Humanoid Balancing Behavior Featured by Underactuated Foot Motion

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Abstract—A novel control synthesis is proposed for humanoids to demonstrate unique foot tilting behaviors comparable to humans in balance recovery. Our study of model based behaviors explains the underlying mechanism and the significance of foot tilting well. Our main algorithms are composed of impedance control at the center of mass, virtual stoppers that prevents over-tilting of the feet, and postural control for the torso. The proof of concept focuses on the sagittal scenario and the proposed control is effective to produce human-like balancing behaviors characterized by active foot tilting. The successful replication of this behavior on a real humanoid proves the feasibility of deliberately controlled underactuation. The experimental validation was rigorously performed, and the data from the sub-modules and the entire control were presented and analyzed.

Index Terms—Balance Control, Humanoid Robot, Underactuation, Foot Rotation.

I. INTRODUCTION

The biomechanical study of human locomotion reveals the phenomenon of underactuation during standing balance and walking [1], and it is also a common observation that people tilt feet and roll around toes under moderate forward pushes, as the laboratory experiments show from Fig. 1(a) in comparison to the flat footed robotic behavior. From the perspective of mechanics, the tilting of the support foot can provide a better foot-ground clearance so that the maximum ankle torques can be sustained. The original purpose of anthropomorphic robots is to utilize human-orientated tools and to traverse complex terrains where only humans can go, not wheeled machines. Though some humanoids might actually have morphology and strength very similar to the human companions, they have not yet demonstrated many comparable balancing skills.

From the perspective of rigid body dynamics, if humanoids have similar physical capabilities, e.g., joint range and motor torque/power, there is no particular reason why these man-made machines could not perform standing balance with underactuation phases comparable to humans. Main practical reasons preventing robots from doing so lie in the control techniques and the actuation technology.

On the one hand, the common balance and dynamic walking control requires the zero moment point (ZMP) (conventionally referred in gait planning stage) or center of pressure (COP) (conventionally referred in terms of measurement) to be inside the support polygon. In this paper, we do not differentiate ZMP and COP because they are identical on a real system [2], [3] and are essentially the same point where a single resultant ground reaction force (GRF) applies. If the foot tilts, the control challenge arises since the edge of the foot becomes the pivot, which is an underactuated degree of freedom (DOF) with zero torque around this axis. Therefore, the physical range of COP vanishes into a singular point. From control’s point of view, we lose direct control authority over this new DOF.

The traditional ZMP control method would fail while undergoing the underactuation, because it is developed on the assumption of a fully actuated system where the foot of the robot is firmly placed on the ground, as if it is a classical manipulator bolted on a base. Therefore, all the controls are greatly simplified and the canonical solutions of kinematics and dynamics that are well developed for industrial manipulators can then be applied. To suffice the prerequisite of an attached base, the net GRF needs to act inside the polygon of support, not the edge, so that the net moment is always zero and the foot wouldn’t tip. With these assumptions satisfied, any applied forces from the robot will always be canceled out by the reaction forces from the ground, so the foot remains stationary. However, once underactuation occurs, no matter how the foot rolls or the net moment around the

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Fig. 1: The underactuation behaviors in human and humanoid push recoveries: (a) foot tilting observed from a person’s response; (b) a humanoid with our proposed control can perform human-comparable foot tilting; (c) the conventional balance control with flat-footed behavior.
axis of rotation changes, the measured COP feedback in foot is always invariant.

Therefore, despite the spatial trajectories of feet can have toe-off and heel-strike motions to imitate that of humans, in order to satisfy the preconditions of classical ZMP based control, linear models such as the Linear Inverted Pendulum Model (LIPM) [4] or the Cart-table Model [5] are typically used to generate center of mass (COM) motions, so the resulted ZMP is preferably limited inside the support polygon. Especially because the foot may start to roll due to the deformation of materials underneath the foot, large safety margins are planned as possible at every time instant [6] [7] [8].

In contrast, during heel-strike and toe-off phases in human locomotion and passive dynamic walkers [9] [10], the actual GRF acts inside a narrow support area or nearly a point in the rolling foot. Though ZMP/COP is still the point where the resultant GRF applies, the geometric distance between the ZMP/COP and the edge of the polygon of support is no longer reasonable to imply the level of balance that whether or not a person/robot is going to fall. Because of this, other physical quantities were proposed from aspects of orbital energy [11] and mechanical energy [12] [13]. Particularly, the Capture Point is a simple and straightforward measure of balance [11]. Based on that, some gait control methods developed in [8] [14] have shown the feasibility of using Capture Point to generate dynamic gaits in real bipedal systems other than the ZMP approach. Hence, in this study, we present the experimental data of Capture Point together with other measurements to show that the robot did not fall as long as the Capture Point is bounded by the convex of a reachable support region.

On the other hand, apart from the stability indicators that limit the exploration of underactuation phases, another major limitation comes from the actuation technology. So far, the majority of actuators are position controlled. Because locomotion is a physical interaction that involves contact forces between the robot and the environment, a purely position controlled system is vulnerable to any unexpected discrepancies. The highly stiff position control can cause damages during any undesired collision, whereas the low stiffness case trades off tracking accuracy in the task space. Therefore, to achieve good locomotion and balancing performance, torque control is very much favored because it permits precise position tracking during collision-free motion and, meanwhile, renders desired contact forces to remain compliant during physical interactions which in turn preserves contacts very well [15] [16].

A. Related Work and Motivation

Hofmann et al. [17] carried out simulation study on the utilization of angular momentum created by non-contact limbs for dynamic balance recovery, and Atkeson et al. [18] demonstrated multiple behaviors by using one single optimization policy for standing balance control. However, in both cases, the applied ankle torque was restricted to prevent tipping of the stance foot. Among the powered bipeds that demonstrated the toe-off and heel-strike [19], [20], [21], their underactuation phases emerged from the assistive control of passive dynamic gaits. Though the Petman prototype from Boston Dynamics has also shown human-like walking with heel-toe transitions, no publication reveals the control details.

Our previous study in [22] demonstrated that the robot could have a short portion of underactuation phase without falling. It shall be distinguished that our proposed scheme in this paper is a proactive approach that deliberately makes use of underactuation to enhance balance recovery, while the previous work in [22] merely targeted at suspending unstable oscillation during foot tilting so the underactuation occurred passively due to larger pushes. Hence, that underactuation behavior in [22] was not an actively controlled behavior.

