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Aerodynamic roughness of glacial ice surfaces derived from high resolution topographic data

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Key Points
- High resolution topographic data permit better glacier ice aerodynamic roughness ($z_0$) estimates
- Spatial $z_0$ variability over three orders of magnitude with different temporal trajectories
- Glacier topographic roughness used to upscale $z_0$ measurements for distributed ablation modeling
Abstract

This paper presents new methods of estimating the aerodynamic roughness ($z_0$) of glacier ice directly from three-dimensional point clouds and Digital Elevation Models (DEMs), examines temporal variability of $z_0$, and presents the first fully distributed map of $z_0$ estimates across the ablation zone of an Arctic glacier. The aerodynamic roughness of glacier ice surfaces is an important component of energy balance models and meltwater runoff estimates through its influence on turbulent fluxes of latent and sensible heat. In a warming climate these fluxes are predicted to become more significant in contributing to overall melt volumes. Ice $z_0$ is commonly estimated from measurements of ice surface microtopography, typically from topographic profiles taken perpendicular to the prevailing wind direction. Recent advances in surveying permit rapid acquisition of high resolution topographic data allowing revision of assumptions underlying conventional $z_0$ measurement. Using Structure from Motion (SfM) photogrammetry with Multi-View Stereo (MVS) to survey ice surfaces with millimeter-scale accuracy, $z_0$ variation over three orders of magnitude was observed. Different surface-types demonstrated different temporal trajectories in $z_0$ through three days of intense melt. A glacier-scale 2 m resolution DEM was obtained through Terrestrial Laser Scanning (TLS) and sub-grid roughness was significantly related to plot-scale $z_0$. Thus, we show for the first time that glacier-scale TLS or SfM-MVS surveys can characterize $z_0$ variability over a glacier surface potentially leading to distributed representations of $z_0$ in surface energy balance models.

Index Terms

0738 Ice; 1814 Energy budgets; 1855 Remote sensing; 1863 Snow and ice; 1894 Instruments and techniques: modeling.
Keywords

aerodynamic roughness; ice surface energy balance; high resolution topography; anisotropy;
Structure from Motion (SfM); Terrestrial Laser Scanning (TLS)

1. Introduction

In glacier surface energy balance models, turbulent fluxes of sensible and latent heat are generally considered to be secondary to radiative heat fluxes [Hock, 2005]. However, they become increasingly influential (up to 80%) in overcast and windy conditions [Holmgren, 1971; Marcus et al., 1984; Giesen et al., 2014] and for glacierised regions characterized by maritime climates [Hay and Fitzharris, 1988; Ishikawa et al., 1992]. Critically, their relative contribution to overall ice surface mass loss is predicted to become more significant in a warming climate [Braithwaite and Olesen, 1990], making it imperative that the key influences on turbulent fluxes are better understood. One of the most important of these influences is the aerodynamic roughness height \( z_0 \), which is related to ice-surface topographic roughness, in a complex way. Improved characterisation of \( z_0 \) on glacier ice surfaces forms the focus of this paper.

All ice-melt models which aim explicitly to incorporate turbulent fluxes, in some way incorporate a value, or range of values, for aerodynamic roughness height, \( z_0 \). This is because, in the absence of direct eddy correlation measurements (which are difficult to obtain in the field; Greuell and Genthon, [2004]), aerodynamic roughness height underpins the derivation of exchange coefficients for potential temperature and specific humidity in the surface boundary layer. These coefficients are often used to approximate turbulent fluxes using the bulk aerodynamic method [Hock, 2005; Brock et al., 2010]. However, \( z_0 \) is difficult
to measure directly and a range of different approximations are used. For example, spatially distributed surface energy balance models assume a uniform and constant value of $z_0$ [Arnold et al., 2006] and $z_0$ is also used as an optimized parameter in the fitting of model output to observations of glacier melt [Hock and Holmgren, 2005].

Uncertainty in $z_0$ values presents a serious challenge in the calculation of ice ablation with an order of magnitude change in $z_0$ leading to a factor of two change in estimated turbulent fluxes [Munro, 1989; Hock and Holmgren, 1996; Brock et al., 2010]. Yet field studies have highlighted the variability of $z_0$ over ice surfaces in both space and time. Brock et al. [2006] summarize $z_0$ values for ice in the published literature, from 0.007 mm for Antarctic blue ice [Bintanja and van den Broeke, 1994, 1995] to 80 mm for very rough glacier ice [Smeets et al., 1999]. While values over smooth ice are ~ 0.1 mm, the majority of glacier ice $z_0$ values are in the range of 1–5 mm [Brock et al., 2006]. Ablation zones of glaciers can exhibit a large range of ice surface roughness features; however, attempts to model variations in $z_0$ over single valley glaciers to inform upscaling have proven unsuccessful [Brock et al., 2006]. Considering temporal variability of $z_0$, systematic increases in $z_0$ through the ablation season are observed on snow surfaces [Arnold and Rees, 2003; Brock et al., 2006; Fassnacht et al., 2009b]. However, such systematic increase is less pronounced on glacier ice which exhibits greater temporal variability in $z_0$ [Müller and Keeler, 1969; Smeets et al., 1999; Denby and Smeets, 2000; Greuell and Smeets, 2001; Brock et al., 2006; Smeets and van den Broeke, 2008]. Such temporal variability remains poorly quantified or constrained.

The calculation of $z_0$ from ice surface topography has retained assumptions put in place under conditions of limited topographic data and computational power. The aim of this paper
is to address this shortcoming through application of recent advances in high resolution surveying to estimate $z_0$ from ice surface topography. Specifically, we aim to:

1. describe novel parameterizations of surface roughness to represent $z_0$ that utilize greater availability of high resolution survey data;
2. examine the spatial variability of ice $z_0$ over the ablation zone of a small Arctic glacier using Structure from Motion;
3. investigate the possibility of upscaling microtopographic $z_0$ measurements to the glacier scale using Terrestrial Laser Scanning; and
4. characterize the temporal variability of $z_0$ as ice melt takes place over several days.

