Molecular dynamics simulations of compression tension asymmetry in plasticity of Fe nanopillars

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Abstract

Tension-compression asymmetry is a notable feature of plasticity in bcc single crystals. Recent experiments reveal striking differences in the plasticity of bcc nanopillars for tension and compression. Here we present results from molecular dynamics simulations of nanopillars of bcc Fe in tension and compression. We find a totally different deformation mechanism applies in the two cases: dislocation glide in compression and twinning in tension. This difference explains experimentally-observed asymmetry in the nanopillar morphology.

Keywords:
Nanopillar, Plasticity, Molecular Dynamics, Dislocations, Twinning

1. Introduction

The development of micro-mechanical testing on single crystals [1] has enabled the study of plastic deformation to be taken to the microscopic level. Under uniaxial compression of single crystals, yield can be observed on a single slip plane. Samples can now be tested in both tension and compression, and there is a marked contrast between the shear banding in compression and twinning observed in tension[2]. Recent work has shifted to bcc materials, where again asymmetry is observed.

For dislocation motion, FCC materials generally obey Schmidt’s law: a dislocation moves once the shear stress on its glide plane exceeds a critical magnitude. Thus Schmidt’s law predicts identical behaviour under tension and compression. By contrast, BCC materials typically do not obey
Schmidt’s law: dislocation behaviour depending on stresses outside the slip plane. This can be traced to the core structure of dislocations.

Recent experiments by Kim and Greer revealed a tension-compression asymmetry in the plasticity of bcc nanopillars [3, 4, 5, 6]. In compression, they observe plastic deformation confined mostly to narrow slip bands, and stress vs strain behaviour characterised by many strain bursts. This stress vs. strain signature would suggest deformation by dislocation nucleation and motion. In tension they observe necking, and the stress vs strain behaviour revealed larger periods of almost constant flow stress. Kim and Greer suggested that the twinning-antitwinning asymmetry could be a cause for the compression-tension asymmetry[3]. However, their experiments cannot determine what processes were occurring at the atomic level. Molecular dynamics simulations can be used to study such atomic level processes.

The dependence of the critical resolved shear stress (CRSS) on the sense of shear (i.e. tension or compression) is a feature of bcc single crystals [7, 8, 9]. Initial explanations for this phenomenon focused on twinning-antitwinning slip asymmetry. \{112\}\{111\} type twins in bcc crystals can be viewed as \(\frac{1}{2}\langle111\rangle\) dislocations split into \(\frac{1}{6}\langle111\rangle\) fractional dislocations which spread out on subsequent planes to create a twin plane [10]. The movement of these fractional dislocations is only permitted in one direction on a given \langle 111 \rangle axis in order to create a twin boundary. Glide in the opposite direction (the anti-twinning direction) creates an unstable stacking fault which is not a twin plane. The CRSS for glide of \(\frac{1}{6}\langle111\rangle\) fractional dislocations in the twinning direction is therefore lower.

Work by Vitek et al gives further weight to this argument[11, 12]: In this study, the gamma surface for a \{112\} plane was calculated using a Finnis-Sinclair potential, and an asymmetry in the \langle 111 \rangle direction was found. For a crystal in a fixed orientation, relative motion of subsequent slip planes in compression will always be in the opposite direction to relative motion of subsequent slip planes in tension. The directional asymmetry in the glide of dislocations is consequently thought to result in a compression-tension asymmetry for single crystals [11, 8, 3, 4, 5]. Further study[11, 13, 14] revealed another mechanism for CRSS dependence on the sense of shear. Molecular dynamics calculations showed that the core structure of dislocations in bcc materials was altered by non-glide shear stresses. Due to a three-fold symmetry in the core structure of \(\frac{1}{2}\langle111\rangle\) screw dislocations in bcc, the change in the core structure depends on the direction of the shear stress. Unlike the twinning-antitwinning asymmetry, these changes in the core structure affect
slip on all slip planes, not just glide on \{112\} planes.