The standing balance control can be classified into two categories by the actuation technologies. One is the position based control that typically utilizes a simplified low dimensional model, calculates the desired Cartesian references by satisfying contact force constraint such as ZMP, and obtains the position reference in joint space via inverse kinematics [23], [24]. The other is the torque based control that has the feedback loop of the targeted objectives at the Cartesian space and uses the joint torque capability to directly apply the desired wrench to deliver the control actions [25], [26], [27]. Our proposed strategy belongs to the latter category.

Given the torque controlled ankles, the control then acquires the ability to actively regulate the COP at the edge of the support feet. Therefore, the balance recovery performance can be maximized by exerting the largest ankle torque as possible. This is very different from the classical ZMP controlled bipeds, where the control not only constantly and carefully positions the ZMP inside the support polygon, but also keeps the ZMP away from the edge of the polygon with a significant safety margin [6], which reduces the magnitude of ankle torque to a great extent.

Our control philosophy is inspired by the previous studies from Mitobe et al. [28], [29] and Sugihara et al. [30], [31] that the task space is the COM state (position and velocity) with non-divergent motion in long term, and the ZMP/COP is regarded as the control effort to actuate the COM motion. Moreover, biomechanical study of human posture regulation has also revealed the same causal relation of COP-COM [32]. Therefore, by respecting a straightforward physical causality of “force results in the change of motion,” we could push the COP to the maximum to drive the COM state for achieving a stable movement. Meanwhile, the balance status is characterized by mechanical/orbital energy-based criterion [11], [13].

To the best of our knowledge, in terms of balance recovery by active foot tilting comparable to that of humans, only the Dexter robot from Anybots Inc. [33] has demonstrated similar performance of stable foot tilting while being pushed. Unfortunately, no further details have been published regarding its algorithms. Hence, we are motivated to answer how stable underactuated behaviors can be achieved in a deterministic and analytic approach.

B. Our Contribution

Most biomechanical studies were concerned about the toe-off during walking [10], [34] but limited explanation is given to humans’ foot tilting behavior during standing push recovery.
TABLE I: Parameters of Kong Robot

<table>
<thead>
<tr>
<th>Segment</th>
<th>Mass [kg]</th>
<th>Length(vertical) [m]</th>
<th>Width(lateral) [m]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Torso</td>
<td>17.67</td>
<td>0.42</td>
<td>0.44</td>
</tr>
<tr>
<td>Pelvis</td>
<td>9.3</td>
<td>0.236</td>
<td>0.206</td>
</tr>
<tr>
<td>Thigh</td>
<td>4.90</td>
<td>0.314</td>
<td>0.14</td>
</tr>
<tr>
<td>Shin</td>
<td>2.81</td>
<td>0.30</td>
<td>0.12</td>
</tr>
<tr>
<td>Foot</td>
<td>3.19</td>
<td>0.107</td>
<td>0.07</td>
</tr>
</tbody>
</table>

Due to the control limitation of dealing with underactuation as stated before, the replication of this human-like behavior is very rare in humanoids. Our analysis based on several inverted pendulum models can explain the advantage of tilting the foot. To overcome the restriction imposed by the conventional control paradigm, we re-evaluate the fundamentals of balance concept and revisit the literature of the energy-based stability criterion that indicates the possibility of balance enhancement by foot tilting. After laying this theoretical foundation, we propose an effective control framework consisting of several unsophisticated controllers to replicate this similar behavior in a humanoid robot.

As a proof of concept, the scope of the paper covers only the sagittal case where we designed the control scheme to perform standing balance with actively controlled underactuation. Hence, there is no need to artificially constrain the ZMP/COP to be within the support polygon. Rather, the COP is permitted to stay at the edge of the contact polygon and embrace underactuation. This result is encouraging because it shows the possibility toward more human-like balancing and walking with real toe-off motion for powered bipeds/humanoids. We wish this study can shed some light on the future research of agile locomotion by using the energy-based balance measure and integrating the torque control actuation to produce more efficient gaits that harvest the natural dynamics of the system.

This paper is outlined as follows. Section II elaborates the principle of the balance criterion based on the mechanical energy and then uses several inverted pendulum models to hypothesize the advantages of foot tilting. Section III explains the whole control framework with necessary sub-modules such as state estimation, ankle torque control, variable COM impedance control, virtual mechanical stoppers, body postural control, as well as the analytic COM compensation and lateral stabilization. Section IV presents our experimental validations, and analyzes the data from sub-modules and push recoveries with actively controlled foot tilting. We discuss the limitations of our method in Section V and conclude our study and suggest the future work in Section VI.

II. REVISIT BALANCE CRITERION: IMPLICATION OF FEASIBLE UNDER-ACTUATION

Most prior work studied the aspect of the force acting on a robot [13] and the resulted moment is used as a criterion for determining the balance status [12]. Given a system with zero kinetic energy, it is mostly true that solely the net moment leads to the change of the motion. However, the divergence and convergence of the future movements undoubtedly become more complicated, while the initial mechanical energy varies. Therefore, the motion state shall be considered together with the forces acting on the system, and the prior work in [12] [13] investigated the global stability of legged systems by measuring the mechanical energy. Following the energy-based balance criterion, we hereby do not need to overrestrict the feet to be always flat on the ground and, therefore, permit a rich diversity of movements.

A. Balance Criterion Based on Mechanical Energy

Under large external disturbances, a robot can tip around the edge of the foot in an inverted pendulum manner, where the COM travels in an arc instead of a line with a constant height. We hereby use general inverted pendulum models to represent different featured motions and to elaborate the energy-based balance criterion, the enhancement of disturbance rejection, and the implication of allowable underactuation.

Fig. 2(a) shows a life-size humanoid robot named KONG, and Fig. 2(b) shows a multi-mass model that considers the segmental masses for computing the estimation of full-body COM. The arms are not utilized in this study, so all masses of the upper body, arms, and head are lumped as one rigid body. Fig. 2(c) shows a planar model that includes: a point mass for the torso and arms and represents the physical body posture; a massless foot that represents the foot orientation;
and a massless inverted pendulum. More details of the robot parameters are available in Table I. The measured weight of KONG is 50.1 kg, which is slightly heavier than the sum of all weights in Table I due to the extra on-board auxiliaries.