2. Meaning and measurement of $z_0$

Aerodynamic roughness height, $z_0$, is defined herein as a length scale that characterizes the loss of wind momentum attributable to surface roughness [Chappell and Heritage, 2007]; i.e. the height above the ground surface at which the extrapolated horizontal wind velocity drops to zero. The term arises as a constant of integration from the fitting of logarithmic profiles to velocity data as specified by boundary layer theory [Prandtl, 1926; Millikan, 1938] and is estimated for both water and air flows over a wide range of surface types [Smith, 2014]. Thus, under some (rough) flow conditions $z_0$ is a function of both surface and flow properties as indicated by wind-tunnel experiments observing an increase of $z_0$ with free-stream velocity (or shear velocity) over the same gravel surface where faster aerodynamically rough flows transfer more momentum to the near surface [Dong et al., 2002]. In practice, $z_0$ is at least weakly related to surface properties, and relationships between $z_0$ and microtopography are exploited frequently to obtain $z_0$ values.
With $z_0$ defined as a property of the air flow, velocity-profile based measurement would seem preferable; however, there are a number of inherent difficulties in adopting this approach. Detailed wind velocity profile measurements over sufficient durations are not always available [e.g. Brock et al., 2006; Rees and Arnold, 2006]. Data requirements are certainly too onerous for distributed measurement of $z_0$ in this way. Moreover, $z_0$ values derived from least-squares model fit to velocity measurements are sensitive to instrumental errors [Sicart et al., 2014]. On glaciers, temperature inversions and katabatic winds often result in a wind speed maximum several meters above the surface [e.g. Wallén, 1948; Denby and Greuell, 2000; Giesen et al., 2014; Sicart et al., 2014] and thus deviate from the theoretical profile. Wind velocity profiles need to be adjusted for surface-layer stability and definition of the surface height above which velocity profiles are measured is not straightforward, particularly over rough surfaces [Sullivan and Greeley, 1993; Smeets et al., 1999; Sicart et al., 2014]. Displacement heights are often defined to account for mutual sheltering through addition of a height adjustment to velocity profiles that represents a uniform distribution of the aggregate volume of roughness elements and their wakes [Smith, 2014]. However, there is some uncertainty as to the appropriate level of the zero-reference plane [Munro, 1989; Andreas, 2002].

Estimations of $z_0$ from surface microtopography show good agreement with velocity profile derived $z_0$ values [MacKinnon et al., 2004]. From wind tunnel experiments on sand surfaces, grain-size approaches have been developed [Bagnold, 1941] where $z_0$ is quantified as $1/30^{th}$ of a grain diameter. This classic approach is inappropriate for complex ice and snow surfaces that are not composed of individual grains and exhibit multiple scales of topographic variability. An equation developed by Lettau [1969] is used more frequently in studies on ice surfaces, where $z_0$ is quantified as
where $h^*$ represents the average vertical extent of microtopographic variations (i.e. effective obstacle height, m), $s$ is the silhouette area facing upwind (i.e. the roughness frontal area, m$^2$) and $S$ is the unit ground area occupied by each element (i.e. the ‘lot’ area, m$^2$). The drag coefficient is represented by an ‘average’ drag coefficient of 0.5. The Lettau equation was developed from experiments placing several hundred bushel baskets in a field upwind of an anemometer mast. With such isolated and well-defined roughness elements, specification of each term in (1) is relatively straightforward and results agreed with velocity profile-based $z_0$ values to $\pm$ 25%. However, on ice surfaces, both velocity profiles and surface roughness are more difficult to measure. Good agreement between eddy covariance, wind velocity profile and microtopographic measurement techniques over ice is often reported (e.g. Brock et al., [2006]), though differences are also apparent. For example, van den Broeke [1996] observed little agreement between the velocity profile and microtopographic methods, calculating a $z_0$ of 0.8 m from wind velocity profiles and 120 mm using the Lettau equation (the latter of which was more realistic for the energy balance; Hock, 2005).

Alternatives to (1) do exist; for example, Sellers [1965] estimates $z_0$ from $h^*$ alone, calibrating a power-law relationship empirically. Meanwhile Counihan [1971] and Fryrear [1985] use the plan area of roughness elements in place of the frontal area, and Theurer [1973] developed an equation that uses both metrics. Banke and Smith [1973] and Andreas [2011] integrate the Fourier transform of elevations for wavelengths <13 m to relate ice roughness to $z_0$. A common simplification of the Lettau equation for complex roughness
fields encountered on ice was developed by Munro [1989] [section 3.4] and applied to topographic profiles perpendicular to the wind direction. However, sheltering effects from upwind are not taken into account and the ability of single profiles to represent roughness accurately is questionable.

High resolution topographic data of glacier surfaces are increasingly available [e.g. Nield et al., 2012]. From a Digital Elevation Model (DEM) the variability of \( z_0 \) for different profiles within the DEM can be reported [Irvine-Fynn et al., 2014]. Yet with advances in surveying techniques and computational power, the advantages of the Munro [1989] method in terms of minimal data requirements and computational efficiency have become less relevant. Indeed, estimation of \( z_0 \) using profile-based methods results in much of the potentially useful topographic data in three-dimensional point clouds of ice surfaces being discarded and does not make full use of this rich topographic data source [Passalacqua et al., 2015]. It is this shortcoming that we seek to address, through the analysis of multiple point clouds derived from Kårsaglaciären, a small glacier in northern Sweden.

3. Methods and Field Site

3.1 Field Site

Kårsaglaciären (68.358739 N, 18.323593 E) is a small (~ 1 km\(^2\)) mountain glacier located in the Vuottasrita massif, part of the Abisko mountains, on the border between arctic Sweden and Norway. It presently terminates at ~ 900 m.asl into a small ice-marginal lake that is developing as the ice margin retreats from a bedrock ridge. Since around 1912 the glacier has been in a state of near constant retreat, but with some isolated areas of minor advance noted.
[Karlén, 1973; Bodin, 1993]. Since the early 1940s the glacier has been included in the Swedish national mass balance programme [Ahlmann and Tryselius, 1926; Wallén, 1948, 1949, 1959; Karlén, 1973; Bodin, 1993]. Climatic conditions at Kårsa are split between maritime (winter) and continental (summer) and dominant winds are katabatic (ice-flow parallel). Wallén [1948, 1949] estimated that turbulent fluxes were responsible for ~40% of ablation at Kårsa.

