tracked directly. Using fluorescence microscopy, we follow the fate of individual *Escherichia coli* bacterial cell lineages as they undergo expansion competition (the race to be the first to colonize a previously empty territory), and as they later compete at boundaries between clonal territories. Our experiments are complemented by computer simulations of a lattice-based model. We find that both expansion competition, manifested as differences in individual cell lag times, and boundary competition, manifested as effects of neighbour cell geometry, can play a role in colonization success, particularly when lineages expand exponentially. This work provides a baseline for investigating how ecological interactions affect colonization of space by bacterial populations, and highlights the potential of bacterial model systems for the testing and development of ecological theory.

1. Introduction

Spatial structure can have profound effects on the composition and dynamics of ecological communities. Ecological theory suggests that even in spatially uniform habitats, local neighbour interactions can lead to a variety of phenomena including competitor coexistence owing to trade-offs between life-history strategies (e.g. between local competitive ability and dispersal) [1,2], community self-organization [3], travelling waves of species dominance [4,5] and spatial variations in the prevalence of parasites or other traits [6,7]. Spatial variations in habitat type can produce even more varied ecological outcomes [8]. However, testing such predictions with well-controlled experiments on spatially structured populations is often challenging (although not impossible [9]) for ecosystems consisting of macro-organisms, i.e. animals or plants.

Laboratory studies with microorganisms provide a way to test ecological theory that can overcome many of the practical issues associated with working with macro-organisms. While a large body of work exists for protist ecosystems [10,11], the potential of bacterial populations for testing ecological and evolutionary theory has only recently become widely recognized [12], as has the importance of using such theory to understand bacterial communities in the natural environment [13]. For bacterial populations, key studies have demonstrated the importance of spatial structure in promoting competitive restraint [14], maintaining coexistence in systems with cyclic dominance [15], favouring the evolution of toxins [16] and speeding up the evolution of antibiotic resistance [17–19]. Of particular interest are recent studies of range expansion, in which patterns of clonal dominance are visualized using fluorescently labelled strains of bacteria or yeast, as a population expands across the empty surface of an agar plate [20–22]. This work has shown that neutral fluctuations at the tips of expanding populations can have strong effects on genetic diversity [23,24]. These experiments provide a powerful tool for the testing and development of theory, because fitness differences between strains can be measured with high accuracy, the spatial fates of different lineages can be tracked in detail,
and the physical and ecological interactions between individual organisms are relatively simple [25–31]. The spatial patterns formed by expanding and competing bacterial lineages are also of interest in a synthetic biology context, where the aim is to produce the controlled local patterns of differential gene expression [32].

In this paper, we use an experimental bacterial model system, combined with computer simulations, to address a different ecological scenario: the colonization of an empty terrain by initially scattered individuals that proliferate to occupy contiguous patches, competing for space at the patch boundaries. This scenario is common in ecology; examples are to be found among lichens [33], algae [34], liverworts [35], vascular plants [9] and territorial animals [36]. In such a situation, where organisms compete locally for space (or, more generally, for resources), ecological theory points to several different processes that are at play [2,36,37]: expansion competition, in which a species captures space not already occupied by another, lottery competition, in which individuals compete to occupy space released when another dies, and overgrowth, or the capturing of space by direct competition at boundaries between species. For a particular ecosystem, a key task is to determine which of these mechanisms plays the major role. More generally, one would like to predict how the various mechanisms involved influence the spatial patterns of genetic mixing which emerge.

In our experiments, two fluorescently labelled strains of *Escherichia coli* bacteria compete locally for space, starting from an initially scattered configuration on an agarose surface. We track under the microscope the fates of hundreds of individual lineages, starting from individual ‘founder cells’. In our system, cells do not die and are not motile, so that the key processes are expansion competition and direct competition at patch boundaries. By defining a measure of competitive success based on the final area occupied by a lineage, we can identify those lineages that are ‘winners’ and ‘losers’, and determine the factors leading to their competitive success (or failure). We find that both expansion competition and boundary competition can play a role in colonization success, with their relative importance being dependent on the founder cell density. More specifically, a picture emerges from our experiments, supported by our simulations, in which the competitive outcome is controlled by both founder cell lag time and ‘squeezing’ between growing microcolonies at their boundaries. We also find that the emergent spatial patterns are density-dependent, with high initial cell densities typically leading to less uniformly shaped final patches. This study provides a baseline understanding of the factors that are at play when bacterial populations colonize soft surfaces, and a baseline methodology for investigating competition for space in microbial communities more generally.

2. Results

2.1. Visualizing the fate of individual cell lineages

To track the fate of individual cell lineages during surface colonization, we mixed two differently coloured fluorescently labelled strains of *E. coli* MG1655 (initially growing exponentially in liquid culture, see Methods) in a 1:19 ratio. A small volume of the mixed culture was spread evenly on the surface of a flat agarose pad containing nutrients, and the sample was sealed with a glass coverslip. We used fluorescence microscopy to record the positions of over 1900 of these ‘founder cells’ (figure 1a) across spatial regions up to \( \approx 2 \times 10^2 \) μm. We then allowed the cells to proliferate during overnight incubation, so that the entire spatial domain became covered, before re-imaging (figure 1b–d). Figure 1 shows typical results, with the minority and majority strains shown in red and green, respectively. After the surface is colonized, distinct patches of red cells can be seen, each of which is surrounded by a ‘lawn’ of green cells. Each red patch corresponds to space that has been occupied by the progeny of an individual red founder cell, in competition with the surrounding green cells. A 1:19 ratio was chosen to minimize the number of CFP colonies sharing collision boundaries. By analysing the sizes and shapes of the red patches, we can investigate the outcome of competition for space among the founder cells.