The COM state, position and velocity, of the robot is computed by forward kinematics using the motor encoder readings and the orientation data from the inertial measurement unit (IMU) which is mounted in pelvis. Thus, the kinetic energy of the robot can be estimated. The virtual leg pointing from ankle to the COM is controlled by the ankle torque $\tau_{\text{ankle}}$ for keeping the global stability, and the body posture is independently oriented by servoing the hip joint. The internal disturbance caused by the COM displacement of torso due to the attitude controller is decoupled analytically by a three-mass model, which will be explained in Section III-E.

The vector pointing from an instantaneous pivot to the COM is the equivalent pendulum that allows the use of the inverted pendulum model (IPM) to analyze the balance behavior. If the total mechanical energy is lower than the apex of potential energy determined by the current contact configuration, then the robot could afford underactuation phases and tip around the edge of the foot for a portion of time, as long as the kinetic energy is bounded by the apex of potential energy.

As shown in Fig. 3, denote $\mathbf{r}_0$ the virtual leg, $\mathbf{d}_{f,r}$ the front/rear foot segment, and $\omega$ the angular velocity. Therefore, the virtual pendulums pointing from the frontal and rear foot to the COM are $\mathbf{r}_f = \mathbf{r}_0 - \mathbf{d}_f$ and $\mathbf{r}_r = \mathbf{r}_0 - \mathbf{d}_r$, respectively.

Let $\mathbf{r}$ be the vector of the equivalent pendulum in general, the kinetic energy $E_k$ about the pivot is approximated by

$$E_k = \frac{1}{2} \omega^T I \omega,$$

where $I = mr^2$ concerning a single mass model and $r = \|\mathbf{r}\|$. As one example illustrated in Fig. 3(a) and (c), where the pendulum of constant length is travelling from an initial angle $\theta_0$ to the potential apex where the COM position is the highest, the potential energy of the equivalent pendulum $\mathbf{r} = \mathbf{r}_f$ is

$$E_p = mgr (\cos \theta_0 - 1).$$

by referencing the apex as zero. Thereby, by examining the total mechanical energy as

$$E_m = E_k + E_p,$$

we can quantitatively determine whether or not the robot will pass over the edge of support foot and fall inevitably: $E = 0$ indicates a perfect rest above the pivot; $E < 0$ implies a return before the potential apex; and $E > 0$ means the COM will cross over the potential apex and diverges away from the pivot.

The above conclusion will have a reasonably good prediction of the global balance state of the robot when the angular momentum around the COM is negligible and the gravitational

Fig. 4: Time-lapse illustration of the foot tilting effects: (a) flat foot with constant COM height; (b) flat foot with constant leg length; (c) foot tilting around toe with fixed ankle joint (zero COM velocity at 0.104 m); (d) active foot tilting around the edge of the foot with rotation of ankle joint (zero COM velocity at 0.093 m).
torque is a dominant factor. It is worth noticing that if a particular robot is able to produce large angular momentum around the COM that changes the future evolution of the COM state, then the above conclusion becomes invalid. However, this is not yet the case or the scope of our study here.

This balance criterion based on mechanical energy implies that any control policy that can actively dissipate more kinetic energy will lead to an improvement in disturbance rejection. Most importantly, unlike the conventional control that restricts the range of COP, we can certainly allocate the COP at the foot tip for producing a maximum horizontal GRF, i.e., maximum ankle torque. An initial stage can be achieved by simply stiffening the ankle joint so that the frontal edge of the foot becomes the pivot and the velocity at the COM is re-directed, as shown in Fig. 3 (c), meaning that the kinetic energy is partially absorbed along the new pendulum direction. As a further enhancement, the equivalent pendulum can be deliberately extended to exert larger GRF against the disturbed velocity. By combining these actions, a better balance augmentation yields, compared to the LIPM based control.

To sum up, compared to the LIPM behaviors with a flat foot and a constant COM height, advantages of foot tilting are:

1) the ankle torque can be escalated to the maximum because of a controlled foot-ground clearance;
2) the resulted velocity received by the disturbance is redirected, leaving a smaller velocity component perpendicular to the new equivalent pendulum;
3) larger ankle torques can produce larger horizontal ground reaction forces.

By these controlled features, we can fully exploit the power of ankles and maximize the capability of disturbance rejection.

B. Balance Performance by Different Behaviors

To analyze the differences in balance performance, we used a general inverted pendulum dynamics for representing different controlled behaviors in response to the same disturbance, and the differential equations with respect to the pivot are:

\[ \ddot{r} = (f - mg \cos \theta + mr \dot{\theta}^2)/m, \]
\[ \dot{\theta} = (r + mgr \sin \theta - 2mrr \dot{\theta})/I, \]

(4)

where \( m \) is the mass, \( g \) is the gravitational constant, \( f \) and \( r \) are the force and torque in the pivot coordinate.

We use (4) to formulate four behaviors: (1) the COM follows a LIPM mode with a constant height; (2) a constant leg length around the ankle; (3) a fixed ankle joint with a constant length of the equivalent pendulum pointing from the COM to the toe; (4) an active extension of the equivalent pendulum by powering ankle. This study has a better cross comparison regarding the model difference in [37]. The origin of the coordinate is the initial position of the ankle. For the first two cases, (4) was applied regarding the origin as the pivot, while the latter two were simulated considering the tip of the foot as the pivot.

Fig. 4 shows the time-lapsed motion of the COM and other data from these four behaviors. The frontal foot length is 0.12 m and the initial COM position is (0, 0.748) m which are the same as our experimental setup. The initial COM velocity was calculated regarding tip of the foot as the capture point, so the COM stops right above the edge of the foot. All the numerical integration was done using trapezoidal Euler method at 1 \( \mu \)s time step. The duration of actively commanded ankle rotation was always 0.5 s for creating equivalent pendulum extension, which is very realizable for most humanoids and meanwhile avoids any assumption of instantaneous force impulse.

Fig. 4(a) and (e) show a critical case that the disturbance produces the COM velocity such that the Capture Point is exactly at the edge of the foot, and the COM is converging to the Capture Point after 1.5 s. Meanwhile, a behavior with a constant leg length is not helpful because some potential energy converts into kinetic energy while lowering the COM height. Therefore, as shown in Fig. 4(b) and (f), the Capture Point goes beyond the edge of the foot and diverges later.

