Dynamical behaviour and stability analysis of hydromechanical gates

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Dynamical Behaviour and Stability Analysis of Hydromechanical Gates

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ABSTRACT

This study revisits the stability of hydromechanical gates for upstream water surface regulation, also known as AMIL gates. AMIL gates are used in irrigation canals, where they are often installed in series. From the regulation perspective, instabilities are undesired, as they generate waves and fluctuations in the discharge. We describe a mathematical model for an AMIL gate as a nonlinear dynamical system, which permits to analyse the dynamic interaction between the local water level and the gate position. The feedback effect of the gate on the water level is introduced by considering a storage volume of length $l$. In the derived model, waves are simplified to fluctuations of the flat water surface of the storage volume. Although previous studies used the same model, none has clarified the sensitivity of the model to the parameter $l$. The role of this parameter is investigated and it is calibrated with experimental measurements. The precision of the regulation is described by the decrement, the range of the water level around the target level. Based on the mathematical model, a relationship for calibration of the gate and precision of regulation is presented. The subsequent stability analysis of the dynamical system focuses on five control parameters and sheds light on their influence on the gate behaviour. Hopf bifurcations are identified, which separate stable equilibrium solutions from stable periodic solutions. Further work might consider the implications of the periodic solutions on gates that work in series, as well as envision the innovative use of such gates outside of the domain of irrigation canals to obtain dynamic environmental flows in hydropower systems.

INTRODUCTION

Hydromechanical gates for upstream water surface regulation, also known as AMIL gates, are used in gravity irrigation systems to control water levels upstream of their location for varying flow rates in the main canal. This flow rate may vary if the inflow upstream changes or as water is removed via lateral off-takes from the main canal according to a varying demand. AMIL gates are a specific type of radial gates, used as automatic control structures in order to cope with these variations in flow rate by opening or closing in response to the current water level. Their objective is to maintain the...
water level in a certain range around their trunnion axis. This range is referred to as decrement (Ramirez-Luna 1997; GEC Alsthom 1992) and can be related to the gate properties (calibration of mass and centre of gravity).

A photo and an illustration of an AMIL gate are shown in figures 1 and 2. In addition to typical radial gates, they are equipped with a toroidal float attached to the upstream side of the gate leaf, counterweights on the downstream side, and a damping device to reduce oscillations. As the gate is operated only by the water force, AMIL gates are counted among the hydromechanical gates (Cassan et al. 2011).

Through the interaction of the gate and the local water level, oscillations are possible and are indeed observed, particularly when the damping element (see ahead) is worn out (Ramirez-Luna 1997; Montañés 2005) (and Bernhard, 2015, unpublished; available by contacting the authors). Fig. 1 and two videos in the supplementary material show an aged experimental AMIL gate at École Polytechnique Fédérale de Lausanne in Switzerland (EPFL) that exhibits an oscillating behaviour. This behaviour was triggered by operation of the lateral off-take structures in the foreground of the photo. We can see a wave propagating in the upstream direction. Waves, and thus oscillating behaviour in general, are undesired as they are likely to affect the discharges in the main canal and the lateral off-takes.

A number of other authors have investigated instabilities related to gate operation in irrigation canals in general or more specifically instabilities of AMIL gates.

Litrico et al. (2007) developed a general method for stability analysis of automatic gates in open-channels. The Saint-Venant equations (1D shallow water equations) for the open-channel dynamics were combined with a model of the automatic gate in order to derive the governing equations. The method was based on linearisation and Laplace transform of these governing equations. To simplify, only a static relationship between the gate opening and the water level was assumed, i.e. the gate is in equilibrium with the water level at each instant. This was based on the assumption that gate dynamics are negligible in front of the pools dynamics. Litrico and Fromion (2009) used a similar approach also throughout (Litrico and Fromion 2009).

Stability of AMIL gates was specifically investigated in (Corriga et al. 1977; Corriga et al. 1980; Ramirez-Luna 1997). Corriga et al. (1977) investigated an AMIL gate connected to a short, level pool and considered a dynamic interaction between the gate position and the water level. A calibration of the gate, that results in zero total decrement, was implicitly assumed. The model was linearised and the step responses of the linear and the nonlinear systems were compared. By means of the Laplace transform, a transfer function of the linear system was derived. Instabilities were discovered and their existence was related to the value of the damping parameter. However, no study on the influence of the choice of the level pool length was done. This seems to be an important problem to address, given that the level pool is a simplifying assumption based on a model-related – not problem related – parameter.