Figure 1b–d shows the examples of individual red patches, in experiments with low (figure 1b, \( n_{\text{low}} = 1.5 \times 10^{-4} \text{cell} \mu \text{m}^{-2} \)) and high (figure 1c, \( n_{\text{high}} = 7.2 \times 10^{-3} \text{cell} \mu \text{m}^{-2} \)) average densities of founder cells. For low founder cell density, we typically obtain patches with straight edges and clearly defined corners. For high founder cell density, patch shapes tend to be more ragged.

2.2. Quantifying winners and losers

To quantify the outcome of competition for space, we need to measure the extent to which a given cell lineage succeeds in outcompeting its neighbours. Starting from the initial configuration of founder cells, we assign a spatial ‘zone’ to each founder cell by performing a Voronoi tessellation based on the founder cell positions (see Methods). Each cell’s zone consists of the region of space that is closer to it than to any other founder cell [38]. This partitioning is illustrated in figure 1a. As a null hypothesis, we suppose that, once the surface is colonized, the progeny of each founder cell will occupy the space defined by its zone. Comparing the shapes of the colonized patches which we observe in our experiments, we see that for low founder cell densities, there is indeed often a close correspondence between patch shape and the zones defined by the Voronoi tessellation (compare, for example, figure 1a,b which show the same region of space before and after colonization). For high founder cell density, colonized patch shapes tend to deviate more from the shapes of the Voronoi zones (e.g. Figure 1d). A more detailed, quantitative analysis confirms that shapes of the colonized patches and of the corresponding Voronoi zones correlate more strongly at low founder cell density than at high founder cell density (electronic supplementary material, figures S1 and S2).

To identify those cells that are ‘winners’ and ‘losers’ in the competition for space, we define a quantity that we call the ‘winner index’ (WI). This is the ratio between the colony patch area which arises from a given founder cell, and the area of its initial Voronoi zone

\[
WI = \frac{A_P}{A_V},
\]

where \( A_P \) is the final patch area arising from a given founder cell, and \( A_V \) is the area of its Voronoi zone. A value \( WI = 1 \) corresponds to a cell whose lineage has colonized only the space closest to it. ‘Winners’, or cells that colonize more
space than that closest to them, will have $WI > 1$, whereas ‘losers’, which colonize less space that that closest to them, will have $WI < 1$. Equation (2.1) does not, of course, provide the only possible definition of competitive success.

Figure 2 illustrates the shapes of the colonization patches (blue) of several ‘winner’ and ‘loser’ cells, together with the shapes of their Voronoi zones (black lines), in an experiment with an initially low cell density ($\rho_{\text{low}} = 1.5 \times 10^{-4}$ cell $\mu m^{-2}$). These images do not reveal any obvious ‘winning or losing strategy’; for example, while some winners seem to have gained territory by pushing out from their corners (figure 2a,b), others seem to have expanded more uniformly relative to their Voronoi zones (figure 2c,d).

Figure 3a,b shows the distribution of $WI$ values obtained in our experiments, for founder cells at high and low initial cell densities, respectively. In both cases, the distribution of $WI$ values is peaked around $WI = 1$, but we also observe significant numbers of winners and losers. Comparing the results for low and high founder cell densities (figure 3a,b), we see that the distribution is broader at high founder cell density. For high founder cell density ($\rho_{\text{high}} = 7.2 \times 10^{-3}$ cell $\mu m^{-2}$), the lognormal coefficient of variation ($c_v$) was $c_v = 0.61$; in contrast, for the low founder cell density experiment, $c_v = 0.31$. Thus, when the founder cell density is high, such that expanding lineages collide earlier, we obtain more deviation from the Voronoi patch shape (electronic supplementary material, figure S2 and figure 1d), and also observe more extreme effects of competition for space (i.e. more winners and correspondingly more losers).

2.3. Expansion competition can play a significant role

Ecological theory suggests that two competitive processes are likely to be important in determining the outcome of our experiments: expansion competition, in which clonal lineages ‘race’ to occupy empty space, and direct competition at the boundaries between neighbouring patches [2,36,37].

2.3.1. Tracking the early stages of surface colonization

To determine the role of expansion competition in our experiments, we measured the growth behaviour of individual cell lineages (microcolonies) in the early stages of growth, i.e. prior to collision with their neighbours, using time-lapse microscopy. We measured the lag time, or waiting time before a founder cell starts to divide [39], and also tracked the rate of microcolony expansion, once a founder cell had started to proliferate. In agreement with others’ observations [40–42], we observed significant variability in lag times among founder cells (figure 4a, mean $t_{\text{lag}} = 53$ min, with a standard deviation of 16 min). This variability is likely part owing to founder cells being at different stages of the cell cycle and intrinsic cell stochasticity (which is poorly understood) [43].

The expansion rates of growing microcolonies show much less variability: tracking the microcolony expansion rate as a function of microcolony size, we find that this varies somewhat during the first few divisions, but thereafter, the microcolonies expand exponentially with a mean area doubling time of 19.98 min and standard deviation of 0.12 min. In agreement with others [31], we also observe a transition
Axes labels are micrometres.

test the effect of lag-time variability, we manipulated the lag-

differences in the lag times of individual founder cells to be

colony expansion rates in our experiments, we expect

Because founder cell lag times are more variable than micro-

2.3.2. Manipulating lag times allows us to probe the effects

between two growth regimes, each with a different expansion

rate, at a microcolony size of about \(5.3(8) \times 10^3 \text{ mm}^2\); this has

been shown to correspond to cells beginning to penetrate the

agarose forming a second vertical layer (see electronic

supplementary material, figure S4). For simplicity, our defi-
nition of WI does not take this vertical stacking into
account; although it would be interesting to include it in
future work.