In contrast, pivoting around the toe creates a larger GRF to attenuate partial kinetic energy along the equivalent pendulum. This redirects the velocity vector and results in the shift of Capture Point toward the interior of the support polygon, which allows the COM to return to the equilibrium, as shown in Fig. 4(c) and (g). The stopping distance, the horizontal distance between the COM position when \( \dot{x}_{\text{com}} = 0 \) and the frontal edge of the foot, is used as an index to quantify the balance performance. Compared to the Capture Point that changes along time, the stopping distance is a constant value specifically for each case, which is easy to be measured. As Fig. 4 (d) and (h) reveal, by intentionally controlling ankle rotation, the equivalent pendulum can exert even larger force and create an extension that produces a bigger stopping distance at an earlier time.

Assuming zero initial velocity and instantaneous shift of the COP, the rejectable impulse derived by Capture Point [11] is,

\[ J_{\text{reject}} = m \sqrt{\frac{g}{z_c}} \Delta_{\text{cop}}, \]

(5)

where \( z_c \) is the COM height, \( \Delta_{\text{cop}} \) is the relative horizontal distance between the constant COP and the initial COM position. Let \( \Delta_{\text{cop}}^+ \) be the physical maximum defined by the foot size, and \( p \) be the ratio that \( \Delta_{\text{cop}} = p \cdot \Delta_{\text{cop}}^+ \), then

\[ J_{\text{reject}} = p \cdot J_{\text{reject}}^+, \quad p \in [0, 1], \]

(6)

![Fig. 5: Stopping distance, the horizontal distance between \( x_{\text{com}} \) when \( \dot{x}_{\text{com}} = 0 \) and the frontal edge of the foot, at a wide range of foot length and deliberately actuated ankle rotation.](image-url)
where \( J_{\text{reject}}^+ = m \sqrt{\frac{g}{z}} \Delta \) is the theoretical maximum of the impulse that can be rejected.

It shall be noted that Fig. 3(a) is an ideal case: since the core assumption of the ZMP based control is to restrict the ZMP inside the support polygon with safety margins, the variation of ZMP/COP is always smaller than the foot size, where \( p < 1 \) and \( J_{\text{reject}}^{\text{ZMP}} < J_{\text{reject}}^+ \). Therefore, the traditional ZMP method would fail at the critical condition in Fig. 3(a).

For example, a safety margin of \( p = 0.5 \) would proportionally downgrade 50% of balance capability \( \text{(4)} \). It is very evident that the over-constraints of ZMP/COP can reduce the balance performance to a great extent.

In contrast to this, our comparison in Fig. 4 shows that the active foot tilting is useful at the upper limit of the LIPM based control that \( J_{\text{reject}}^{\text{ZMP}} < J_{\text{reject}}^+ \). Using the same boundary condition as in Fig. 4, the parameter scan in Fig. 5 quantifies the improvements by the stopping distance. An average case where the frontal foot is 12 cm, an ankle rotation of 15° within 0.5 s can create a stopping distance about 2 cm. Since an average ankle rate of 30°/s is quite conservative and many real robots can do better, a greater stopping distance can be possibly achieved. This implies that an inevitable falling can be successfully prevented by a variety of control strategies that follow the same underlying principle.

### III. Balance Control Framework

To prove the novel concept of balance control involving actively controlled underactuation, we need a set of control realizations in order to validate the theoretical principles in a real platform. We designed a control scheme comprised of the variable impedance control at the COM of the robot, the nonlinear mechanical stoppers to prevent feet from over-tilting, and the torso attitude control. It shall be clarified that our proposed control produces the foot tilting due to the generation of excessive ankle torque from the COM impedance control. The overall scheme with sub-systems, e.g., state feedback and controllers, is shown in Fig. 6. The lateral compliance control and leg force equalizer are purposely omitted here for keeping a neat illustration.

#### A. Estimation of the Whole Body COM

In order to recover balance, we first need to obtain good estimation of the COM state for computing the desired ankle torque. The COM position feedback was computed by the forward kinematics using the motor encoder measurements combined with the orientation of the pelvis measured by the IMU. The COM velocity was then obtained by numerical differentiation. The segmental COM of the lower body was obtained from the mechanical design, and was approximately at the center of each limb. The main variation of the real whole-body COM comes from the torso because of the change of on-board equipment. Therefore, we have calibrated the torso COM vector via least square fitting by using the COP measurement in feet as the ground truth during statically balanced movements.

Given the limited range of motion in our push recovery study, the accuracy of the COM estimation was validated to be sufficient for the COM controller. The COM state was also used to compute the Capture Point in the following experiments to indicate the level of balance stability.

#### B. Ankle Torque Control Via the Admittance Scheme

We adopted the admittance controller in [22] to acquire the torque control capability in ankles. Though KONG robot has position controlled actuators, the torque feedback provided by the 6-axis F/T sensors in feet allows the ankle joints to be torque controlled. The rubber pads underneath the feet have certain level of compliance and can be modeled as linear spring dampers, as shown in Fig. 7 which also corresponds to an equivalent torsional spring-damper around the axis of the F/T sensors. This physical compliance makes it easier to achieve torque control by deforming the compliant materials based on the regulation of positional reference.

Define \( \theta_d \) as the desired pitch orientation for the motor side, \( \tau \) as the real torque measurement, \( K_s, K_d \) as the physical and desired stiffness \( (K_s > K_d) \), and \( B_s, B_d \) as the physical and desired viscous damping. At the discrete time \( i \) with the sampling time \( T \), the admittance controller is

\[
\theta_d(i) = \frac{T}{K_d T + B_d - B} A(i) + \frac{B_d - B}{K_d T + B_d - B} \theta_d(i-1),
\]

where the term \( A \) is

\[
A(i) = K_d q_0(i) + \frac{K_d - K_s}{K_s} \tau(i) + \frac{B_d - B}{K_s} \dot{\tau}(i).
\]

The torque tracking can be realized by controlling the set-point \( q_0(i) \) in (8) as

\[
q_0(i) = \theta_d(i-1) - \frac{\tau(i)}{K_s} + \frac{\tau_d(i)}{K_d}.
\]

Substitute (9) into (8) then (7), yields

\[
\theta_d(i) = \theta_d(i-1) + \frac{\tau_d(i) - \tau(i)}{K_d + \frac{B_d - B_s}{K_s}} + \frac{B_d - B_s}{K_s} \frac{\tau_d(i)}{K_d + \frac{B_d - B_s}{K_s}} \dot{\tau}(i).
\]

Equation (10) implies that the feedback loop compares the torque error between the reference \( \tau_d \) and the measurement \( \tau \), and incrementally modulates the position reference of the actuator to thrust the desired torque.