Corriga et al. (1980) considered two long canals connected by an AMIL gate. The Saint-Venant equations were used for the canals and the gate was modelled with an adaptation of the model developed in (Corriga et al. 1977). The adaptation included the assumption of a static gate. The system was identified to be unconditionally stable for
subcritical flows.

Ramirez-Luna (1997) applied the approach that was later described in (Litrico et al. 2007) to three different hydromechanical gate types including AMIL gates. The findings for AMIL gates were also reported in (Ramirez-Luna et al. 1998). The angular moment exerted by the water on the gate was based on (Corriga et al. 1977), but it was refined by taking into account the decrement. Canal hydrodynamics were then modelled using the Saint-Venant equations. When connected to a canal, the gates were also assumed to be in a static equilibrium, based on the different time scales of the gates and canals considered in the study. Coupling of a single canal to an AMIL gate was determined to be unconditionally stable, while coupling of multiple canal reaches with AMIL gates were identified to be possibly unstable. For the latter case, a stability criterion was developed. These instabilities, however, were not attributed to the coupling of a canal reach to an AMIL gate, but rather to the interaction between canal reaches through waves.

Above overview shows that in most of the previous studies (apart from (Corriga et al. 1977)) the gate was assumed to be in static equilibrium with the current water level. The time scale of the gate dynamics were assumed to be much shorter than the dynamics of canal reaches in typical irrigation networks. The gate dynamics were thus neglected and the gate’s purpose consisted only in determining the boundary conditions for the water level and the discharge based on the static equilibrium law (illustrated further on by Fig. 4).

However, observed wave formation through gate oscillation suggest that, on a local spatial scale of the order of the generated surface perturbations, the dynamics of a gate and a canal can be of similar time scales. (Wave formation was observed for example at an experimental gate at EPFL and is shown in Fig. [1] and by two videos provided as supplementary material.) A dynamic gate-water level relation seems required in order to characterise the dynamics of the instability and to envision the use of such gates outside of irrigation canals, e.g. to generate non-proportional releases at water intakes (Razurel et al. 2015; Gorla and Perona 2013). We adopt an approach similar to the one in (Corriga et al. 1977), but differing in some basic aspects. We use a model that allows for a decrement (by considering an arbitrary position for the centre of gravity as in (Ramirez-Luna 1997)) and also distinguish between submerged and free flowing discharge of the gate. The gate response to perturbations depends on various gate parameters and can be investigated with a stability analysis. We investigate systematically the influence of the level pool length $l$ as well as the other model parameters (damping, discharge, and decrement). Lyapunov and asymptotic stability theory is used in order to determine the parameter domains in which instabilities might occur. Besides using linearised methods we attempt a characterisation of the nonlinear system.

This article can be outlined as follows. In section 2 the technical description and the dimensionless gate parameters are presented. Then, in section 3 we derive the mathematical model describing the dynamics and expose the relationship between the decrement and the calibration, that can be attained by altering the position of the centre of gravity using the counterweights. In section 4 we then assess the stability of the derived system with respect to various control parameters. In section 5 the model is calibrated to two observed dynamic behaviours of the EPFL gate.

3
TECHNICAL GATE DESCRIPTION AND DIMENSIONLESS GEOMETRY

An AMIL gate in a trapezoidal canal can be characterised by the geometrical quantities shown in Fig. 2.

Gate dimensions are described by: gate axis height $Y_a$; gate radius $R$; float radius $r$; bottom width of gate leaf $b$; top width of gate leaf $D$; width of float $b_F$.

The float is of constant width and thickness and corresponds thus to a toroid with a rectangular cross section of side lengths $b_F$ and $(r - R)$. The width of the float is assumed to be a fraction of the canal width at the bottom ($b_F/b = 0.8$).

The gate position is given by $\theta$, which is defined as the angle between the horizontal line and the lower part of the float. Other angles are: extension of gate leaf below float $\omega_F$; position of centre of gravity in polar coordinates $\omega_{CG}$ and $r_{CG}$. The position of the closed gate can be expressed using above quantities as

$$\theta_c = \arcsin\left(\frac{Y_a}{R}\right) - \omega_F. \quad (1)$$

The canal is characterised by: bottom width $b$; side slope of trapezoidal canal wall $\alpha$.