3.2 Field data collection

3.2.1 Large-Scale DEMs from Terrestrial Laser Scanning

The ablation zone of Kårsaglaciären was surveyed in July 2013 using a RIEGL VZ-1000 terrestrial laser scanner (TLS). While the maximum range of the instrument is stated to be 1400 m [RIEGL, 2012], absorbance of the narrow Class 1 infrared laser beam over the wet ice surface reduced the observed maximum range here to ~ 400 m on wet ice surfaces. The theoretical data acquisition rate was 100,000 points per second, but again this was reduced with lower point recovery on ice surfaces because of the lower reflectivity of ice at infrared wavelengths. The manufacturer stated precision and accuracy is 0.005 m and 0.008 m respectively [RIEGL, 2012]. A nominal spatial resolution of 0.1 m at 450 m range was applied resulting in an angular increment of 0.012°. At large ranges, the laser beam divergence (stated as 0.003 mm m⁻¹) is typically the largest source of error [Carrivick et al., 2015] with beam widths of 0.015 m at 500 m range. The relative orientation of the surface would also have influenced the laser beam footprint through determining the angle of incidence.
Four TLS surveys of Kårsaglaciären were undertaken between 22\textsuperscript{nd} and 24\textsuperscript{th} July 2013 from scan positions surrounding the \( \sim 1 \text{ km}^2 \) lower glacier (Figure 1A). There was little overlap between the scans on the glacier ice itself and so gaps in coverage resulted from occlusions behind obstacles or negligible returns from wet ice surfaces oblique to the TLS survey sites (Figure 1B). The first three scan positions were repeated after an interval of three days (25\textsuperscript{th} and 26\textsuperscript{th} July) to yield a second topographic model of the glacier. Accessibility and laser absorbance by snow precluded the acquisition of topographic data from the accumulation zone of the glacier. For survey control, a network of six tripod-mounted static targets was established surrounding the survey area utilising bedrock outcrops and sites clearly visible throughout the survey area (Figure 1A). Using a minimum of four targets visible from each scan position, the TLS surveys were co-registered into a single local co-ordinate system. The standard deviations (or 3D error) of the co-registrations were between 4.5 mm and 13.8 mm. The two merged scans of the lower glacier contained \( 15 \times 10^6 \) and \( 9 \times 10^6 \) points.

The open-source topographic point cloud analysis toolkit (ToPCAT) [Brasington et al., 2012] was used to unify point densities and create two glacier DEMs. A DEM resolution of 2 m was specified and cells containing fewer than 4 points were discarded (\( \sim 20\% \) of total cells). The mean cell elevation was applied to represent the glacier surface elevation and the detrended standard deviation of elevations was used to represent sub-grid roughness [Vericat et al., 2014; Smith and Vericat, 2015]. The grids of the two DEMs were aligned to enable a DEM of Difference (DoD) to be calculated. The DoD represents changes on the glacier over a three day interval; however, the exact days over which this interval spans are not identical for each scan owing to different days of occupation.
3.2.2. Plot-scale topography from SfM-MVS

To characterize finer scale topographic variability, 31 plots were surveyed using Structure from Motion Multi-View Stereo (SfM-MVS) photogrammetric techniques. The scale-dependence of $z_0$ calculation is an important consideration [Arnold and Rees, 2003; Fassnacht et al., 2009a]. Rees and Arnold [2006] observed two scale-free domains (<0.1 m and ~1 m), suggesting that the intermediate region is characterized by a definite scale. They suggest that topographic data of sampling interval of < 0.1 m and length of > 1 m with millimetric vertical accuracy is required to best represent $z_0$. Thus, plots were approximately 2 m x 2 m in size and 20 digital photographs of 6 Megapixels were taken of each plot with a Canon PowerShot G11 digital SLR camera. Images surrounding each plot were taken from 2 m above ground with angular changes of < 20° between adjacent camera locations to facilitate identification of correct keypoint correspondence [Moreels and Perona, 2007; Bemis et al., 2014]. Oblique convergent images were captured to avoid the doming effect observed when exclusively vertical images are used [James and Robson, 2014; Smith and Vericat, 2015]. Plots were distributed on the glacier surface to incorporate the greatest possible range of surface type and topographic variability and to ensure, as far as possible, good spatial coverage of the lower glacier surface (Figure 1A). Glacier surface types were classified into qualitative categories including smooth/superimposed ice, runnels, cryoconite, sun cups, blocky crystalline ice, supraglacial channels, dirty ice, light/medium/dense scree, shallow/deep crevasses and snow (Table S1).

Groups of photographs pertaining to each plot were imported into Agisoft Photoscan Professional 1.1.6, and SiM algorithms implemented, to estimate simultaneously camera positions, camera intrinsic parameters and scene geometry (see James and Robson [2012] and Smith et al. [2015] for further details). Georeferencing of the SiM point cloud was performed
using control points surveyed with a TLS. Five reflective disk targets (50 mm diameter) were fixed into the ice in the plot corners and plot centre and directed to face the nearest TLS scan position. The targets were identified in additional TLS surveys undertaken from each scan position that were focused on each plot. The 3D co-ordinates of each target (referenced to the same local co-ordinate system as the TLS surveys) were imported, and a linear similarity transformation performed to scale and georeference each SfM point cloud. Average georeferencing errors were sub-cm (see Supplementary Information Table S1). Using these coordinates the intrinsic camera parameters and scene geometry were refined and the bundle adjustment re-run to optimize the image alignment by minimising the sum of the reprojection error and the georeferencing error. Both original and optimized point clouds were calculated and MVS image matching algorithms performed to produce final dense point clouds (Figure 1C). Average point density of the final plot point clouds was >300,000 points m$^{-2}$. ToPCAT was applied to the plot-scale SfM-MVS surveys for the generation of a DEM of 5 mm resolution. While TLS surveys of each plot were performed as part of the georeferencing, the absorbance of the near-infrared laser by ice and snow was such that relatively few TLS points were observed within each plot (typically 500 points m$^{-2}$) but this was sufficient to validate the SfM-MVS point clouds.

To analyze the temporal variability of ice surface roughness, of the 31 plots, 9 were revisited after 3 days (Plots A–C, E, F, H and S–V; Figure 1A). TLS targets were replaced and re-surveyed as described above. Additionally, 3 of these 9 plots (A, B and F) were re-surveyed again a few hours afterwards.

To facilitate upscaling, the extent of each plot was mapped onto the glacier-scale TLS-derived DEM. Plot extents and DEM cells did not align perfectly owing to the variability of
plot spacing, so the mean sub-grid roughness value of all cells containing at least part of each plot was calculated to compare plot-scale and glacier-scale models. The DEM surveyed on the same day as the plot was used in each case.

3.2.3 Meteorological data

Meteorological data were recorded during the survey interval to explain the surface lowering rates observed. Air temperature was monitored every 30 minutes throughout the field campaign at an automatic weather station (AWS) located ~500 m down-valley of the glacier terminus. The AWS comprised a Campbell Scientific CR200 data logger connected to an air pressure, air temperature, relative humidity, wind speed and wind direction sensors. This AWS has been in operation since 2007 and mean July temperatures have been 8.6°C, compared to -10.6°C in February.

3.3 Validation of SfM-MVS surveys

TLS data co-incident and contemporaneous with each SfM-MVS plot survey were used to validate both non-optimized and optimized SfM-MVS dense point clouds. Cloud-to-cloud comparisons were conducted in CloudCompare (CloudCompare 2.6.1, 2016). The 3D distance between each TLS point and its nearest neighbour in the dense SfM-MVS cloud was computed and split into X, Y and Z components. Where either the X or Y components were >0.02 m, the validation point was discarded. The mean and median Z distances were calculated alongside the standard deviation and RMSE of the errors for each plot. Beam divergence and laser footprint long axis were calculated (after Schürch et al., [2011]) to estimate the error of the TLS validation data. While only negligible differences between RMSE values for optimized and non-optimized SfM-MVS point clouds were observed.
(typically ~ 1 mm), for each plot the point cloud with the lowest RMSE was used for analysis.