In this study, we have equipped new rubber pads under the feet with the equivalent physical stiffness \( K_s \) of about 2363.3 Nm/rad, which was stiffer than the old rubbers used in the previous study [38]. The desired viscous coefficient \( B_d \) was tuned proportionally to \( \sqrt{K_d} \) with a minimum damping ratio to guarantee the necessary passivity for avoiding unstable oscillations. \( \theta_d \) was used to update the orientation of both feet in the calculation of inverse kinematics.

#### C. Variable COM Impedance Control

Using the COM state feedback as described in Section III-A, an impedance control can be designed to compute the reference for the torque tracking loop as in Section III-B. A number of experiments qualitatively ruled out that a good impedance regulation is to be compliant when the Capture
Fig. 8: Variable impedance gain regulation.

Point margin is large and vice versa. This inspires the use of variable gains [39] depending on the stability indication. Ideally, Capture Point shall be used for changing the gains. In practice, due to limited sensor resolution, the ripples in the velocity component of the Capture Point produces an undesired oscillation by the viscous damping torque computed from the COM velocity feedback. On the other hand, the latency introduced by low-pass filtering the velocity is not desirable neither. Therefore, as a compromise, we only used the COM position for the variable gain regulation. Fig. 8 shows the variable torsional impedance at the ankle joint which is converted from the Cartesian impedance at the COM. The gains are dependent on the horizontal projection of the COM position with respect to the support polygon.

Define \( \tau_{\text{ankle}} \) as the ankle torque applied to the equivalent pendulum pointing from the local coordinate to the COM, then, the reaction torque applied on the foot has an opposite sign as in Fig. 9. The ankle torque is

\[
\tau_{\text{ankle}} = \begin{cases} 
  k_p^c (x_{\text{COM}}^d - x_{\text{COM}}) - k_d^c f_{\text{COM}}, & \text{if } \tau_{\text{ankle}} > \tau_{\text{max}}, \\
  \tau_{\text{max}}, & \text{if } \tau_{\text{ankle}} > \tau_{\text{max}}, \\
  \tau_{\text{min}}, & \text{if } \tau_{\text{ankle}} < \tau_{\text{min}}.
\end{cases}
\]  

(11)

In order to deliberately produce a large torque at the ankle that allows the feet to tilt, \( \tau_{\text{ankle}} \), which is the sum of the torques commanded from the impedance loop and the gravity compensation, has the saturation limits higher than the torque created by the total weight of the robot with respect to the edge of the feet. Hence, we have \( \tau_{\text{max}} > mg \| d_f \| \) and \( \tau_{\text{min}} < -mg \| d_f \| \). The detailed formulation of \( \tau_{\text{max}} \) and \( \tau_{\text{min}} \) will be further explained by (10) in the following section.

D. Virtual Mechanical Stopper: Nonlinear Spring-Damper

If no additional constraint is imposed, simply setting \( \tau_{\text{max}} \) and \( \tau_{\text{min}} \) larger than the counteracting gravity torque might cause the foot to over tilt, especially when a very large ankle torque is commanded. For torque controlled robots, it is common to have unstable oscillations observed as a “chattering” problem in a real system during the transition between contact phases, e.g. between fully actuation and underactuation phases.

For example, when the foot resides on one edge, the physically achievable torque is unilateral, and commanding a torque reference at this moment with the opposite sign to the current applied torque is very dangerous because the foot will rotate rapidly into an aerial phase and later collide with the ground on the other edge. This causes a large collision...
that damages the hardware and a large torque error that in turn produces a large feedback control action which leads to the next collision. Consequently, we would observe a vibration of the foot when the underactuation time is significant. This is exactly the good reason that the control strategies in literature always applied a distance margin to keep the COP away from the edge of the foot, in other words, to set the torque limits very much below the real physical limit.

We have investigated a variety of different strategies to suppress the aforementioned unstable oscillations and to prevent over-tilting. The most neat, simple, and effective method we have found was the virtual model approach [40]. We virtually place the nonlinear spring-dampers at the feet as the ‘mechanical stoppers’ to generate unilateral torque based on the pitch angle measured from feet with respect to the ground, as shown in Fig. [9]. Once the foot tilts, the computed virtual torque is used to deduct the sum of the torques from the impedance control and gravity compensation (Fig. 6). Accordingly, it results in an equivalence of reduced net torque as if the physical mechanical stoppers were really there.

The nonlinear spring-dampers have the following formulation to ensure that a large portion of desired ankle torque can be diminished when the over-tilting of foot occurs:

\[
\theta_p = \theta_f / \theta_{th},
\]

\[
\tau_{vd} = \begin{cases} 
-\|\theta\| k_p \dot{\theta}_p, & \text{when } \theta_p > 0 & \text{and } \dot{\theta}_p > 0, \\
0, & \text{otherwise}.
\end{cases}
\]

where \(\theta_p\) is the pitch angle of the foot normalized by the threshold \(\theta_{th}\), so if \(\theta_f\) goes beyond \(\theta_{th}\), i.e. \(\theta_p > 1\), the virtual torque from the spring component \(\tau_{vd}\) increases significantly. Also, after normalization, \(\theta_p\) becomes unit-less, so the corresponding gains of virtual stiffness \(k_p\) and viscous damping \(k_d\) have the units of Nm and Nm-s respectively. The total virtual torque is the superposition of \(\tau_{vd}\) and \(\tau_{an} \). In our study, the configurations were \(k_p = 10.0\) Nm and \(k_d = 0.1\) Nm-s. Particularly, the non-linear damping coefficient \(\|\theta\| k_d\) is in proportional to the magnitude of foot tilting angle which is very useful to generate sufficient damping for avoiding unstable oscillations. Hence, the resultant virtual torque is

\[
\tau_{virtual} = \tau_{vd} + \tau_{an}.
\]

The angular threshold \(\theta_{th}\) is of particular importance, where the generated virtual torque from the virtual spring is targeted to decrease the commanded torque down to the ideal torque limits exactly determined by the weight of the robot as \(mg\|d_r\|\) and \(-mg\|d_f\|\) respectively. Hereby, the torque limits for impedance loop and gravity compensation were configured such that this cancellation can be made when the feet have reasonable clearance off the ground, where

\[
\begin{align*}
\tau_{max} &= mg\|d_r\| + k_p, \\
\tau_{min} &= -mg\|d_f\| - k_p.
\end{align*}
\]

The torque limits shown in Fig. [8] are computed from (16). In our study, we have \(\theta_{th} = 10^\circ\). If the foot starts to tilt beyond \(\theta_{th}\), then the nonlinear ‘mechanical stopper’ will drastically produce a large torque to decrease the desired torque command. Hence, the proposed virtual stopper method can effectively suppress the over-tilting of the foot without trading off the maximum ankle torque by setting \(\theta_{th}\) as the margin for foot-ground clearance.