2.3.2. Manipulating lag times allows us to probe the effects

of expansion competition

Because founder cell lag times are more variable than micro-

colony expansion rates in our experiments, we expect

differences in the lag times of individual founder cells to be

the dominant factor controlling expansion competition. To

test the effect of lag-time variability, we manipulated the lag-

time probability distribution. This can be achieved by using

founder cells taken from the stationary phase of growth in

liquid culture, which have been exposed to a sublethal heat

shock (for 15 min), prior to deposition on the agarose surface

(see Methods). This treatment has been shown in previous

work to increase both the mean and variance of bacterial lag

times [44–46], and this was, indeed, the case in our experi-
iments (figure 4a compare with figure 4b). Sublethal heat

shocks of Gram-negative bacteria are believed to disable

important cellular components, with the biosynthesis of

replacements causing a delay in cell growth [45].

2.3.3. Broader lag-time distribution produces more winners

and losers

If expansion competition is a significant factor in our ex-

periments, we would expect that the broader lag-time

distribution for heat-shocked founder cells should result in

a broader distribution of WI values, with a higher proportion

of lineages that either outcompete their neighbours (owing to

relatively short lag times) or are outcompeted by their neigh-

bours (owing to relatively long lag times). Thus, we expect

our measure of WI distribution dispersion, \(c_v\), to be larger

for the heat-shocked cells than for those deposited on the sur-

face in the exponential phase of growth. This was, indeed,

the case, as shown in figure 3: for heat-shocked founder

cells, we observed that, for a founder cell density of \(1.5 \times
\)

\(10^{-4}\) cell mm\(^{-2}\), \(c_v = 0.51\), compared with \(c_v = 0.31\) for the

exponentially growing founder cells at the same cell density

(compare the WI distributions in figure 3e). We assume

that heat-shocking our cells only affects the cell lag times,

because batch culture experiments showed population

growth rates \((k)\) in the exponential phase to be the same

within error (e.g. at 32°C for RJA002, \(k = 0.0101(8)\) min\(^{-1}\)

compared with \(k = 0.0110(4)\) min\(^{-1}\) for cells previously

heat-shocked while in stationary phase. See the electronic

supplementary material, figure S4).

2.4. Boundary competition is significant at high cell

densities

Direct competition at the boundaries between colliding

microcolonies may also be an important factor in our experi-

ments. At these collision boundaries, local competitive

interactions could, in principle, involve secretion of toxins

or bacteriophage, extracellular polymeric substances or

antibiotics [47]. For example, E. coli MG1655, however, cell–cell

interactions within growing microcolonies on agarose surfaces

are believed to be mainly mechanical—i.e. generated by

physical pushing of the cells against each other, and by phys-

ical interactions between the cells and the agarose surface
(as well as the glass coverslip) [25–31]. These mechanical

interactions are expected to generate pushing forces between

neighbouring patches as they collide, influencing the final

colonies shape.

2.4.1. Correlating winner index with local neighbour geometry

provides a probe of boundary competition effects

If boundary competition is a significant factor in our exper-

iments, then we would expect the local geometry of the

neighbours of a given founder cell to affect its eventual

success. This local neighbour geometry is captured in the

geometry of a founder cell’s Voronoi patch—thus, by looking

\[\text{WI} = \frac{A}{v}\]

\[\begin{align*}
\text{A} &= \text{area of the Voronoi patch} \\
\text{v} &= \text{number of neighbours}
\end{align*}\]

\[\text{WI} = 2.02\]
growth, three agarose pads. Two measures of distribution width are quoted in the panels: the median absolute deviation (MAD) and lognormal coefficient of variation (\(v\)).

On the one hand, mean lag times (\(s\)) are typically more anisotropic when they collide. Because early-stage microcolonies tend to have already ‘buckled’ into the vertical direction when they collide. In this case, newborn cells can be accommodated in layers, reducing the horizontal outward pressure within the microcolony [31].

Our analysis showed that cells with smaller patches tended to have a higher average WI (figure 3). This was true for both the initial cell densities tested (in both cases for exponentially growing founder cells), although for the higher density (\(\rho_{\text{high}} = 7.2 \times 10^{-3} \text{ cell} \, \mu\text{m}^{-2}\), exponential growth, \(N = 340\), pooled from five mapped agarose pads. (c) Heat-shocked cells, low initial cell density (\(\rho_{\text{low}} = 1.5 \times 10^{-4} \text{ cell} \, \mu\text{m}^{-2}\), exponential growth, \(N = 16\), pooled from three agarose pads. Two measures of distribution width are quoted in the panels: the median absolute deviation (MAD) and lognormal coefficient of variation (\(v\)).