Vertical heights are defined as: upstream, controlled water level $Y_1$, which is the target of the regulation; downstream water level $Y_3$; vertical opening of gate $Y_g$ (not shown). The gate opening can be expressed as

$$Y_g = Y_a - R \sin(\theta + \omega_F). \quad (2)$$

Further quantities are needed to define the model that we develop in section 3. For the conservation of angular momentum we will refer to: angular damping coefficient $c_{\omega}$; moment of inertia of movable parts of the gate about the gate axis $I$. We also consider a volume of water in front of the gate of length $l$. In- and outflow of this volume are designated by $Q_i$ and $Q_g$. To express the gate discharge $Q_g$, a discharge coefficient $\mu$ is used, combining the effect of the contraction and velocity coefficient ($C_c$ and $C_v$). Note that we neglect the slope of the canal bottom at the gate.

Brochures by gate manufacturers indicate 21 typical gate sizes with varying geometries (e.g. see (GEC Alsthom 1992)). These 21 sizes can be grouped into four classes with distinct dimensionless characteristics. By using the top width of the gate leaf $D$ as scaling, we define dimensionless length parameters as follows

$$\hat{Y}_a = \frac{Y_a}{D}, \quad \hat{b} = \frac{b}{D}, \quad \hat{R} = \frac{R}{D}, \quad \hat{r} = \frac{r}{D}. \quad (3)$$

The dimensionless gate parameters of these typical sizes are shown in Fig. 3 and the group averages are shown in table 1. Table 1 shows additionally the values of the gate used in (Corriga et al. 1977). To facilitate comparison we base our stability investigations on the same gate. (The gate in (Corriga et al. 1977) is based on $D = 3.95m$, $I = 4500Nms^2/rad$, $c_{\omega} = 20000Nms/rad$, and $l = 1m$.)
MATHEMATICAL MODELLING

AMIL Gate as a Dynamical System

In the following, the dynamical system description of an AMIL gate in a trapezoidal canal is derived.

Gate Movement

To determine the gate movement, we follow closely Corriga et al. (1977) and Ramirez-Luna (1997) and consider the moments on the gate acting about the gate axis

\[ I \frac{d^2 \theta}{dt^2} + c \omega \frac{d\theta}{dt} = M_w(\theta, Y_1) + M_g(\theta). \]  

(4)

We refer with \( M_w \) respectively \( M_g \) to the moments exerted by the water respectively by gravity on the gate (the sign is defined by the direction of \( \theta \), i.e. positive sign of \( M \) in the direction of closing gate). As third moment, we consider the effect of the angular damping coefficient \( c_{\omega} \).

The moment by gravity \( M_g \) depends on the position of the centre of gravity \((\omega_{CG}, r_{CG})\) and the mass \( m \) of the movable parts of the gate. Referring to Fig. 2 we can write

\[ M_g(\theta) = -mr_{CG}g \cos(\theta + \omega_{CG}). \]  

(5)

To compute the moment due to the water, we simplify by assuming a hydrostatic pressure distribution along the gate leaf based on the water level \( Y_1 \). In doing so we follow Corriga et al. 1977, Ramirez-Luna 1997. Preliminary investigations (Bernhard, 2015, unpublished; available by contacting the authors) compared the hydrostatic model to a model based on conservation of momentum over a control volume. The simpler hydrostatic model was able to reproduce more faithfully measured equilibrium positions of the EPFL gate as well as Computational Fluid Dynamics (CFD) simulations for three different gate positions. Hence, we neglect non-hydrostatic effects. As AMIL gates are radial gates and have a radial float with a curvature centred in the gate axis, the water pressure on the gate leaf and curved float surface does not exert a moment about the gate axis. We furthermore assume that any water mass on the downstream side of the gate doesn’t exert any moment either. Thus, it is sufficient to consider only the bottom part of the float for the moment due to the water. We can express the hydrostatic pressure \( p \) as a function of \( \theta \) and \( Y_1 \) and the distance \( \hat{r} \) to the gate axis

\[ p(\hat{r}, \theta, Y_1) = \rho g \left( Y_1 - (Y_a - \sin(\theta)\hat{r}) \right), \]  

(6)

and integrate the moment about the gate axis over the float bottom. This leads to the expression for the moment exerted
by the water (7)

\[ M_w(\theta, Y_1) = -b_F \int_R^\infty \hat{r} p(\hat{r}, \theta) \, d\hat{r} \]
\[ = -b_F \rho g \left( \frac{r^2 - R^2}{2} (Y_1 - Y_a) + \frac{r^3 - R^3}{3} \sin(\theta) \right). \] (8)

The angular damping coefficient is assumed to be constant, although the elongation of the dashpot used for damping depends on the current gate position. The reader might refer to (Ramirez-Luna 1997), where this nonlinear effect is further treated. To include it, additional parameters describing the exact attachment configuration would need to be defined. However, when using the parameters given by (Ramirez-Luna 1997), the nonlinear effect remains small as shown recently (Bernhard, 2015, unpublished; available by contacting the authors) and it will therefore be neglected in this study by using a constant angular damping coefficient.