Previous molecular dynamics studies of plasticity in nanopillars of bcc Fe have focused on tensile strains. Observed plasticity mechanisms for tension have varied, with some studies reporting deformation by dislocations and phase transitions while others report deformation by twinning. These differences in plasticity behaviour may be due to a number of factors, including the potentials used and differing pillar geometries. In particular, the value for the difference in energy per atom between the fcc and bcc phase of the material can differ significantly across different potentials. Using a potential where this energy value is low may result in a tendency for bcc Fe to change to fcc in certain parts of the system under the influence of an applied stress or strain. The crystallographic orientation of the surfaces of the pillars may also affect the simulation results. It is energetically favourable for bcc structures such as nanopillars to have low energy \langle 110 \rangle surfaces. Pillars containing high energy surfaces may have a tendency to deform in a way which allows surface reconstructions to occur as reported by Ackland in fcc nanopillars [15]. The direction of the compression or tension could also affect the plasticity behaviour as the tendency to observe dislocation glide in a material depends on the schmidt factors for the slip planes in the pillars and these schmidt factors in turn depend on the direction of the applied strain. Here we offer a brief overview of previous molecular dynamics studies of plasticity in Fe nanopillars.

Zhang et al [16] performed simulations of tensile strain of nanopillars oriented along \langle 100 \rangle and \langle 110 \rangle directions. The \langle 100 \rangle pillars contained \{100\} type side surfaces and the \langle 110 \rangle pillars contained two \{100\} and two \{110\} type side surfaces. Deformation was observed to occur by dislocation glide in the \langle 100 \rangle pillar and by a phase transformation from bcc to fcc in the \{110\} pillars. This dependence of plasticity behaviour on pillar geometry may be due to the different crystallographic surface orientations in the side faces of these two pillars as well as differing schmidt factors for slip planes in each pillar. The potential used in this study was one for Fe developed by Mishin et al [17]. For this potential, the difference in energy per atom between the fcc and bcc phases is 50 meV [17]. This value is lower than calculated in many \textit{ab initio} calculations which typically give values between 70 meV and 120 meV [18, 19, 20, 21].

Simulations of tensile strain of bcc Fe nanowires were also carried out by Sandoval and Urbassek [22]. They constructed pillars oriented along \langle 111 \rangle with a circular cross section. In this study deformation was found to occur
by a phase transformation from fcc to a combination of fcc and hcp. The potential used in this study was one for Fe developed by Meyer and Entel [23]. The energy difference in energy per atom between the fcc and bcc phases is 40 meV for this potential [18, 23] which is again rather low in comparison to values calculated in \textit{ab initio} calculations.

Li \textit{et al} [24] performed simulations of tensile strain on \{100\} pillars with \{110\} type side surfaces. Deformation was found to occur by twinning. The potential used in this study was one developed by Mendelev \textit{et al}[19] for which the difference in energy per atom between the fcc and bcc phases is 120 meV.

The phase transitions observed in the simulations by Zhang \textit{et al} and Sandoval and Urbassek are most likely the result of using potentials with low values for the difference in energy per atom between the fcc and bcc phases. This is evidenced by the lack phase transitions in the simulations by Li \textit{et al}. In this study, we use a modified version of the Mendelev \textit{et al} potential as the difference in energy per atom between the fcc and bcc phases lies within the range of values typically found from \textit{ab initio} calculations. We construct nanopillars containing low energy \{110\} type side surfaces to avoid possible surface reconstructions which could occur in order to generate low energy surfaces on the pillars as the strain is applied.

One might speculate that the observed tension-compression asymmetry in bcc nanopillars is related to the intrinsic non-Schmidt behaviour of the dislocations. Alternately, one might argue that the mechanism should be the same as for fcc materials. Here we use molecular dynamics simulations to simulate the tension-compression asymmetry in nanopillars of bcc Fe. We show that the asymmetry is due to different deformation mechanisms: dislocation glide in compression and twinning in tension. For completeness, we also examine fcc nanopillars and find no such effect.

2. Simulation Details

Our system consisted of a pillar with a square cross-section in between two "indenter plates" as seen in figure 1(a). The pillars had approximate dimensions of 5.8×5.8×15.4 nm and contained 45513 atoms. The sample is confined by the indenter plates, each containing 9901 atoms (12.1 nm × 12.1 nm × 0.9 nm). Movement of indenter plate atoms is constrained in order to apply external forces. The side faces of the pillar were \{110\} type faces and the pillars were compressed in the [001] direction. It is necessary to have
faces on the pillar as these are the lowest energy surfaces. Creating a pillar with higher energy surfaces will result in recrystallization during the simulation and this has been shown to have create spurious deformation behaviour[15].