3.4 $z_0$ calculation

Each plot-scale point cloud was rotated to be aligned with the prevailing wind direction, observed to be predominantly down-glacier. Point clouds were cropped to ensure an approximately equal number of rows and columns. We undertook three different approaches, described in sequence below, to estimate $z_0$ from the microtopographic roughness data acquired. The first follows the method of Munro [1989] for the purposes of comparison with previous studies; the remaining two present new methods which utilize the greater volume of roughness information that can be gathered using raw and gridded TLS and SfM-MVS data sets. Differences between the three methods are summarized in Table 1.

3.4.1 Profile-based approach

To estimate $z_0$ following Munro [1989], we simplify the Lettau equation (1) by assuming that $h^*$ can be represented by twice the standard deviation of elevations of the detrended profile ($2\sigma_d$, m), with the mean elevation set to zero (Figure 2A) (similar to the ‘random roughness’ metric commonly applied to soil and snow surfaces [e.g. Kuipers, 1957; Fassnacht et al., 2009a]). Roughness elements are modeled by calculating the number of upcrossings above the mean elevation ($f$) in any profile of length $X$ (m). The frontal silhouette area of roughness elements in the profile is then estimated as

$$ s = \frac{2\sigma_d X}{2f} $$

(2)
and the ground area occupied by each roughness element (so-called ‘lot’ area), $S$ (m$^2$), is approximated as

$$S = \left( \frac{x}{l} \right)^2.$$  

(3)

Thus the aerodynamic roughness length for a given profile becomes

$$z_0 = \frac{f}{x} (\sigma_d)^2.$$  

(4)

As demonstrated in Figure 2A, (4) makes the assumption of uniformly distributed roughness elements of equal height along the profile. Despite this, Munro [1989] found that it performed well as an approximation of $z_0$ differing by only 12% from the true $z_0$ value (though note the later re-analysis of Andreas [2002] which questioned height corrections to velocity profiles implemented by Munro [1989]). Using this method, $z_0$ was calculated for every profile ($n \approx 400$) in both orthogonal directions for each plot. Since profiles should be taken perpendicular to the wind direction, to avoid confusion, we state consistently wind direction when describing the $z_0$ value. Following normality tests, the probability distribution of profile-based $z_0$ values was characterized by the mean and standard deviation of values in each orthogonal direction.

3.4.2. DEM-based approach

Profile-based simplifications, while computationally efficient, discard large volumes of potentially useful topographic data. Such simplifications are more appropriate for the situation faced by Munro [1989] where, prior to the widespread application of TLS or SfM-MVS, limited manually measured point data were available (~30 points) and more
demanding $z_0$ calculation methods cannot be supported. With a DEM-based approach, the following assumptions of the profile approach can be relaxed:

1. All roughness elements are of equal height.
2. All roughness elements are equally spaced.
3. No sheltering of roughness elements occurs.
4. The frontal area of roughness elements is equal for opposing wind directions (isotropy).

Considering the Lettau [1969] equation, a DEM-based approach enables the roughness frontal area $s$ to be calculated directly (Figure 2B) for each cardinal wind direction, thereby relaxing assumptions [1], [2] and [4]. Sheltering (assumption [3]) is implicitly represented by including only frontal areas above the detrended zero plane. Calculating the combined roughness frontal area across the plot, the planar plot area is then used as the ground area $S$ (since the ‘lot’ area per roughness element as specified by Lettau [1969] incorporates both the ground area of the roughness element and the surrounding plot area). Specifying the effective obstacle height $h^*$ is more problematic, and the rationale for the use of $2\sigma_0$ by Munro [1989] is unclear. Considering assumption [3], only points that are above the detrended plane are considered and $h^*$ is instead calculated as the mean deviation above this plane. Any single summary of obstacle height will be somewhat arbitrary; however, the mean deviation above this plane is perhaps most meaningful on an irregular ice surface. This DEM-based approach results in four $z_0$ values are generated for each plot, one for each cardinal direction.

3.4.3. Point cloud-based approach

High resolution surveying techniques produce dense point clouds containing rich information that require summary even for DEM construction. Using several simplifying assumptions, the
dense point clouds were employed here directly, for a further method of $z_0$ calculation as follows.

Raw point clouds are not of a uniform density as the feature matching process as part of the SfM-MVS workflow may oversample more visible local topographic highs owing to their greater visibility in the raw images and higher density of successful matches [Smith et al., 2015]. To yield a uniform point density the plot-scale point clouds were subsampled after detrending using an octree filter (a tree-based method of point cloud partitioning) [Meagher, 1982]. Normal vectors for each point were computed using triangulation (Figure 2C) and the number of normal vectors facing each cardinal direction (i.e. within a 90° bin centred on the cardinal direction) was counted to represent $s$ in each cardinal direction under the assumption that each point represents a comparable surface area following octree subsampling. Points below the detrended plane and ‘flat’ surfaces defined as having a normal vector greater than 80° from horizontal were not used in the estimation of $s$. The plot area $S$ was approximated by the total number of points in the cloud (approximating the 3d surface area). Finally, the effective obstacle height was calculated as the mean height above the detrended plane of all points above that plane.

4. Results

4.1 Validation of SfM-MVS

Quantitative comparison of SfM-MVS points with TLS survey points demonstrated good agreement between the two datasets. In 4 plots TLS surveys showed insufficient points for comparison with SfM-MVS owing to the poor reflectance of wet ice at the instrument
wavelength. Across the remaining 27 plots for which validation data were available, the average Mean Absolute Error (MAE) for non-optimized point clouds was 8.47 mm. Optimized SfM-MVS models performed slightly better (8.14 mm), though there was little observable difference between them (full details in Tables S1 and S2). However, MAE values were an order of magnitude below the mean of the estimated maximum error in the TLS points (69.66 mm) owing to the sometimes long survey ranges and beam divergence. Restricting analysis to situations where modeled TLS error was <10 mm, non-optimized and optimized MAE values were 6.02 and 5.55 mm respectively. Given the much shorter survey range for SfM-MVS than TLS, it is reasonable to assume that expected errors are lower from plot-scale SfM-MVS than for glacier-scale TLS and are mm-scale (see Smith and Vericat, [2015]).

4.2 Spatial variability in ice $z_0$

4.2.1. Comparison of $z_0$ calculations

Table 2 shows the results for $z_0$ calculation from the three different methods. Using the concordance correlation [Lin, 1989, 2000] which measures agreement of variables rather than linearity, we found that when averaged in all directions the strongest agreement was between DEM-based and point-cloud-based $z_0$ calculations ($\rho_c = 0.973$), with lower agreement between profile-based $z_0$ values and both DEM-based (0.730) and cloud-based (0.620) values. Separating the values into orthogonal components showed weaker agreement but a similar pattern (Figure S1). In general, point-cloud-based $z_0$ values were the highest (and had the lowest inter-quartile range) and DEM-based values the lowest, though differences between all
three calculation methods were relatively minor with a range in overall average \( z_0 \) values of just 0.247 mm (Table 2).