2.4.2. Founder cells with small Voronoi patches tend to be winners

for correlations between Voronoi patch geometry and WI, we can investigate the influence of boundary competition in our experiments. As a basic hypothesis, one might expect the area of the Voronoi patch to play an important role. On the one hand, cells with small patches need to gain less absolute area to achieve a large WI (because WI depends on the relative area). On the other hand, however, founder cells with large patches can produce large microcolonies, which might exert a greater pushing force upon collision. One might also expect the shape of a cell’s Voronoi patch to be significant, because this reflects the number and geometrical arrangement of neighbouring founder cells, which should affect the force balance at the boundary between colliding microcolonies. We therefore looked for correlation between the eventual success of a given founder cell (as measured by its WI value) and both the size and shape of its Voronoi patch.
shapes. In these plots, we have separated winners and those that are far apart are different in their Voronoi patch together are similar in their Voronoi patch shapes while spectra). Thus, founder cell points that are shown close (as measured by the Euclidean distance between their FD closely as possible, the dissimilarity between their shapes differences between all pairs of patches onto two dimensions. An MDS plot projects the multidimensional matrix of shape correspondence to individual founder cells by their FD spectra. Importantly, this allows us to conveniently quantify the in shape between two Voronoi patches, by computing the Fourier descriptor spectra [48]. The FD spectrum of a given shape is a list of numbers (FD magnitudes) that describe the amplitudes of different Fourier modes associated with the perimeter of the shape (for details, see Methods). The FD spectrum of an object depends only on its geometrical shape (it is independent of scaling, translation or rotation [48]). Thus, we can describe the shapes of the Voronoi patches corresponding to individual founder cells by their FD spectra. To explore the effects of Voronoi patch shape, we also characterized the shapes of individual patches, by computing their Fourier descriptor (FD) spectra [48]. The FD spectrum of a polygon and the distance between two points represents, as closely as possible, the dissimilarity between their shapes (as measured by the Euclidean distance between their FD spectra). Thus, founder cell points that are shown close together are similar in their Voronoi patch shapes while those that are far apart are different in their Voronoi patch shapes. In these plots, we have separated winners and

Figure 5. Cells with smaller initial patches are more likely to be winners. Median WI values are shown as a function of Voronoi patch size for (a) an experiment at high founder cell density \((p_{\text{high}} = 7.2 \times 10^{-3} \text{cell} \, \mu \text{m}^{-2})\), and (b) an experiment at low founder cell density \((p_{\text{low}} = 1.5 \times 10^{-4} \text{cell} \, \mu \text{m}^{-2})\). In both cases, founder cells were taken from exponential culture.

2.4.3. Voronoi patch shape differs between winners and losers

To explore the effects of Voronoi patch shape, we also characterized the amplitudes of differences in Fourier modes associated with the perimeter of the shape (for details, see Methods). The FD spectrum of an object depends only on its geometrical shape (it is independent of scaling, translation or rotation [48]). Thus, we can describe the shapes of the Voronoi patches corresponding to individual founder cells by their FD spectra. Importantly, this allows us to conveniently quantify the difference in shape between two Voronoi patches, by computing the Euclidean distance between their FD spectra (see Methods). We used this method to test for differences in the geometrical characteristics of winning versus losing Voronoi patches. Figure 6 shows our results, in the form of multidimensional scaling (MDS) plots for the high and low founder cell density experiments (figure 6a,b, respectively). An MDS plot projects the multidimensional matrix of shape differences between all pairs of patches onto two dimensions. In these plots, each point represents a founder cell Voronoi polygon and the distance between two points represents, as closely as possible, the dissimilarity between their shapes (as measured by the Euclidean distance between their FD spectra). Thus, founder cell points that are shown close together are similar in their Voronoi patch shapes while those that are far apart are different in their Voronoi patch shapes. In these plots, we have separated winners and losers by colour; the red points represent founder cells that eventually become ’losers’—i.e. those whose eventual WI is in the lowest 10% of the population, and the blue points represent founder cells that go on to become ‘winners’—i.e. those whose eventual WI is in the highest 10% of the population. Clustering among either red or blue points in the plot would indicate a ‘typical’ Voronoi patch shape for either losers or winners.

Figure 6 shows that we do indeed observe clustering between Voronoi patch shapes for eventual winners and losers (distinct red and blue clusters of points), for both the high and low founder cell density experiments (figure 6a and b, respectively), although the clustering is more marked in the high-density case. The statistical significance of this apparent clustering can be measured using multivariate ANOVA [49] (PERMANOVA; see Methods); this showed a significant distinction between the winner and loser points for both the high-density experiment \((p = 0.001)\) and the low-density experiment \((p = 0.008)\). This supports our
hypothesis that there are indeed geometrical features of the neighbour configuration that predispose founder cells towards success or failure in the competition for space, irrespective of patch size, even though these features are not immediately apparent on visual inspection of winner and loser Voronoi patches (figure 2).

2.5. Simulations reproduce our experimental results

Our experimental results suggest that the eventual success of a given cell lineage in outcompeting its neighbours depends on both the lag time before the founder cell begins to divide, and on the size and shape of the founder cell’s Voronoi patch, defined by its neighbours. To verify this picture, and to further investigate the interplay between these two factors, we performed computer simulations of a simple model.

In our simulations, the spatial habitat is represented by a two-dimensional square lattice of 500 × 500 sites. We assume that each site can be occupied by a single bacterial cell. Upon reproduction, a cell retains its original site and also produces a progeny cell which occupies a previously empty site; thus, each founder cell gives rise to a microcolony which expands in space. The simulation algorithm is described in detail in Methods. Briefly, at the start of the simulation, randomly chosen sites are populated by founder cells. Each founder cell begins to reproduce after a waiting time which is chosen from one of our experimental lag-time distributions (figure 4). The age at which a cell reproduces is chosen from a uniform distribution with range 18–22 min (based on experiments tracking the area growth of colonies on 3% agarose at early times). Upon reproduction, the progeny cell is placed at random into any of the eight sites surrounding its parent (i.e. the Moore neighbourhood), if empty. In most of our simulations, if none of these sites is empty, the progeny cell is instead placed on the perimeter of the microcolony. This mimics the fact that in our experiments, birth of new cells deep within the microcolony pushes existing cells outwards, expanding the microcolony area. If the microcolony becomes completely blocked by neighbouring cells, i.e. there are no empty lattice sites at its perimeter, its growth ceases. To mimic a scenario where cell growth could be inhibited deep within the colony (e.g. by nutrient limitation), we also carried out some simulations in which progeny cells could only be placed in sites surrounding the parent. We term these two scenarios ‘exponential area growth’ and ‘perimeter growth’, respectively.