With the virtual torque \(\tau_{vd}\) and the torque limits \(\tau_{an}\), we can obtain the desired torque \(\tau_d\) as the sum of the saturated ankle torque from (11) and the virtual torque:

\[
\tau_d = \tau_{an} + \tau_{vd}.
\]

E. Torso Attitude Control and COM Compensation

The attitude of the torso is modulated by a PD controller that commands the desired angular velocity reference based on feedback of the orientation error. The reference body posture in our push recovery study was to keep the body upright. To control the body posture, we need reaction torques at hips. Since there was no torque sensors in hip joints, we realized alternatively by controlling the angular rate in the desired orientation of the body in the inverse kinematics.

The reference frame used in the inverse kinematics is a virtually stationary coordinate \(\Sigma_i\) whose origin is at the midpoint between the centers of two 6-axis FT sensors mounted in feet, as shown in Fig. [10]. Locally in \(\Sigma_i\), the z-axis is always upright as shown in Fig. [10] (a) and (b). So with respect to \(\Sigma_i\), the desired orientation of the torso \(\phi_d\) is manipulated to keep the real \(\phi_b\) tracking the reference \(\phi_{ref}\) and the desired orientation of the foot \(\theta_f\) is operated to deliver the desired ankle torque \(\tau_{an}\), as illustrated by time-lapse overlays in Fig. [10] (b).

It shall be distinguished that regarding the feedback of the real COM position vector and the orientation of torso and feet, our state estimation takes the IMU feedback into account and computes the correct positional and rotational information. The virtual coordinate \(\Sigma_v\) is used here merely as an easy interface with the inverse kinematics.

![Fig. 10: Analytic COM compensation for torso motion using a three-mass model: (a) definition of local coordinate \(\Sigma_L\) used in inverse kinematics; (b) \(\Delta r\) compensation from \(\Sigma_L\) in the local coordinate \(\Sigma_L\); (c) observation from the state estimation integrated with IMU data in base coordinate \(\Sigma_B\) whose orientation aligns with the world coordinate.](image)
The velocity controller for the torso attitude regulation is
\[
\begin{aligned}
\omega_d(i) &= k_p^b (\phi_{ref}(i) - \phi_b(i)) - k_d^b \dot{\phi}_b(i), \\
\phi_d(i) &= \phi_d(i-1) + \omega_d(i)T,
\end{aligned}
\] (18)
where \(\phi_b\) and \(\dot{\phi}_b\) are the directly measured angle and rate of the body pitch from IMU, \(k_p^b\) and \(k_d^b\) are the gains, where \(k_p^b=7.8\) and \(k_d^b=1.25\) in the following experiments. The updated body orientation \(\phi_d\) is obtained by numerically integrating the desired angular rate \(\omega_d\).

To integrate seamlessly two controllers of the COM and the torso attitude, we need to compensate for the COM displacement caused by the torso orientation control, and eliminate undesired coupling effects that downgrade the performance. Inspired by the three-mass model in [41], we resolve the mass compensation analytically where the mass of the leg is equally divided and lumped at the hip and the ankle respectively. The first mass \(m_b\) is the mass of upper body (torso, pelvis, two arms and the head); the second \(m_l\) is the mass of one leg located at the hip; and the third mass \(m_f\) at the foot is the sum of the mass of one leg and two feet.

During the standing balance, the feet do not produce a very large range of motion, thus the variation of the \(m_f\) vector in \(\Sigma_b\) does not affect much the overall COM of the robot thus its effect can be omitted. We focus on the compensation caused by the major mass \(m_b\). Define the COM vector of \(m_b\) as \(\vec{r}_b = [x_b, y_b, z_b]^T\), the objective is to compute the hip compensation \(\Delta \vec{r}\) for the change of the COM caused by the rotation of \(\vec{r}_b\), as depicted in Fig. 10(b). The positional compensation \(\Delta \vec{r}\) can be computed analytically as
\[
\Delta \vec{r} = \frac{m_p}{m_b + m_l} (R_0 - R_d) \vec{r}_b,
\] (19)
where \(R_0\) is initial rotational matrix of the torso and \(R_d\) is calculated by \(\phi_d\) from (18). \(\Delta \vec{r}\) is superimposed to the initial hip position in \(\Sigma_b\) as presented in Fig. 9 and delineated in Fig. 10. In such a way, the total COM remains the same, and the rotation of the torso does not disturb the effective pendulum pointing from the base frame \(\Sigma_b\) to the whole-body COM. Hence, we guarantee the use of two decoupled controllers for controlling the COM and the torso orientation independently.

### F. Lateral Compliance Control and Leg Force Equalizer

Despite the attempt to apply external force sagittally, the real robot has dynamical effects in a 3-D space; thus there exists coupled disturbances laterally as well. This cross effect can cause some lateral oscillations, particularly the perturbation on the vertical leg forces. Because ankle torques need to be equally distributed on two feet to use the same torque thresholds \(\tau_{max}\) and \(\tau_{min}\), equal vertical leg forces are required. Otherwise, a foot with a smaller leg force will over tilt whereas the other with a larger leg force will remain stationary. In this case, it successively creates more unbalanced motion on the lateral plane.

To resolve this issue, we adapted a variant of the compliance control for a stiff system from [22] in a translational form for stabilizing the lateral motion and damping out undesired disturbances. We also used an additional integral control to equalize the left/right leg forces. Define \(y_{cop}^r(i)\) and \(y_{cop}^l(i)\) as the desired and measured lateral COP, the compliance control is regulated by modifying undesired coupling effects that downgrade the performance.

\[
\Delta y_c(i) = \frac{T}{K_d^y + B_d} [y_{cop}^r(i) - y_{cop}^l(i)] + \frac{B_d^y}{K_d^y + B_d} \Delta y_c(i-1),
\] (20)
where \(K_d^y\) and \(B_d^y\) are the desired stiffness and viscous coefficient to realize a compliant behavior. The leg forces are equalized by the integral control of the filtered force error
\[
\Delta y_f(i) = k_f^y [\vec{f}_x^r(i) - \vec{f}_x^l(i)]T + \Delta y_c(i-1),
\] (21)
where \([\cdot]\) denotes the low-pass filtered signals. In our experiments, we had \(k_f^y = 0.0002\) that was sufficient to remove the steady state error of vertical leg forces.