### 4.2.2. Variability of \( z_0 \) between plots

A wide range of \( z_0 \) values was observed across the 31 plots on the ablation zone of Kårsaglaciären (Figure 3A). Summary statistics are separated out by direction in Table 2 and values for each plot are provided in Table S3. All \( z_0 \) values were > 0.05 mm and the majority were < 3 mm. All plots containing deep crevasses and one containing shallow crevasses yielded values > 10 mm, comparable with those reported on very rough glacier ice [Smeets et al., 1999]. Plots traversed by supraglacial channels exhibited consistently high \( z_0 \) values (> 1 mm), while plots containing dirt cones on the ice surface also yielded locally high values. The presence of scree distributed over the ice surface also produces a high \( z_0 \) (~ 1 mm); however, the extent of debris cover is important with lower areal concentrations exhibiting a lower \( z_0 \) (particularly for the DEM-based approach). The lowest \( z_0 \) values were for surfaces classified as ‘smooth’, ‘slushy’ or ‘superimposed’ ice (< 0.3 mm). Intermediate values were observed for patches of snow cover, sun cups, runnels and patches classified as ‘dirty ice’ (with \( z_0 \) typically between 0.5 and 1 mm).

### 4.2.3. Variability of profile values within a plot

DEM and cloud-based methods generate a single value for the plot (for each cardinal direction), whereas extraction of profile-based \( z_0 \) values from a DEM enables multiple values to be compared for a single plot. Skewness-kurtosis tests confirmed normality of all sets of profiles; only one plot was not normal at \( P < 0.01 \) and all plots were normal at \( P < 0.05 \). With
over 400 profile-based $z_0$ measurements in each direction per plot, analysis of the standard
deviation of these values is informative (Figure 3B; Figure S2). Mean values are consistently
in line with DEM-based and cloud-based values; however, the variability about that mean is
substantial. For two plots, the standard deviation of $z_0$ is greater than the mean. In all cases
the high standard deviation of >20% of the mean $z_0$ value presents an important sampling
issue for conventional topographic profiles.

4.2.4. Anisotropy

In Table 2, the largest differences between $z_0$ calculation methods emerge when the
directionality of surface roughness is considered. Following Smith et al. [2006], an anisotropy
ratio ($\Omega$) is calculated for comparison of surface roughness in wind parallel ($z_0\parallel$) and wind-
perpendicular ($z_0\perp$) directions.

$$\Omega = \frac{z_0\parallel - z_0\perp}{z_0\parallel + z_0\perp}$$

(5)

This ratio tends towards 1 when $z_0\parallel$ dominates, towards -1 when $z_0\perp$ dominates, and 0 when
roughness is isotropic. Setting the down-glacier direction as parallel to the prevailing wind,
Figure 4 summarizes the variation of anisotropy values between $z_0$ calculations. Profile-based
metrics indicate greater $z_0$ for glacier-flow parallel winds and exhibit the largest range, DEM-
based metrics suggest generally isotropic surfaces and have the smallest range of values,
whereas cloud-based metrics highlight greater $z_0$ for winds blowing across the glacier.
Detection of anisotropy thus appears to be an important discriminant of the metrics examined
here.
A breakdown by plot is provided in Table S3 and Figure S3. The most extreme anisotropy ratio values (and the biggest differences between metrics) are observed in plots containing large surface features, such as crevasses or supraglacial channels. The specific values are sensitive to the orientation of the channel within the plot. However, no significant relationship was observed between anisotropy and $z_0$. The presence of debris often resulted in positive anisotropy ratios.

While profile-based approaches only separate orthogonal components, DEM-based analyses produced a $z_0$ value for each cardinal direction and point-cloud-based metrics can yield a $z_0$ value for any given wind direction, though here, for comparability, only values for cardinal directions have been calculated. The difference between $z_0$ for two opposing wind directions is summarized as a percentage of the average $z_0$ value (for both directions). The DEM-based $z_0$ values exhibit greater variability for opposing wind directions (32% and 22% for glacier flow parallel and perpendicular components respectively) than cloud-based $z_0$ values (9% and 12% respectively).

4.3 Modeling surface roughness at the glacier scale

Statistical relationships were explored between plot-scale $z_0$ and glacier-scale variables to provide a basis for upscaling $z_0$ beyond the plot (Figure 5A-C). Large values of $z_0$ associated with crevasses had a significant leverage over such statistical relationships. Thus, the four plots that comprise Figure 3Aii were excluded from upscaling analysis [Helsel and Hirsch, 1982]. A further plot, located in the accumulation area was excluded as there were insufficient co-incident TLS data.
No statistically significant relationships were observed between \( z_0 \) and plot mean elevation, plot distance from glacier terminus or plot mean slope. However, a significant relationship was observed between sub-grid TLS roughness and all three \( z_0 \) values; the relationship was strongest for DEM-based \( z_0 \) values (Figure 5B). This relationship presented the possibility of upscaling \( z_0 \) estimates beyond the plot to represent \( z_0 \) variability over the majority of the lower glacier (where data are available), though since differences in absolute \( z_0 \) values between methods were smaller than the natural variability of \( z_0 \) on a single glacier, all three calculation methods are likely to be equally suitable in this regard. The relationship for DEM-based \( z_0 \) values was used to provide such a glacier scale \( z_0 \) map in Figure 5D using the first TLS survey as a basis for upscaling. As plot data were only reliable where \( z_0 < 3 \) mm, only cells in this range were included.

Across the glacier, areas of relatively high \( z_0 \) values were found to be associated with crevasse features (Figure 5D) and the medial moraine running through the centre of the glacier. Considering only the 0.14 km\(^2\) area of the ablation area of Kårsaglaciären for which sufficient TLS data were available to estimate \( z_0 \), the mean modeled \( z_0 \) was 0.99 mm, the median value was 0.85 mm and the standard deviation was 0.61 mm. This is likely to be an underestimate of \( z_0 \) as some notable areas of high sub-grid roughness were not able to be included (e.g. close to the glacier terminus).