Our simulations allow us to investigate systematically the role of expansion and boundary competition. By adjusting the lag-time distribution, we can control the extent of expansion competition. By adjusting the founder cell density, we can mimic our experiments at low and high density and control the extent of boundary competition. Finally, by switching between the ‘exponential’ and ‘perimeter’ growth regimes, we can vary the strength of ‘pushing’ interactions between microcolonies once they have collided.

Because the microcolony area is observed to increase exponentially in our experiments (electronic supplementary material, figure S4), we begin with the exponential area growth regime, in which progeny cells are placed at colony boundaries if the Moore neighbourhood of their parent is full.

2.5.1. Effects of expansion competition

We first tested whether our simulations could reproduce our experimental observation that a broader lag-time distribution led to a broader distribution of WI values (figure 3). To this end, we performed simulations in the (exponential area growth regime) with lag times sampled from our two experimental distributions: the lag-time distribution for exponential phase founder cells (figure 4a), and that for heat-shocked founder cells (figure 4b). As expected, we observed a wider distribution of WI values for the simulation with the broader (heat-shocked) lag-time distribution (figure 7). In our simulations, we are also able to correlate the lag times of individual founder cells with their eventual fate (i.e. their WI value). This analysis showed that indeed those cells with shorter lag times had, on average, higher values of the WI (figure 7b,c and electronic supplementary material, figures S5 and S6).

2.5.2. Effects of boundary competition

In our simulations, we can also eliminate the effects of expansion competition, by allowing all the founder cells to divide from the start of the simulation (i.e. removing the lag times, so that all colonies expand at equal exponential rates from the start). This allows us to investigate the effects of boundary competition in isolation. Figure 8 shows typical snapshots of the final configuration from such simulations (with different microcolonies coloured differently). In these simulations, final colony shapes are typically irregular, suggesting that there is an effect of ‘pushing’ at the boundaries between colliding colonies. This is also apparent in the WI distributions for these simulations (figure 8c,d), which are broad, showing that boundary competition has created significant numbers of winners and losers.

Repeating our analyses of Voronoi patch size and shape, we find that, as in our experiments (figures 5 and 6), in our simulations, founder cells with smaller Voronoi patches tended to be successful (figure 9), and there is clear clustering between the shapes of the Voronoi patches corresponding to ‘winning’ and ‘losing’ founder cells (figure 9, statistically significant clustering of winners and losers, p = 0.001 for both low- and high-density simulations).

Interestingly, however, founder cell density seems to have a slightly different effect in our simulations compared with our experiments. In the experiments, the distribution of WI values was broader for experiments at high founder cell density, compared with low founder cell density (figure 3a,b), and we also observed a more pronounced effect of Voronoi patch size and shape at high founder cell density, compared with low founder cell density (figures 5 and 6); although the effect of shape was statistically significant in both cases. In contrast, in the simulations, the distributions of WI values are similar in width for simulations at low and high founder cell density (4 × 10^{-4} and 1.6 × 10^{-3} cell site^{-1}, or 100 and 400 initial seed cells, respectively), and we observe similar effects of Voronoi patch size and shape for the two founder cell densities (figure 9, left and right panels). One possible explanation for this might be that in the experiments, colonies that collide when they are small (as in the case of high founder density) are still growing strictly as a single layer in the horizontal plane, whereas colonies that collide when they are larger (as in the case of low founder cell density) are already growing as multiple layers [31], so exert reduced
2.6. ‘Pushing’ interactions between microcolonies play an important role in boundary competition

In our simulations, we can change the way that microcolonies interact at collision boundaries, by switching between the ‘exponential area growth’ and ‘perimeter growth’ regimes. In the former regime, microcolonies that collide will continue to grow exponentially, adjusting their shape to fit between the gaps until each microcolony is completely surrounded. In the latter regime, growth is locally inhibited at collision boundaries such that colliding microcolonies slow, and eventually stop, their growth. This regime might correspond to a case where nutrient penetration to the inner parts of the colony is a limiting factor [30], or might loosely mimic a case where colonies grow in several stacked layers [31].

Repeating our simulations in the perimeter growth regime (again in the absence of lag times), we obtain quite different results. Figure 10 shows typical final snapshots from our simulations, for the same parameters as in figure 8, but in the perimeter growth rather than the exponential growth regime. Comparing figure 10 with figure 8, we see that in the perimeter growth regime, the final patch shapes are more regular, corresponding more closely to the Voronoi polygon areas associated with the founder cells. Analysing the effects of Voronoi patch size and shape on the final outcome of competition in this regime (figure 11), we also find that neither patch size nor shape are significant factors in distinguishing winners from losers (compare figure 11 with figure 9). These results suggest that microcolony ‘squeezing’ at the boundaries of colliding colonies may be responsible for the boundary competition effects (e.g. effects of Voronoi polygon size and shape) that we see in our experiments.

3. Discussion

In this paper, we have used a bacterial model system to investigate the ecological factors influencing competition for space as an initially scattered population colonizes a spatial domain. Our study has focused on a ‘simplest possible’ model system, in which the competing populations are identical (except for their fluorescent markers) and death, dispersal and complex ecological interactions are all absent. For this system, we can track the fates of individual founder cells as they proliferate, allowing us to define a simple measure of the outcome of competition, which we term pushing forces in the horizontal plane. This factor is not taken into account in the simulations, but could be tested in future work.
the ‘WI’. Quantifying success in this way allows us to investigate in detail the factors that influence the outcome of competition for space, at the level of individual founder cells.