Water Level Change

Modelling a level pool allows dynamic interaction between the gate position and the water level. This level pool acts as a finite control volume for mass conservation of an incompressible fluid (Munson et al. 2009). It allows to transform the effect of a change in the gate position via a change in discharge into a change in the water level. Note that a level pool represents a simplification of reality and that the length we choose for this reservoir is a model parameter that can be linked to reality for example through calibration.

Considering a length \( l \), the level pool leads to a volume

\[ V = blY_1 + \tan(\alpha)lY_1^2. \] (9)

Note that only the volume in front of the gate is considered (between the first two dashed, red lines in Fig. 2) and that the volume below the gate is approximated with a constant value regardless of the gate position. Change in the level pool volume is related to the in- and outflow by a simple reservoir volume balance equation

\[ \frac{dV}{dt} = Q_i - Q_g, \] (10)

or, in terms of water level \( Y_1 \) by using (9)

\[ \frac{dY_1}{dt} = \frac{1}{l(b + 2 \tan(\alpha)Y_1)} (Q_i - Q_g). \] (11)
**Discharge Through the Gate**

The flow rate or discharge through the gate needs to be expressed as a function of $Y_1$, $\theta$, and $Y_3$. We distinguish between free and submerged flow depending on the downstream water depth. In case of free flow we replace $Y_3$ with $C_c Y_g$, which represents the depth of the vena contracta.

The discharge law and coefficients we use are based on (Corriga et al. 1977). The law computes the total discharge as a sum of an orifice flow and free weir discharge by considering two distinct areas $\sigma_{\text{orifice}}$ and $\sigma_{\text{free}}$. These areas are shown for the free flowing gate in Fig. 2 and they represent the unobstructed areas between the canal bottom and the downstream depth $Y_3$ ($\sigma_{\text{orifice}}$), respectively between the downstream depth $Y_3$ and the upstream depth $Y_1$ ($\sigma_{\text{free}}$). For simplicity, the same correction factor $\mu$ is used for both these discharges, similar to (Corriga et al. 1977). To express the discharge over each area we make the common assumptions of horizontal flow, atmospheric pressure within the weir nappe, as well as uniform and small approaching velocity upstream of the gate (Munson et al. 2009). We write the discharge as

$$Q = \int_0^{Y_1} u(\hat{y}) b(\hat{y}) d\hat{y}. \quad (12)$$

To express the discharges for the two distinct areas with the problem parameters, we need to distinguish between the cases $Y_3 > Y_g$ (submerged) and $Y_3 < Y_g$ (e.g. free flow), where $Y_g = Y_g(\theta)$ refers to the gate opening from equation (2).

For $Y_3 < Y_g$ (e.g. for free flow $Y_3 = C_c Y_g$) we decompose the total discharge in an orifice part: $Q_1$, a free weir part through the area below $Y_g$: $Q_2$, and a free weir part through the area on the side of the gate: $Q_3$. This leads to

$$Q_g = Q_{g,\text{free}} = Q_1 + Q_2 + Q_3,$$  \quad (13)

where

$$Q_1 = \mu \sqrt{2g} \left( Y_3 (b + \tan(\alpha)Y_3) \right) \sqrt{Y_1 - Y_3} \quad (14a)$$

$$Q_2 = \mu \sqrt{2g} \left[ \frac{2}{3} b ((Y_1 - Y_3)^{3/2} - (Y_1 - Y_g)^{3/2}) \right.$$

$$\left. + \frac{4}{15} \tan(\alpha) \left( (3Y_3 + 2Y_1)(Y_1 - Y_3)^{3/2} \right.$$

$$\left. - (3Y_g + 2Y_1)(Y_1 - Y_g)^{3/2} \right] \quad (14b)$$

$$Q_3 = \mu \sqrt{2g} \left( \frac{2}{3} \tan(\alpha) Y_g(1 - Y_g) \right) \sqrt{Y_1 - Y_g}. \quad (14c)$$