4.4 Temporal changes in \( z_0 \)

4.4.1 Glacier-scale changes
Over the 3 day TLS survey interval, a substantial amount of ice surface lowering was observed throughout the ablation zone (Figure 6A). To demonstrate that the observed lowering is not a survey artefact, the change detected in two bedrock areas was compared with that seen on the ice surface (Figure 6B and C). The two distributions are statistically different. Median change observed by TLS over bedrock was 7.28 mm (over 7,532 m² outlined in bold in Figure 6A), whereas that observed on ice surfaces was -206.99 mm (over 0.12 km²). At higher elevations within the survey area, surface lowering rates (~150 mm) are slightly less than at the glacier margins and across the lower parts of the glacier (~200 mm). Relatively high rates of lowering (~280 mm) were observed on the true right of the glacier which corresponds to the entry point of a stream running under the ice along the glacier margin, fed by a waterfall indicated in the lower left of Figure 6A. A large area at the true left margin of the glacier close to the south-facing bedrock outcrop also showed higher than average lowering (~250–300 mm). Large elevation changes (> 2 m) were also observed at the terminus where Kårsaglaciären calves into a small proglacial lake. Glacier advances and calving events can be clearly observed from the DoD at the terminus (Figure 6A) and represent the biggest elevation changes over the three day survey interval.

4.4.2. Plot-scale changes

The change in z₀ observed over the 9 resurveyed plots is summarized in Figure 7. Plots were resurveyed after an interval of 0.5, 3 and/or 3.5 days resulting in a maximum of four time periods for a single plot. Values for all three z₀ calculation metrics are presented, incorporating averaged values for all directions and values separated into both down-glacier and across-glacier averages. Analysis of the AWS record revealed that the period following
23rd July 2013 (Figure 6E) was considerably warmer than any time previously in the melt season of 2013 when average daily temperatures rarely rose above 10°C.

Despite high rates of surface lowering (e.g. Figure 6D), estimated $z_0$ values (Figure 7) remained relatively constant for three plots containing surface meltwater features (supraglacial channels or runnels). Decreases in $z_0$ were observed for plots where surface debris was observed (dirty ice or debris band) or which contained minor stress features (a shallow crevasse or crevasse traces), while increases in $z_0$ were observed where the ice was very smooth and on a plot pocked with cryoconite. All three $z_0$ values were well correlated and, as reported in section 4.2.1, point-cloud-based $z_0$ values were typically highest while profile-based $z_0$ values had the highest variability.

Over three days, observed surface lowering was typically ~0.2 m; however, three plots exhibited much higher values >0.45 m. These rapidly lowering plots covered a wide range of $z_0$ values, including the more deeply incised of the two supraglacial channels and crevasse traces and smooth ice, all of which were located in the upper ablation zone towards the true left margin of the glacier. Overall, observed surface lowering was positively correlated with degree days ($r = 0.87, n = 24, P < 0.0001$). The three rapidly lowering plots experienced surface lowering rates between 10.2 and 11.1 mm K$^{-1}$ day$^{-1}$ while other plots were between 4.2 and 7.0 mm K$^{-1}$ day$^{-1}$. 

5. Discussion

5.1 Methods for calculating $z_0$ from topographic data

Previously, collection of topographic data suitable for $z_0$ calculation required either laborious and time-consuming measurement or the construction of bespoke equipment [e.g. Herzfeld et al., 2000]. Recent advances in the acquisition of high resolution topography have revolutionized the study of Earth-surface processes [Passalacqua et al., 2015], yet the calculation of $z_0$ from ice surface topography has typically retained assumptions put in place under conditions of limited topographic data and computational power. With these restrictions lifted, the DEM-based analysis presented herein permits frontal area exposed to a prevailing wind direction to be calculated explicitly over an ice (or snow) surface. Furthermore, with alternative approximations, $z_0$ can be rapidly estimated directly from point clouds.

Overall differences between profile, raster and cloud-based $z_0$ measurements were relatively minor (Table 2). More detailed comparison of calculation methods reveals three weaknesses in the conventional topographic profile-based approach. First, calculating $z_0$ from a single topographic profile presents a sampling issue given the variability of topographic profile-based values within a single plot (Figure 3B). Similar $z_0$ variability was also reported by Irvine-Fynn et al. [2014]. Second, while orthogonal profiles are often computed, the different frontal areas from two opposing wind directions cannot be resolved. DEM-based $z_0$ values for opposing wind directions differed by $>20\%$ meaning conventional approaches may not be appropriate for anisotropic surfaces. Third, topographic profile-based $z_0$ values do not account for sheltering of an obstacle. With many ice-surface features streamlined either by wind or
water flows having continuous topographic expressions for 10s of meters or more (sastrugi, for example; Jackson and Carroll [1978]), such an assumption is limiting for glacier surfaces. This important weakness is revealed when $z_0$ values are separated into orthogonal directions (Figure 4).

In the extreme case where a crevasse or supraglacial channel is aligned perpendicular to the prevailing wind direction (Figure 8A) a detrended topographic profile will not detect this feature even if located within the crevasse or channel and would yield a relatively low $z_0$ value. Conversely, if the plot were rotated by 90° (Figure 8B) a detrended topographic profile perpendicular to the wind direction would yield a relatively high $z_0$ value. However, visual examination of the two plot surfaces in Figure 8 reveals that the plot in Figure 8A has a greater frontal area exposed to the prevailing wind, whereas the plot in Figure 8B is relatively streamlined to the wind direction. In this case computing $z_0$ using frontal area calculated from a DEM or approximated from a point cloud results in a higher $z_0$ for Plot 8A; the opposite of profile-based $z_0$ values. Such differences are not seen when uniform arrays of discrete roughness elements are present (from which the Lettau [1969] equation was derived) and are only significant where natural streamlined surfaces are the focus of study.

5.2 Spatial variability of $z_0$ and potential for upscaling

A wide range of $z_0$ values for ice surfaces is reported in the literature; yet in this study a similar range of $z_0$ values was observed over a single glacier ablation area. Our mean $z_0$ value of ~1 mm reflects the typical values reported in the literature [Brock et al., 2006]. Indeed the ‘typical’ ice roughness value of 0.66 mm that is applied in the glacier-scale distributed surface energy balance model of Arnold et al. [2006] is similar to our median modeled value.
of 0.85 mm (Figure 5D). However, considering DEM-based $z_0$ values in this study, variation over three orders of magnitude was detected from 0.05 mm on superimposed ice to 22 mm for a deep crevasse. It is clear that a single $z_0$ value cannot accurately represent the important contribution of $z_0$ to glacier melt. Prominent surface features (e.g. crevasses) result in locally high $z_0$ values. Scale-dependency of $z_0$ values requires further investigation; however, the sampling method used here captures the length scales identified by Rees and Arnold [2006].