In our experimental system, competition for space involves expansion competition, manifested as differences in the founder cell lag times, and boundary competition, manifested as ‘pushing’ interactions between growing microcolonies as they collide at their boundaries. The former is detectable in an effect of changing the lag-time distribution (which we achieve by heat-shocking the founder cells), and the latter is detectable in the form of correlations between the founder cell’s neighbour geometry and its eventual success. We find evidence for the importance of both these competitive mechanisms, but boundary competition shows more pronounced effects when the experiment is initiated with a high founder cell density, such that colonies collide when they are smaller. We speculate that this may be because small colonies are typically expanding asymmetrically and exponentially, in a single horizontal plane, whereas larger colonies are typically more symmetric in shape, may be nutrient-limited in their centres (although this is unlikely in our experiments) and are likely to consist of several layers of cells.

Importantly, we are able to reproduce the key features of our experiments using computer simulations of a simple model that includes only patch expansion (with a lag time) and exclusion between microcolonies at their boundaries. In our simulations, we can manipulate the growth rules to favour either expansion or boundary competition. Eliminating ‘squeezing’ of microcolonies as they collide with their neighbours, by restricting cell proliferation to the perimeter of expanding microcolonies, drastically decreases the effects of boundary competition in our simulations.

Our study is intended as a starting point in investigating competition for space among expanding microbial populations, and as such, naturally involves technical aspects that warrant further discussion. First, our analysis inevitably forces us to make a somewhat arbitrary definition of the WI. Second, we chose to end our analysis soon after the whole surface was colonized (i.e. after $\approx 16$ h); one might wonder whether our results might change over a longer timescale, as cells continue to interact at microcolony boundaries. This would certainly be interesting but from a practical point of view, very long timescale experiments are difficult owing to the tendency of the agarose pad to dry out. Third, it is

![Figure 8. Snapshots of final simulation configurations, for simulations with no lag times, in the exponential area growth regime. In both panels, the lattice is $500 \times 500$ sites, with either (a) 100 seed cells or (b) 400 seed cells. Simulations without lag times produce a spread of winners and losers, suggesting that boundary competition is important. WI distributions are shown for simulations in the exponential area growth regime, without lag times, for two founder cell densities: (c) $N = 100$ seed cells, (d) $N = 400$ seed cells.](http://rsif.royalsocietypublishing.org/)

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![Figure 8. Snapshots of final simulation configurations, for simulations with no lag times, in the exponential area growth regime. In both panels, the lattice is $500 \times 500$ sites, with either (a) 100 seed cells or (b) 400 seed cells. Simulations without lag times produce a spread of winners and losers, suggesting that boundary competition is important. WI distributions are shown for simulations in the exponential area growth regime, without lag times, for two founder cell densities: (c) $N = 100$ seed cells, (d) $N = 400$ seed cells.](http://rsif.royalsocietypublishing.org/)

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![Figure 8. Snapshots of final simulation configurations, for simulations with no lag times, in the exponential area growth regime. In both panels, the lattice is $500 \times 500$ sites, with either (a) 100 seed cells or (b) 400 seed cells. Simulations without lag times produce a spread of winners and losers, suggesting that boundary competition is important. WI distributions are shown for simulations in the exponential area growth regime, without lag times, for two founder cell densities: (c) $N = 100$ seed cells, (d) $N = 400$ seed cells.](http://rsif.royalsocietypublishing.org/)
important to note that for larger microcolonies, a second layer of cells forms prior to collision with the neighbours; i.e. growth is occurring to some extent in the vertical as well as horizontal direction [31]. This is not taken into account in our definition of the WI. One could perhaps include it by measuring total fluorescence rather than patch area, or by performing confocal microscopy, but both involve their own technical challenges.
Despite these challenges, our results do provide a clear picture of the ecological factors influencing competition for space in this system. One of the interesting results that emerge from our study is that at low founder cell density, the patches colonized by individual lineages are in the main remarkably similar to the Voronoi patches corresponding to the founder cell neighbour configurations (figure 1). This is by no means an obvious outcome, because growing \textit{E. coli} microcolonies are essentially granular materials, with complex internal cell orientations \cite{25–31}, which should lead to complicated force balances upon collision with neighbouring microcolonies. Indeed, some other studies of similar systems have reported ‘fractal-like’ patterns, in which colliding lineages form elongated, intertwined domains \cite{21,32}. Although we do see greater deviation between final and Voronoi patch shapes at higher founder cell densities (figure 1), we do not observe fractal-like patterns, even at very high founder cell densities. Although this requires further investigation in future work, our set-up does differ from previous studies \cite{21,32} in that the growing populations are confined by a glass coverslip that is firmly pressed down on them. If this does turn out to be important in determining the patterns formed, this would be an interesting manifestation of the importance of physical interactions (such as elasticity and friction) in determining the outcome of bacterial community organization \cite{30,31}.

To what extent can the approach described here be used to understand spatial competition in more complex ecological communities? Many of the complex interactions observed in macro-ecosystems exist in the microbial world; microbes show a plethora of dispersal strategies \cite{50,51}, life-history trade-offs involving lag times, survival probabilities, growth rates and yields \cite{52–54}, as well as social interactions including chemical signalling, quorum sensing, toxin and viral warfare \cite{12,55}. The effects of these factors on the development of spatially structured communities could easily be investigated by varying the microbial species and strains that compete in our experimental set-up. Interestingly, we note that recent high-throughput macroscopic studies of growing colonies of bacteria extracted from soil arrived at a similar conclusion to ours concerning the importance of variation in founder cell lag times for eventual competitive success \cite{40}; although for soil bacteria the situation appears to be more complex, because lag times were dependent on initial cell density \cite{40}. More generally, natural microbial communities often show extremely high levels of species diversity, and as yet, we lack basic fundamental understanding of how this diversity arises and is maintained, and what functional role it may play. Well-controlled laboratory experiments, in conjunction with ecological theory, are essential if we are to change this state of affairs \cite{13}.