The resulted lateral positional modification \(\Delta y_d\) is therefore composed by two terms as
\[
\Delta y_d(i) = \Delta y_c(i) + \Delta y_f(i),
\] (22)
where the compliant component \(\Delta y_c\) deals with the external force perturbation and has a relatively high control bandwidth; the integral component \(\Delta y_f\) moves the COM closer to the leg with less vertical force, where this counterbalancing action is of a relatively low control bandwidth. For the reason of clarity and readability, the lateral compliance control and the leg force equalizer are not displayed in Fig. 6.

### IV. Experimental Validation

This section presents the validations that benchmark the performance of each sub-system, followed by the demonstrations of the whole control framework such that the method can be best replicated by other robotics researchers.

#### A. Validation of State Estimation and Sub-modules

Before using the COM feedback for the balance control, we validated the accuracy of the COM estimation compared against the COP measurement during a very slow and statically balanced motion, as shown in Fig. 11. The COM position was first moved from the initial position to \(-0.05\) m, followed by two cycles of periodic movements between \(-0.05\) m and \(0.05\) m with a period of 120 s. The blue line is the COP used as
The stiffness and viscous coefficient are contributed by the torsional spring and damping respectively.

\[ \tau_{\text{ankle}} = -K_s \theta_f - B_d \dot{\theta}_f, \]  

where \( \theta_f \) is the orientation of the foot with respect to the world frame, which is computed by the forward kinematics combined with IMU measurement. Fig. 12 shows the ankle torque contributed by the torsional spring and damping respectively. The stiffness and viscous coefficient are 2363.3 Nm/rad and 10.5 Nm/s/rad, respectively.

The torque control using (10) was validated by tracking references at 1.0 Hz and 2.0 Hz respectively, as shown in Fig. 13. The controlled parameters of the admittance control were \( K_d = 1000 \text{ Nm/rad} \) and \( B_d = 60 \text{ Nm/s/rad} \). The torque tracking was reasonable for such a hardware system and sufficient for this particular standing balance task.

Subsequently, we performed the gravity compensation by controlling the ankle torque to counteract the gravitational torque estimated from the COM position, as shown in Fig. 14. In order to prevent drifting due to small errors in torque tracking and COM estimation, we applied very small gains for the Cartesian PD control at the COM. From 0 s to 25 s, the robot stood still; from 25 s to 35 s, the robot was moved to lean forward by laboratory personnel; from 35 s to 45 s, the robot was leaned backward with positive ankle torque to counteract gravity; and after 45 s, the robot was again inclined forward, and then returned to its nominal posture.

In Fig. 14, the upper plot shows the torque references for gravity compensation and the Cartesian PD control; the bottom plot shows the total torque reference (blue) and the real measurement of ankle torque (green). The robot was actively moved back and forth by the external force, therefore, the torque measurement was leading the torque reference.

Fig. 15 shows the validation of the torso attitude control and the COM compensation scheme proposed in Section III-E. The angular reference of the torso was commanded to pitch back and forth for two cycles. As shown by the upper plot in Fig. 15 without the feedforward COM compensation, the COM of the robot (red) was moving as the torso orientation was changing. However, with the compensation scheme, the overall COM position was decoupled from the torso attitude control and was almost constant despite torso’s inclination was changing, as shown by the blue line in the upper plot in Fig. 15. The body pitch was commanded to move between \(-6^\circ\) to \(12^\circ\) with a period of 120.0 s. As shown by the bottom plot in Fig. 15, the torso attitude control shows good tracking in both cases.
Fig. 16 displays the comparison during a more dynamic motion for validating the COM compensation as well as the torso attitude control, and the measurements are plotted in Fig. 17. The reference body pitch was commanded to move fast between $-6^\circ$ and $12^\circ$ with a period of $2.0 \text{ s}$. From 0 to $7 \text{ s}$ in Fig. 17(a) the torso moved slowly to the initial angle of $-6^\circ$, then started the periodic motion since $7 \text{ s}$. Without the modification of the hip position for the COM compensation, the COM had an overshoot, while the torso was moving forward and then lost balance while the torso was moving backward. After $9 \text{ s}$, the robot had to be secured by laboratory personnel and the falling motion was interrupted for safety, as shown by the last snapshot in Fig. 16(a).

In contrast, the compensation scheme in (19) canceled the COM coupling, and the modification of the hip position and the torso orientation were out of phase as shown in the bottom plot of Fig. 17(b). In the top plot of Fig. 17(b) the desired COM position was set at $0.01 \text{ m}$, the COP had the variation within $-0.04$ and $0.05 \text{ m}$, and the COM was bounded within $-0.01$ and $0.03 \text{ m}$. So the deviation of the COM position was no more than $0.02 \text{ m}$ away from the desired position.

Fig. 18 shows the measurement of vertical ground reaction forces with the lateral compliance control and leg force equalizer from Section III-F. From 0 to $5 \text{ s}$, the robot was loaded on the ground; from $5$ to $10 \text{ s}$, the force equalizer balanced the vertical forces at two feet; from $15$ to $20 \text{ s}$, an external force disturbance was applied on the sagittal plane and created a disturbance also on the lateral plane and fluctuations on the vertical ground reaction forces. The test stopped after $20 \text{ s}$; then the compliance control quickly stabilized the oscillations and the leg force control equalized vertical forces.

B. Balance Recovery with Under-actuation Phase

Fig. 19 shows the snapshots from the successful balance recovery experiments of forward and backward pushes. The underactuation phase can be seen by the angle of the foot with respect to the ground. From the snapshots, we can see that there is no much overshoot of the whole body position while the robot was returning back to its original posture. This is because the COM controller took the COM velocity into account and commanded the ankle torque to produce deceleration, thus it prevented big overshoots of the COM position. From the accompanied video, we can intuitively see
the action of the active ankle torque control where the ankle motor spun very rapidly during underactuation and landing phases to dissipate excessive kinetic energy.