The significance of the relationship between $z_0$ calculated from plot-scale SfM-MVS and glacier-scale TLS roughness suggests that the relevant components of topographic variability influencing $z_0$ can be approximated at the glacier scale. The modeled $z_0$ map presented in Figure 5D contains substantial data gaps, though these could be filled with a dense network of survey stations. However, caution is required since approximation of $z_0$ with a simple metric of sub-grid roughness is a considerable simplification and does not capture the directional variability observed with the more sophisticated metrics we investigated at the plot scale. Nevertheless, the relationships in Figure 5 suggest that a reasonable approximation of glacier-scale $z_0$ variability can be made using topographic data products that are increasingly available. Indeed, with the increased ease of data acquisition, upscaling $z_0$ to represent the variability over the glacier-scale becomes a distinct possibility. Existing large scale TLS [e.g. Kerr et al., 2009; Nield et al., 2012] and SfM-MVS [e.g. Immerzeel et al., 2014; Ryan et al., 2015] survey campaigns demonstrate this enhanced capability clearly.

Glacier surface energy balance calculations require estimates of turbulent fluxes of sensible and latent heat and these are typically derived from high-resolution meteorological observations alongside a single $z_0$ value to represent the ice surface [e.g. Arnold et al., 2006]. However, as this study has shown, an assumption of homogeneous $z_0$ values over entire
glacier surfaces is questionable. Derivation of a distributed $z_0$ map such as is presented in Figure 5D therefore opens up several key possibilities for those interested in modeling glacier surface energy balance. First, it allows the modeller to compare $z_0$ acquired at a point with a range of values across a whole glacier and thus assess how representative it is. Second, it permits analyses of scale dependence. Since velocity-profile measurements of $z_0$ reflect not just the surface in the immediate vicinity of the velocity profile, but are the aggregate effect of surface obstacles distributed over a larger fetch area, a $z_0$ value for a single 4 m$^2$ cell in Figure 5D cannot be directly compared with velocity profile derived $z_0$ values at that same point. Rather, aggregation of heterogeneous $z_0$ values over areas representing an estimated fetch of the wind enables comparison with wind-profile derived values [Panofsky, 1984]. The distributed nature of $z_0$ in Figure 5D will also assist with future calculations of varying $z_0$ values with varying wind direction. Finally, given that many inputs to surface energy balance models are gridded datasets, the inclusion of a dynamic and distributed $z_0$ map, rather than a single assumed value, is a logical next step.

5.3. Temporal variability of $z_0$

Our observations of temporal variability in ice surface roughness with surface melt were acquired on Kårsaglaciiären during a short period of relatively high air temperatures and agree with previously reported findings [e.g. Brock et al., 2000, 2006; Smeets and van den Broeke, 2008]. Ice with surface debris or small amounts of dirt on the surface tended to become smoother, as did surfaces exhibiting small crevasse features suggesting preferential melting out of protruding roughness. Supraglacial channels did not exhibit such a decline in roughness possibly as down-cutting kept pace with preferential melting. This variable
response contrasts with the systematic increase in roughness observed on melting snow surfaces [Fassnacht et al., 2009b].

Substantial surface melt was recorded over just 4 days (Figures 6 and 7). Average surface lowering was 0.2 m and showed a similar association between surface lowering rates and degree days as reported for Norwegian glaciers by Laumann and Reeh [1993] (5.5-7.5 mm K$^{-1}$ day$^{-1}$) and rates are similar to the maximum values reported in Wallén [1948]. Three plots showed substantially higher surface lowering rates; these could not be discriminated by surface roughness or other features and instead appeared to reflect variation in incoming radiation being relatively flat plots positioned close to a south-facing slope. Although surface lowering rates were rapid, the monitoring interval of just 4 days is insufficient to quantify the full range of ice roughness variability through the melt season. With a longer monitoring period over seasonal timescales, a wider range of roughness values is likely to be observed.

5.4. Further work

The alternative $z_0$ calculation methods introduced here require validation using velocity-profile or eddy-correlation data [Nield et al., 2013]. Similarly, modeled $z_0$ variability at the glacier scale requires validation both through finer scale measurements and through incorporation into spatially distributed surface energy balance models that are in turn validated against proglacial stream discharge measurements. Velocity profile data are needed alongside the distributed $z_0$ map of Figure 5D and map of glacier surface change in Figure 6A to validate the novel approach of $z_0$ estimation outlined herein and to examine the relevant scales at which to aggregate microtopography-derived $z_0$ estimates. With glacier-scale topography acquired through TLS or SfM-MVS, distributed energy balance models have the
potential to incorporate sophisticated models of insolation by calculating shading from valley topography directly. Orthophotograph mosaics are a further output of plot-scale SfM-MVS that could be used to estimate surface albedo directly [Dumont et al., 2011; Rippin et al., 2015]. In addition, glacier-scale surveys may be able to bridge the gap between microtopography and satellite remote sensing of glacier surfaces for a more extensive upscaling of $z_0$ as demonstrated by Blumberg and Greeley [1993] and investigated on glacier surfaces by Rees and Arnold [2006].

Conventional methods of estimating $z_0$ from topographic profiles make several assumptions about the nature of the surface which is typically simplified as a regular array of uniform roughness elements (e.g. Figure 2A). Here we have presented a novel method of calculating $z_0$ directly from high resolution DEMs that does not rely upon such simplifying assumptions. However, further investigation as to the specific parameters used in $z_0$ calculation (detailed in Table 1) is required, particularly the representation of effective obstacle height.

Sheltering of surfaces has been studied in detail in the atmospheric sciences and in investigations of aeolian erosion [e.g. Garratt, 1992; Bottema, 1996; Chappell and Heritage, 2007]. While Garratt [1992] suggested a displacement height of $0.7h^*$ for most natural surfaces, the assumption made in Table 1 (for DEM-based and cloud-based $z_0$ calculations) was that frontal areas below the detrended plane level would be effectively sheltered. For the ice surfaces investigated herein, roughness element density (i.e. frontal area divided by surface area; Wooding et al., 1973) was <0.13 in all plots aside from one deeply crevassed plot and thus still within the range for which the Lettau [1969] equation holds. Certainly more sophisticated sheltering parameterisations should be investigated [see Raupach, 1992; Chappell et al., 2010] and the availability of high resolution topographic data facilitates more
direct inclusion of mutual sheltering of roughness elements [see Smith, 2014]. Similarly, the average drag coefficient of 0.5 used here is likely to be an overestimate for many glacier surfaces which tend to be streamlined [Wieringa, 1993; Smeets et al., 1999] in at least one direction and would thus exhibit a much lower drag coefficient [Powell, 2014]. As demonstrated in Figure 8, the degree of streamlining and hence the drag coefficient may be dependent on the wind direction.

6. Conclusions

Through direct representation of the surface area of roughness elements more sophisticated parameterisations of $z_0$ from ice surface topography can be realized from high-resolution three-dimensional survey data. Properties of surface roughness that best represent the process of momentum transfer from air flows to the ice surface can be quantified directly, enabling calculation of $z_0$ from topographic data to better reflect the underlying theoretical equations. When averaged over all cardinal wind directions, there is little difference between the novel DEM-based $z_0$ values and values calculated from profiles using assumptions on the form of surface roughness. However, large differences emerge when $z_0$ is calculated separately for each wind direction, particularly where surface roughness is anisotropic.