4. Experimental methods

4.1. Bacterial strains and growth conditions

Two strains of \textit{E. coli} MG1655 were used in our experiments, one carrying a cyan fluorescent protein (CFP) reporter
construct and the other a yellow fluorescent protein (YFP) reporter construct. These strains were made by P1 transduction from strain MRR of Elowitz et al. [56] into an MG1655 background. The reporter constructs are integrated into the E. coli genome at positions on either side of the origin of replication (equidistant from the origin) and are under the control of the constitutive \( \alpha_B \) promoter [56]. Separate overnight cultures for each strain were prepared by transfer of a single isogenic plate colony (themselves sourced from freezer stocks (LB + 30% glycerol)) into 5 ml M9 medium, supplemented with glucose (0.4%) and casamino acids (0.5%; all further references to M9 include these supplements) and incubated for approximately 16 h at 37°C, 200 r.p.m., where they reached the stationary phase. Growth curves obtained from plate reader data showed no significant difference in growth rates between the two strains.

For experiments using founder cells in the exponential growth phase, a \( 10^{-3} \) dilution was performed on each strain overnight into fresh M9 medium, and cells were grown to an optical density \( \text{OD}_{600\text{nm}} \approx 0.3 \). Heat-shocked cells were prepared by pipetting 1.5 ml of stationary phase overnight culture into an Eppendorf, and placing it in a 50°C heat-block for 15 min. Liquid cultures were mixed at a 1:19 (CFP:YFP) ratio, gently vortexed and diluted to the target optical density (which determined the resulting founder cell density on the surface) using fresh M9 medium.

In a typical experiment, we obtain between 20 and 100 red patches per agarose slab (see ‘sample preparation’ below), depending on the initial cell density. Any cases where patches arising from two separate red founder cells share an interface were discarded in our analysis.

### 4.2. Sample preparation

A sterile 55 × 25 × 2.4 mm Perspex slide with a 33 mm × 10 mm hole was lightly fixed to a standard glass microscope slide using petroleum jelly, creating a 792 \( \mu \)l well. Molten 3% M9 agarose was pipetted into the cavity and a microscope coverslip used to flatten the surface. Once the agarose had solidified, the coverslip was carefully removed, revealing an agarose slab. One microlitre of diluted mixed culture was pipetted three quarters up the length of the agarose, and the slide held at an angle, so liquid culture would run the length of the surface.

After the liquid culture had been fully absorbed, a clean coverslip was carefully placed over the agarose and sealed to the Perspex frame using VALAP [57]; the Perspex frame was then also sealed to the microscope slide to ensure air tightness.

For cell lag-time experiments, the Perspex slide was replaced with a Gene Frame (Thermo Scientific), a disposable, double-sided adhesive plastic frame with volume of 125 \( \mu \)l [58]. The cell mixing ratio was 1:1, and cultures were diluted to an appropriate optical density to maximize the number of cells in a single field of view.

### 4.3. Microscopy analysis of dual-fluorescence competition experiments

In our experiments involving mixtures of CFP and YFP-expressing cells, image acquisition was performed using fluorescent microscopy with filters appropriate for detection of either CFP or YFP. An inverted Nikon Ti Eclipse epifluorescent microscope, with \( 20\times \) objective (NA = 0.75 or 0.5) and CoolSNAP HG² (Photometrics) CCD camera at \( 2 \times 2 \) binning were used for all samples. Excitation light was from a mercury lamp, passed through Chroma EYFP and ECFP filter sets. Automatic shutters controlled by MetaMorph (Molecular Devices) limited sample exposure to excitation light. A motorized stage (Prior Scientific) facilitated a precise raster scan of the sample, so relative positions of seed cells were accurately known. Following identification of seed cell positions (‘day 1’), the sample was placed in an airtight container and statically incubated overnight at 30°C, before repeating the imaging process (‘day 2’) to record the resulting colonies.

### 4.4. Time-lapse microscopy

Time-lapse microscopy was used to study the growth of microcolonies prior to collision; here, only a single strain was used. All samples were incubated at 32°C during image acquisition. Fluorescence and phase contrast time-lapse microscopy was performed on an upright Nikon E800 epifluorescent microscope with a 100× objective (Nikon, NA = 1.3, Ph3), and CCD camera (QImaging Retiga 2000R) at 1 × 1 binning. Excitation light was provided by a mercury lamp passed through appropriate filter sets. The microscope’s XYZ-stage and shutters were controlled via µManager [59], and image acquisition automated using the inbuilt ‘Oughton Focus’ autofocus algorithm. Multiple fields of view were observed in time by saving numerous XY-stage coordinates in the software.

### 4.5. Image analysis

Images were thresholded in ImageJ [60], and multiple fields of view were stitched together to form a complete, high-resolution montage of the entire surface from both day 1 and 2. The Voronoi map was generated in MATLAB using the built-in ‘Voronoi’ plugin, before being overlaid with a montage image of CFP cells, so Voronoi polygons generated by CFP cells could be identified. The CFP colonies and Voronoi polygons were then paired by identifying overlapping objects in the two images, using routines written in MATLAB® (2012a, The MathWorks).

For cell lag times, phase contrast time-lapse movies of dividing cells were manually checked for division times using CellCounter in ImageJ, and corresponding fluorescent images used to determine if the cell expressed CFP or YFP.