For $Y_3 > Y_g$ (submerged case) we follow (Corriga et al. 1977) and write

$$Q_g = Q_{g,\text{submerged}} = \mu \sqrt{2g} \left( \sigma_{\text{orifice}} + \frac{2}{3} \sigma_{\text{free}} \right) \sqrt{Y_1 - Y_3}. \quad (15)$$
where
\[
\sigma_{\text{orifice}} = bY_g + Y_g^2 \tan(\alpha) + 2Y_g \tan(\alpha)(Y_3 - Y_g) \tag{16a}
\]
\[
\sigma_{\text{free}} = 2Y_g \tan(\alpha)(Y_1 - Y_3). \tag{16b}
\]

Corriga et al. (1977) modelled submerged conditions with a varying downstream depth, based on the discharge itself. The applied formulation does not always yield physical solutions, especially for low discharges at almost closed gate. For submerged conditions, we impose therefore a fixed downstream depth, independent from the flow rate, and consider the free flowing gate separately.

Next, we normalise the input discharge by introducing a hypothetical nominal discharge \(Q_n\) as a scaling
\[
Q'_i = \frac{Q_i}{Q_n}. \tag{17}
\]
For both, free and submerged gates, we define the nominal discharge as the free discharge at completely open gate with the water level at axis height, i.e.
\[
Q_n := Q_{g,\text{free}}(\theta = 0, Y_1 = Y_a, Y_3 = C_c Y_g). \tag{18}
\]

**Combined system and nondimensionalisation**

Combining the derived models for the variation of the gate position (4) and water level (11), we can derive a dynamical system governed by the following basic equations
\[
\frac{d^2 \theta}{dt^2} = \frac{c_1}{T} \frac{d\theta}{dt} + c_2(Y_1 - Y_a) + c_3 \cos(\theta) + c_4 \sin(\theta) \tag{19a}
\]
\[
\frac{dY_1}{dt} = \frac{1}{l(b + 2 \tan(\alpha)Y_1)} \left[ \frac{Q_n Q'_i - Q_g(\theta, Y_1, Y_3)}{b + 2 \tan(\alpha)Y_1} \right]. \tag{19b}
\]

With basic algebraic manipulations we reformulate (19) as
\[
\frac{d^2 \theta}{dt^2} = c_1 \frac{d\theta}{dt} + c_2(Y_1 - Y_a) + c_3 \cos(\theta) + c_4 \sin(\theta) \tag{20a}[\text{rad/s}^2]
\]
\[
\frac{dY_1}{dt} = c_5 \frac{1}{b + 2 \tan(\alpha)Y_1} \left[ Q_n Q'_i - Q_g(\theta, Y_1, Y_3) \right]. \tag{20b}[\text{m/s}]
\]

where the definitions of the constants \(c_1\) to \(c_6\) are reported in appendix I.
We now derive the dimensionless form of the basic equations (20) by introducing a length scale \( \Lambda \) and a time scale \( \tau \), to scale all the lengths (\( Y, l, R, r, \ldots \)) and time

\[
Y = \Lambda \tilde{Y} \quad t = \tau \tilde{t}.
\]

Based on the geometrical normalisation it is straightforward to choose \( \Lambda = D \). We assume a time scale \( \tau = \sqrt{\frac{D}{g}} \). Equations (20) can then be reformulated as

\[
\frac{d^2 \theta}{dT^2} = C_1 \frac{d\theta}{dT} + C_2 (\tilde{Y}_1 - \tilde{Y}_a) + C_3 \cos(\theta) + C_4 \sin(\theta) \quad [\text{rad}^2] \tag{21a}
\]

\[
\frac{d\tilde{Y}_1}{dT} = C_6 Q_n Q'_i - Q_g(\theta, \tilde{Y}_1, \tilde{Y}_3) \quad [-] \tag{21b}
\]

where the constants \( C_1 \) to \( C_6 \) in equations (21) are given in appendix I.

The system designated by equations (21) can be rewritten as three first-order equations

\[
\frac{d\theta_1}{dT} = \theta_2 \tag{22a}
\]

\[
\frac{d\theta_2}{dT} = C_1 \theta_2 + C_2 (\tilde{Y}_1 - \tilde{Y}_a) + C_3 \cos(\theta_1) + C_4 \sin(\theta_1) \tag{22b}
\]

\[
\frac{d\tilde{Y}_1}{dT} = \frac{C_6}{\tilde{b} + 2 \tan(\alpha) \tilde{Y}_1} (Q_n Q'_i(\tilde{t}) - Q_g(\theta, \tilde{Y}_1, \tilde{Y}_3(\tilde{t}))), \tag{22c}
\]

which is a system of the form

\[
\frac{d}{dT} x = F(x, \tilde{t}), \tag{23}
\]

with states \( x = (\theta_1, \theta_2, \tilde{Y}_1)^T := (\theta, \frac{d\theta}{dT}, \tilde{Y}_1)^T \).