Fig. 20 presents the data from the forward push recovery with an underactuation time more than 1 s. Here, the measurements $\theta_f$ and its rate $\dot{\theta}_f$ are the average pitch angle and angular velocity of both feet. Fig. 20(a) shows that the COP moved to the front and stayed almost constantly from 0.3 to 1.5 s for a duration of 1.2 s, which indicated the COP resided at the narrow rubber edge of the foot. This can also be confirmed with the orientation of the foot $\theta_f$ (see Fig. 20(a)), which was close to $10^\circ$ during 1 and 1.2 s. The body orientation varied no more than $3^\circ$ under the feedback control of torso attitude. The Capture Point $x_{CP}$ shifted quickly to its maximum value at 0.4 s after the forward push. It shall be noted that the maximum/minimum values of $x_{CP}$ was always bounded by that of $x_{COP}$. The fact that the Capture Point always remained inside the reachable region of contact polygon indicated that the mechanical energy of the robot was bounded below the potential apex, as discussed in Section III and therefore, the robot would never fall over despite the underactuated tipping around the edge of the feet. We also show that the COM position had a very small backward overshooting during 1.6 and 2.0 s after the foot landed back on the ground surface, and how the COP drove the evolution of the COM state.

Fig. 20(b) shows the COM velocity, angular rate of the torso, and the average angular rate of two feet. During the external push, the COM velocity at 0.3 s reached up to 0.2 m/s and the body pitch had an instant angular rate of $12^\circ$/s. While tilting forth and back, the angular velocity $\theta_f$ of the foot reached $12^\circ$/s at 0.3 s and $-32^\circ$/s at 1.55 s. After 1.5 s, the first underactuation phase ended, and the feet started to rest on...
the ground surface between 1.5 and 1.6 s. We observed that at 1.6 s the COM fell back with a high peak velocity about 
−0.3 m/s, and the feet spun back at a peak angular rate of 
−32°/s. The body was stabilized, hence the torso pitch rate 
\( \dot{\phi}_b \) (−15°/s) was less than half of that of the foot \( \dot{\theta}_f \).

From the data of angular position and rate of the feet in 
Fig. 20(a) and Fig. 20(b) we can conclude that the feet had 
restored the contact with the ground since 2.0 s. During 2.0 
to 4.0 s, the COM position and velocity, the body attitude, 
and the foot orientation were converged to the steady state. 
Our preliminary study found that some low-frequency ripples 
of about 2 Hz existed during the steady phase due to the 
coupling effect between sagittal and lateral planes in a real 
system, and the lack of any control in the lateral dynamics 
caused the oscillations in the feedback signals [38]. Compared 
to our previous work, we show here that the lateral compliance 
control and the leg force equalizer successfully eliminated 
these undesired ripples.

Fig. 21 and Fig. 22 present data from the backward push. 
Fig. 21 shows the measurement of external force with a 
duration of 0.45 s and a magnitude of 70 N, the impulse was 
calculated as −16.1 N-s. This impulse would cause a velocity 
disturbance about 0.3 m/s, if no ground reaction force resists 
the disturbance. However, as shown in Fig. 22(a) during the 
first 0.45 s, the COM impedance controller generated the 
ankle torque, and thus, the COP moved backward to partially 
counterbalance the disturbance. The feet tilted backward fur-
thermore with the maximum angle of −9° at 1.2 s. The peak 
velocity resulted from the disturbance was eventually about
–0.2 m/s, as shown in Fig. 22(b).

The major underactuation phase lasted from 0.4 to 1.6 s (a duration of 1.2 s). After 1.6 s, the feet landed back to the ground, and the peak COM velocity and $\dot{\theta}_1$ occurred at 1.7 s. In turn, the COM controller computed a large control torque given the COM position and velocity errors, and the robot underwent one more underactuation motion from 1.7 to 2.2 s, as indicated by both $x_{COP}$ and $\dot{\theta}_1$ in Fig. 22(a). This allowed the ankle to retain a maximum torque for attenuating the excessive energy. From Fig. 22(a) and Fig. 22(b), the readings of $\theta$ and $\dot{\theta}_1$ since 2.5 s implied that the feet mostly conformed with the ground, and the COM position/velocity and the Capture Point were converging to the equilibrium.

V. DISCUSSION

Our study in this paper is concerned about how the balance performance can be achieved until its best by stably controlled underactuation in a human comparable manner. The maximum ankle torque is fully exploited for balance recovery before transitioning to other strategies, so the robot does not have to switch between different control modes unnecessarily if the current one is still able to handle.

However, if the perturbation keeps increasing, due to the physical limit, all ankle based balance strategies will eventually fail and other control policies shall be adopted. Without changing the support polygon, angular momentum control can be used such as swinging arms and lounging body [17]. If the disturbance is beyond the limit of the above strategies, then the robot has to change physical contacts to gain more contact forces from the environment, including taking new steps [27] or using hands and other body contacts.

VI. CONCLUSION AND FUTURE WORK

We are motivated to demonstrate the feasibility and realizability to actively create underactuation phases for human-like balance recovery using ankle torque control. During our experiments, the COP physically acts at the narrow edge of the support feet. Because the COP becomes almost a singular point, the conventional ZMP criterion of using the geometric distance between the COP and the boundary of the support polygon no longer implies the balance status. Instead, the energy-based stability criterion, such as the Capture Point, is still able to measure the balance level of the robot in agreement with all our real experimental investigations [38].

To provide a good overview of the control framework and ensure the repeatability for other researchers, we present the state estimation, the sub-controllers, as well as the integrated control scheme. We further consolidate the comprehension by presenting the data from the validations of the sub-systems. Accordingly, the experimental of balance recovery from forward and backward pushes are presented and analyzed.

Since the goal of our study is to prove the viability, we validated our hypothesis only in the sagittal scenario. Compared to the previous study [38], we have improved the COM control using a three-mass model to analytically resolve the hip position compensation for canceling the torso mass variation during large motions. To cope with the undesired lateral disturbance due to dynamical coupling, as found in [38], we have implemented compliance control and leg force control that significantly improve the performance during steady state. For future work, we are interested in exploring multi-contact control by using hands for humanoid balance augmentation on the basis of this presented approach, particularly for the scenarios in which the proposed method reaches the maximum performance and there are only hand contacts available from the environment. After realizing this human comparable level of balancing skills, a further plan will be followed to extend the same principles to realize more versatile whole-body locomotion in complex environments.

REFERENCES

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