### 4.6. Computation of Fourier descriptors

The complex FD method provides a convenient way to characterize Voronoi patch shapes. FDs are commonly used in shape recognition analysis [48,61]. A complete description of the boundary of the shape in frequency space is captured by taking the Fourier transform of the two-dimensional boundary coordinates, expressed as a real-complex number pair. This analysis results in a list of FD magnitudes corresponding to a given shape. Here, higher frequency terms (higher-order FDs) describe smaller features of the shape, whereas lower frequency terms describe larger, more coarse-grained features. The FD spectrum of a shape is translation, rotation and scale invariant.

To compute the FD spectra of our Voronoi patches, patch-boundary pixel coordinates were extracted in MATLAB and...
ordered so they formed a closed loop of $M$ pixels. Vectors were created to store the coordinates $x_m$ and $y_m$ of each boundary pixel (where $m$ denotes the index in the vector of boundary pixels for a given patch). Because an even number of boundary points is needed in the discrete fast Fourier transform algorithm [48], the last boundary coordinate was duplicated if necessary.

The real and imaginary parts of the FDs, $a_n$ and $b_n$, were calculated from the boundary coordinates using

$$a_n + ib_n = \sum_{m=0}^{M/2} (x_m + iy_m) \left( \cos \frac{2\pi m n}{N} - i \sin \frac{2\pi m n}{N} \right),$$

where $n$ is the descriptor number and $N$ the total number of descriptors [61]. We then obtained the FD magnitude $f_n$ for each index $n$, using $f_n = (a_n^2 + b_n^2)^{1/2}$. Descriptors of order $|n| \leq 5$ were used in analysis [61]. The list of $f_n$ values for each Voronoi patch was used to characterize its shape.

### 4.7. Quantifying differences in Voronoi patch shape using Fourier descriptors

To determine if there was a difference between Fourier signatures for each Voronoi polygon associated with a loser or winner progenitor cell, MDS analysis was used. Pairwise Euclidean distances between each Fourier spectra were used to build a dissimilarity matrix, quantifying the difference in shape between pairs of Voronoi polygons associated with a given experiment. Note that in this analysis we included only patches that fell into either the top or bottom 10% of the WI distribution (i.e. ‘winners’ or ‘losers’). A two-dimensional projection of the dissimilarity matrix was created in MATLAB, and the points colour coded by their status as either winners or losers. An MDS plot was then generated from this two-dimensional projection, in which each point represents an individual Voronoi polygon and the distance between any pair of points represents the difference in their shape. To analyse the statistical significance of the apparent clustering visible in these plots (figure 6), we used PERMANOVA, implemented in the software PRIMER [49]. PERMANOVA analysis involves making multiple permutations of the dataset, randomly assigning colour labels. For each permutation, the average distance between points within and between colony colour sets is computed, and a distribution is computed for the ratio of these quantities. Comparing the ratio computed for the actual (non-permuted) dataset with this distribution allows one to assign a statistical significance to the apparent clustering seen in the MDS plot.

### 4.8. Computer simulation methods

Our discrete event computer simulations used a two-dimensional grid of $500 \times 500$ spatial lattice points, as described in the main text. We assumed that an individual bacterium occupied one lattice site, and bacteria were not allowed to overlap.

First, seed-cell coordinates were generated via a random number generator. From this, a list of cells was created (henceforth referred to as the ‘cell list’), each with an index number (which later was used to index the cell lineage). In our simulations with large times, these were sampled from the experimental lag-time distributions and assigned to seed cells at random; the cell-list was then sorted in ascending order by these lag times. If no lag time was used, then division times were assigned instead, picked from a uniform distribution with range $18–22$ min, and the cell list sorted by these division times. This range was determined from area growth rates derived from time-lapse movies of isolated microcolonies (see electronic supplementary material, figure S4).

Simulation updates were performed by jumping directly to the next division event in time. In practice, this meant looping over the cell list, previously sorted in chronological order, where each iteration of the loop encapsulated the division of one cell, with the top-most cell in the cell list the current mother cell undergoing division. Each ‘timestep’, therefore, was the difference in division time between the current and previous cell to divide, and the system state was assumed to remain unchanged between each cell division event.

For each simulation update, the top-most cell in the cell list would be dividing (the mother cell). To decide where a daughter cell would be placed, any unoccupied eight-way connected lattice sites were first checked, and one chosen at random for occupation. Both the daughter and mother cell were then assigned new division times, and sorted back into the main cell list, and the next iteration of the loop advanced, where a new mother cell would undergo division. However, if the mother cell had no free adjacent lattice sites available, the daughter cell was instead placed on the edge of the colony. To do this, a list of empty lattice sites on the edge of each colony was maintained. From this list, empty lattice sites which were within a threshold distance (defined by the user) were selected. Changing the threshold value allowed control of the manner of colony growth, such as perimeter only growth, or exponential area growth. Both daughter and mother cells were then assigned a new division times and sorted into the main cell list. If no available sites existed, then the mother cell was permanently removed from the cell list. If a mother cell tried to place a daughter cell beyond the boundary edge, it was allowed, but the new cell was not tracked. This way, the edges were treated as open, and did not confine growth. This is similar to the experimental set-up, where a microscope has a finite field of view which colonies at the edges can grow beyond. However, because we did not then know the true area of colonies that touched the edge of our simulation ‘field of view’, these colonies were not used in analysis. The simulation finished once all lattice sites were occupied by cells.

**Data accessibility.** Datasets are available for download through the following link at http://goo.gl/dQlqNV.

**Competing interests.** We declare we have no competing interests.

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### Endnote

1Correlating lag times of individual cells with winner index values is not possible in our experiments, due to insufficient objective resolution.