Prior to loading, all pillars were heated to 300K by running a simulation for 50 picoseconds with a Nosé-Hoover thermostat[25, 26]. Uniaxial strain was applied by moving the indenter plates and rescaling the atomic coordinates in the direction of loading by 0.05% at 2 picosecond intervals. The resulting strain rate is $2.5 \times 10^8$ s$^{-1}$. This method of compressing the system, by rescaling the coordinates of the atoms in the compression direction, is required so that a shock wave is not produced in the pillar. Since the thickness of the pillar may change through the simulation, “stress” on the sample is not easily defined: we measure the force required to hold the indenter plate in position, converted to a stress by dividing by the indenter area. Simulations were carried out using the MOLDY molecular dynamics code[15]. The potential function used was that developed by Hepburn and Ackland [27].

Images were created using AtomEye[28] some analysis of dislocations was carried out using the OVITO package [29].

3. Results

3.1. Compression

![Figure 1](image)

Figure 1: (a) Pillar prior to applied strain, with the atoms in the plates at the top and bottom of the pillar constrained. (b) Pillar following a compressive strain of 26%
Under compressive strain-loading, deformation in the pillars was mediated mainly by dislocation glide. Dislocations are created at the surfaces of the pillars when the stress is high and move quickly through the pillar. Typically, ⟨111⟩ dislocations form at corners, which allows them to be short but requires a mixed edge-screw character. This gives characteristic bursts of deformation leading to sudden decreases in stress, as can be seen in the graph in figure 2(a). Each sudden drop in pressure on the indenter plate happens when a dislocation is created and moves through the pillar, creating a discrete strain burst. This behaviour is qualitatively similar to stress vs strain signatures obtained by Kim et al.[5] in experimental studies of nanopillars of Nb, which can be seen in figure 2(b). Each dislocation slip event creates a step on the surface of the pillar. Figure 1(b) shows an image of a pillar following a strain of 26%. Many steps in the surface of the pillar due to dislocation glide activity can be seen in this figure.

Initially, the flat side surfaces provide the only nucleation sites, and yield depends on dislocation nucleation from perfect {110} side surfaces. At the initial yield corresponding to the first peak in figure 2(a), several dislocations are nucleated from the boundaries of the pillar simultaneously. Subsequent dislocation glide events generally involve the nucleation and glide of a single dislocation line from the side faces of the pillar.

It may be possible to predict when the dislocation glide events occur in the simulation and what the pressure on the indenter plates is immediately prior to yielding. Alternatively these values may occur at random for each dislocation glide event. To test whether these values were deterministic or occurred at random, we repeated the compression simulation 60 times. In all 60 simulations the first dislocation creation event occurs at an indenter pressure of 2GPa and at a strain of about 7.5%. Many dislocations are created almost simultaneously at this point. Subsequent dislocation creation and glide events occur stochastically within a range of indenter pressure values and at varied values of strain. This is illustrated by figure 3. Figure 3(a) shows plots of indenter plate pressure vs strain for 60 different simulations superimposed on one graph. From this graph, it can be seen that the indenter plate pressure and strain values at the initial yield point are the same for all simulation runs. These values are distributed at random for subsequent dislocation glide events. This interpretation is confirmed by the average indenter plate pressure vs strain graph shown in figure 3(b) which shows the pressure on the indenter plates at various strain values averaged over the 60 different pillar compression simulations. As the data is averaged over many
simulation runs, the indenter plate pressure approaches an approximately constant value after the initial yield due to the random positions of the stress peaks associated with each dislocation glide event.

Comparing with nanopillar experiments we see similar bursts of deformation: in our strain controlled experiments this manifests as a sharp drop in stress at fixed strain, whereas under stress control the same mechanism would give sharp increase in strain at fixed stress. The experimental boundary conditions mix stress and strain control, hence the same mechanism manifests as simultaneous strain increase and stress drop. The lower stresses required to initiate subsequent bursts is due to the roughening of the pillar having lowered the potential energy barrier for dislocation creation at the surface. The dislocation creation events after the first one typically involve the creation of just one dislocation.

The sequence of images in figure 4 shows a typical occurrence of dislocation glide. \( \frac{1}{2}(111) \) dislocations are created at the corners of the pillars. Initially the dislocation lines are curved and have a mixed edge/screw character. As the dislocation lines grow in length the dislocation line becomes straight and the dislocation has pure screw character. Each dislocation glides on many different \( \{110\} \) planes as a high degree of cross slip occurs. The dislocations continue to glide and cross-slip along the direction of highest shear stress until they reach one of the pillar surfaces, where they leave a step behind. The process then repeats.