The aerodynamic roughness of ice surfaces can be estimated at the glacier scale using a relationship established between $z_0$ and sub-grid roughness of topographic models gridding at the meter-scale. Such upscaling is important considering: (i) the wide variability of $z_0$ over three orders of magnitude over a relatively small glacier ablation zone; (ii) the lack of a statistical relationship between $z_0$ and more general topographic variables such as elevation and slope; and (iii) the relatively large effect that $z_0$ variability has on estimations of turbulent
heat fluxes and glacier ice melt, particularly in the context of future climate warming. With increased availability of high resolution topographic data at the glacier scale, surface energy balance models can incorporate distributed $z_0$ parameterisations and better predict rates of ice loss under climate change scenarios.

**Acknowledgements**

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**References**


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**Tables**

**Table 1.** Summary of $z_0$ calculations.

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Profile-based</th>
<th>DEM-based</th>
<th>Cloud-based</th>
</tr>
</thead>
<tbody>
<tr>
<td>Drag coefficient</td>
<td></td>
<td>0.5</td>
<td>Mean height of all points above the detrended plane</td>
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<tr>
<td>Effective obstacle height $h^*$ (m)</td>
<td>$2 \times$ detrended standard deviation of profile perpendicular to wind</td>
<td></td>
<td></td>
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<tr>
<td>Ground area $S$ (m$^2$)</td>
<td>For each ‘roughness element’ separately: $(X/f)^2$.</td>
<td></td>
<td>Full plot planar area approximated by number of points after octree subsampling. No units.</td>
</tr>
<tr>
<td>Silhouette area $s$ (m$^2$)</td>
<td>Uniform roughness elements approximated. Frontal area of a ‘typical’ roughness element calculated using equation 2 (see Figure 2A).</td>
<td>Exposed frontal area for each cardinal direction calculated across whole DEM. Only includes areas above detrended plane.</td>
<td>Surface area facing each cardinal direction estimated by counting number of points with normal vector $45^\circ$ either side of that direction. Only points above detrended plane where normal vector is $&lt;80^\circ$ from horizontal. No units.</td>
</tr>
</tbody>
</table>
Table 2. Summary of $z_0$ values for all 31 plots. The wind direction is given (i.e. wind blowing from ‘up-glacier’ or from the ‘true left’, etc.). Thus, ‘glacier flow parallel’ profile-based values are for profiles orientated across the glacier surface (i.e. perpendicular to the wind direction). Robust metrics provided owing to the non-normality of the dataset (see outliers on the right panel of Figure 2A). IQR = Inter Quartile Range.

<table>
<thead>
<tr>
<th>Z0 method</th>
<th>Direction (wind)</th>
<th>Overall average</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Up-glacier</td>
<td>Down-glacier</td>
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<td>Profile</td>
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<td>Median (mm)</td>
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<td>IQR (mm)</td>
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<td>DEM</td>
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<td>IQR (mm)</td>
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<td>Point Cloud</td>
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<tr>
<td>IQR (mm)</td>
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<td>0.883</td>
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</tbody>
</table>
**Figures**

![Figures](image)

**Figure 1.** Study site. (A) Scan positions, targets and plot locations overlaid onto an orthophotograph of lower Kårsaglaciären generated from glacier-scale SfM-MVS (not contemporaneous with plot surveys and used to generate an orthophotograph only). See Table S1 for plot descriptions. Note the location of Scan 2 varied slightly between the two surveys; (B) oblique viewpoint of TLS point cloud of the lower Kårsaglaciären rendered by return reflectance (dB) displaying areas of wet ice oblique to the TLS that exhibited low point density (in black); (C) example SfM-MVS plot dense point cloud viewed obliquely (Plot A, supraglacial channels, approx. 2 x 2 m).
Figure 2. Schematic illustrations of $z_0$ calculations. (A) Conventional profile-based approach (shown for Plot N). Upcrossings are defined as points where the profile crosses the detrended mean moving from below the mean to above the mean. (B) DEM-based approach highlighting frontal area for two orthogonal wind directions. (C) Demonstration of normal vectors on a triangulated wireframe mesh of a point cloud (Plot N, for illustration only).
Figure 3. (A) Variability of $z_0$ between plot surfaces (ordered by $z_0$ DEM). See Table S3 for values. Plot IDs provided in parentheses (see Figure 1A for locations). Directionally averaged $z_0$ values are presented for each plot. (B) Relationship between mean and standard deviation of profile-based $z_0$ values presented separately for each orthogonal direction. Note log-log scale.
Figure 4. Summary of anisotropy ratio values for each method of $z_0$ calculation.
Figure 5 (A-C) Relationships between directionally averaged $z_0$ values and sub-grid TLS roughness (represented by the detrended standard deviation of elevations). Model fits correspond to the regression parameters indicated (excludes Plots F, H, I and Y). (D) Map of modeled glacier $z_0$ using TLS-derived sub-grid roughness to upscale DEM-based $z_0$ (2 m resolution). Gaps relate to areas with insufficient TLS data to compute sub-grid roughness or areas where predicted $z_0$ is $> 3$ mm and beyond the range of the relationship demonstrated in Figure 5B. The distribution of modeled $z_0$ values is shown (inset).
Figure 6. (A) DEM of Difference from repeat TLS over a three day interval. Bedrock areas are outlined in black. The waterfall supplying a subglacial stream is indicated with a white arrow. (B) Frequency histogram of observed topographic changes for ice surfaces and (C) for rock and proglacial debris surfaces. Only changes ±0.5 m shown for clarity. (D) Example of lowering observed from repeat SfM-MVS dense point clouds (‘Dirt Ice’ Plot E over a 3 day interval showing an average surface elevation change of 0.23 m); (E) 30-minute smoothed temperature data recorded at the AWS over the survey interval. Mean daily temperatures reported for each day. A data gap spanning 24\textsuperscript{th} and 25\textsuperscript{th} July has been interpolated (dashed line).
Figure 7. Plot-scale changes in $z_0$ values with surface lowering over several days of intense melting (Figure 6E). Note different scales on $z_0$ axes for improved clarity of changes within each plot. Plot IDs are indicated in the top-right corner of each panel and relate to Figure 1A. Survey intervals were not exactly contemporaneous with the DoD in Figure 6A.
Figure 8. Demonstration of differences between $z_0$ anisotropy ratios for different calculation methods. The plot surface in (A) is rotated through 90 degrees in (B), while the prevailing wind direction remains constant. A greater frontal area is exposed to the prevailing wind in (A); however a profile perpendicular to the wind direction shows greater topographic variability in (B).