3.1.1. Dislocation Geometry

The compression mechanism is clearly dislocation-based. Using the dislocation extraction algorithm (DXA) developed by Stukowski and Albe [30] we find that all dislocations have \( \frac{1}{2}(111) \) Burgers vectors. Dislocations could also be identified by measuring centrosymmetry of nearest and second nearest neighbours of atoms with respect to the atom in question. A numerical measure of this central symmetry can be found using the centrosymmetry parameter defined by Kelchner et al [31].

3.1.2. Atomic Shear Strain Analysis and Slip Planes

Atomic strain tensor analysis shows that a significant amount of cross slip occurs in the sample under compression. Slip was found to occur on a series of connected \( \{110\} \) planes for each dislocation. Figure 5 shows a cross section of the pillar following a compressive strain of 14%. Atoms are coloured according to the local atomic shear strain metric defined by Shimizu et al [32].
Cross sectional slices were taken across two faces of the pillar and the viewing direction is a $\langle 100 \rangle$ direction which runs diagonally through the centre of the pillar. Atoms coloured light blue and green have high local atomic shear strains and are therefore atoms located on slip planes on which dislocation glide has occurred. The jagged profile of these slip plane atoms indicates that a significant amount of cross slip has occurred. Closer inspection of the slip plane atoms reveals that the profile for each of these slip surfaces is jagged on one side of the pillar and generally straight on the other side. This is due to the orientation of the dislocations being perfect straight screw dislocations as seen in figure 4. The straight lines formed by the dislocation lines were always parallel to one of the side faces of the pillar and therefore the slip path cross sections seen in figure 5 must always be straight on one face of the pillar cross section even when a significant amount of cross slip has occurred. Cross slip allows many dislocations to traverse a path which runs at approximately 45° to the direction of compression. The dislocations cross-slip so as to travel in this direction of maximum shear stress.

3.2. Tension

We have also carried out simulations on pillars in tension, and found that deformation occurs by twinning.

This is consistent with the mechanism whereby partial dislocations with burgers vector $\frac{1}{6}(112)$ move on successive planes creating a twin boundary on a $\{112\}$ plane[10] as reported in similar molecular dynamics simulation recently by Li et al[24]. However, in our simulations the twin formation is very rapid, and it is not possible to identify individual fractional dislocation events.

A typical image of a pillar following a tensile strain of 16% is shown in fig 6. Twin formation occurred in a single event - as shown in the massive yield event at 6% strain in 7(a). After the initial yield event, twinning deformation proceeds by motion of the twin boundary in a continuous process as shown by the plot of indenter plate pressure vs strain in figure 7(a). A large stress is required to create the twins initially, but the strain continues at an almost continuous stress level following that as the twin boundaries move. The applied stress is lower than that required for compression by a factor of 3: more than can be accounted for by changes in the cross-sectional area. With the exception of the initial stress peak in 7(a), this stress vs strain behaviour is qualitatively similar to the stress vs strain signature recorded in experiments on nanopillars of Nb reported by Kim et al[5] which can be seen.
in figure 7(b). The initial stress peak observed in our simulations is probably due to the high strain rates which we are limited to in molecular dynamics simulations.

The sequence of images in figure 8 shows the creation of pairs of twin boundaries during the tensile strain simulation. When the pillar first begins to deform plastically, three pairs of twin boundaries are created. As the separation between the twins in the middle of the pillar grows, the other two pairs of twins shrink in size to allow the central twins to move.

It should be noted that this twinning process results in the creation of \{100\} surfaces on the pillar in the plastically deformed region in the centre. These surfaces are unstable and our nanosample will recrystallize if held at this strain and allowed to relax. Alternately, if the stress is removed the sample will untwin in order to reduce the surface energy. In a sense, this nanopillar exhibits superplasticity. To study the deformation, we worked at shear rates where these diffusive reconstructions did not occur. This is consistent with previous MD calculations. Suppressing these reconstruction events is justifiable because the driving force for them is the dominant effect of surface energy, something which is only the case at the nanoscale, and not in pillars of the size considered in experiment.

3.3. FCC materials

We have tested the plasticity behaviour for fcc Cu nanopillars and have found little differences between plasticity behaviour in compression and tension. Deformation in these pillars occurred through partial dislocation glide on \{111\} planes, without any cross slip occurring, for both tension and compression. The yield stress in tension for these pillars was about half that in compression. This is consistent with previous reports of MD simulations of plasticity in copper [33, 34].

4. Discussion

Under compression, our Fe pillars deform by glide of \(\frac{1}{2}\langle 111 \rangle\) dislocations on slip planes. Under tension a twinning mechanism operates. This is consistent with much experimental evidence including that of Kim and Greer [3, 4, 5, 6] which showed bursts of dislocation motion punctuated by periods of rising stress.

There are some differences in the behaviour between our MD simulations and experimental results, due to differences in boundary conditions. Exper-
imental results for compression of bcc nanopillars often reveal strain bursts in the stress vs strain behaviour. In contrast we see a series of sudden stress drops. This apparent difference is because we apply fixed strain, which means that events involving large spontaneous strain are impossible. There may be some difference due to the small size of our pillars, the high strain rates which we have to work with in MD: in particular the surface-driven recrystallization may well be a size effect. The experimental boundary conditions are difficult to characterize: although nominally under stress control, they actually show large sudden changes both in stress and strain.

In the tensile case, the twinning we observe is a possible mechanism by which the necking seen in Kim and Greer’s experiments could occur. The long periods of constant flow stress observed in these experiments agrees well with that seen in simulations as seen in figure 7. The biggest difference between simulations and experiment in this case is the large initial stress required to nucleate the twin in our simulations. This is because unlike the experiments we have an atomically-flat surface, on a dislocation free sample. Such high yield stresses are observed in experiments with dislocation-free single-crystal whiskers.

A possible explanation for the observed asymmetry comes from the fact that dislocation cores in bcc are spread in three dimensions. The more compact the core, the easier it is for the dislocation to move. Hence, under compression, the core will be compacted, favouring the dislocation mechanism, while under tension the core can spread even further, making dislocation motion more difficult[11, 13, 14].

The twinning-antitwinning asymmetry is not present in fcc crystals as formation of twins is not mediated by fractional dislocations as in bcc materials. The change in the core structure under stress in bcc materials is dependent on the presence of edge components in fractional dislocations[11]. Due to the lack of fractional dislocations in fcc materials, this effect is not observed in fcc materials.

5. Conclusion

In bcc nanopillars, the deformation mechanism is completely different in compression and tension. This asymmetry is not present in fcc nanopillars.

In the compressive case, plastic deformation is mediated by dislocations. Plastic deformation occurs in discrete bursts when one or more dislocations are created at the pillar surfaces and move through the pillar by glide. A
large amount of cross slip is observed in this deformation regime allowing for the dislocations to move in the direction of maximum shear stress. By contrast, in the tensile case deformation occurs through the creation and motion of twin boundaries. This is consistent with asymmetry observed in various experiments.

References


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Figure 2: (a) Plot of pressure on indenter plates vs strain for pillar in compression. The pressure on the indenter plates does not start at zero due to surface tension. (b) Graph of Stress vs Strain for Nb micropillar compression experiments under stress control performed by Kim et al[5].
Figure 3: (a) Indenter plate pressure vs strain for 60 different simulation runs superimposed on a single graph. (b) Average pressure on indenter plates vs strain over 60 pillar compression simulations.
Figure 4: View from the top of the pillar as a dislocation runs through the pillar in a compression simulation. Only atoms with high centrosymmetry parameter (typically free surface and dislocation line) are shown. Frames (a)-(d) show a $\frac{1}{2}(111)$ dislocation emerge from the top left corner of the pillar. The dislocation initially has mixed character. However by frame (d) the dislocation forms a straight line with pure screw character. Frames (e)-(h) show this dislocation move through the pillar until it meets one of the sides. A second dislocation can be seen emerging from another corner from frame (f) onwards. Although our simulations have a higher strain rate than the experiment, this sequence shows that the deformation on compression is still primarily due to independent single-dislocation events.
Figure 5: Cross section of the pillar following a strain of 14%. Atoms are coloured according to atomic shear strain. The light blue and green atoms have high atomic shear strains while the dark blue atoms have low atomic shear strains.

Figure 6: Image of pillar following a tensile strain of 16%.
Figure 7: (a) Pressure on indenter plates vs strain for pillar tension. (b) Graph of Stress vs. Strain for micropillar tension experiments on Nb performed by Kim et al[5].
Figure 8: Side view cross section of the pillar during tension. Only atoms with high centrosymmetry parameter are shown. Frames (a)-(f) show the creation of three twins in the initial yielding event following 7% tensile strain. As deformation proceeds, two of these twins disappear until only the single, central, twin remains. This can be seen in frame (g) which shows the pillar following 11% tensile strain.