Equations (22) characterise a three-dimensional, nonautonomous, nonlinear dynamical system. The inputs to the system are \( Q'_i(\tilde{t}) \) and \( \tilde{Y}_3(\tilde{t}) \) (if submerged). By integrating system (22) it is possible to simulate a transient response to time dependent inputs.

However, most of the stability analysis in this study is based on the assumption that the inputs are constant in time.

In that case, the inputs can be regarded as parameters of a completely autonomous system

\[
\frac{d}{dT} x = F(x). \tag{24}
\]

Based on equation (24) we define an equilibrium point \( x^* \) such that \( F(x^*) = 0 \).
Calibration of the Gate and Control Parameters

In the following, we show how the mass and the position of the centre of gravity can be related to the
decrement in \( \tilde{Y}_1 \).

We define the decrement as the difference in the equilibrium state \( \tilde{Y}_1 \) between completely closed
gate \( \theta_1 = \theta_c \) (\( Q'_i = 0 \)) and completely open gate \( \theta_1 = 0 \). Fig. 3 shows the equilibrium states \( \tilde{Y}_1^* \) vs. \( \theta_1^* \) for various \( Q'_i \). The figure
indicates the decomposition of the total decrement into a decrement above \( (\tilde{d}_A) \) and a decrement below the gate axis
(\( \tilde{d}_B \)). Given these definitions we can derive an analytical expression for \( \omega_{CG} \) and \( \tilde{m}_{CG} \) as function of \( \tilde{d}_A \) and \( \tilde{d}_B \) by
considering the equilibrium points at these two positions. According to the above definition of the decrement, these
gate positions are in principle \( \theta_{1A} = 0 \) and \( \theta_{1B} = \theta_c \). However, we can remain more general by using arbitrary positions
\( x_A^* = (\theta_{1A}, 0, \tilde{Y}_a + \tilde{d}_A)^T \) and \( x_B^* = (\theta_{1B}, 0, \tilde{Y}_a - \tilde{d}_B)^T \). Setting equation (22b) at these positions to zero yields

\[
\begin{align*}
\tilde{m}_{CG} &= -\frac{(\tilde{\theta}_1^2 - \tilde{R}_1^2) \tilde{d}_A + (\tilde{\theta}_1^2 - \tilde{R}_1^2) \sin(\theta_{1A})/3}{\cos(\theta_{1A} + \omega_{CG})} \\
\tilde{m}_{CG} &= -\frac{(\tilde{\theta}_1^2 - \tilde{R}_1^2) (-\tilde{d}_B) + (\tilde{\theta}_1^2 - \tilde{R}_1^2) \sin(\theta_{1B})/3}{\cos(\theta_{1B} + \omega_{CG})}.
\end{align*}
\]

(25)

Considering the specific positions \( \theta_{1A} = 0 \) and \( \theta_{1B} = \theta_c \), equation (25) simplifies eventually to

\[
\tan(\omega_{CG}) = \tan(\omega_{CG} + k\pi) \quad \forall k \in \mathbb{Z}
\]

\[
= \frac{1}{\tan(\theta_c)} - \frac{1}{\tilde{d}_A} \frac{2(\tilde{\theta}_1^2 - \tilde{R}_1^2)}{3(\tilde{\theta}_1^2 - \tilde{R}_1^2)} + \frac{\tilde{d}_B}{\tilde{d}_A} \frac{1}{\sin(\theta_c)}
\]

(26)

Thus, an analytical expression for \( \omega_{CG} \) and \( \tilde{m}_{CG} \) is given by

\[
\begin{align*}
\omega_{CG} &= \pi + \arctan\left(\frac{1}{\tan(\theta_c)} \frac{2(\tilde{\theta}_1^2 - \tilde{R}_1^2)}{3(\tilde{\theta}_1^2 - \tilde{R}_1^2)} + \frac{\tilde{d}_B}{\tilde{d}_A} \frac{1}{\sin(\theta_c)}\right) \\
\tilde{m}_{CG} &= \frac{1}{\cos(\omega_{CG})}\left(-\frac{\tilde{\theta}_1^2 - \tilde{R}_1^2}{2}\tilde{d}_A\right).
\end{align*}
\]

(27)

Note that we assumed \( \tilde{d}_A \neq 0 \) to derive (25). If one imposes \( \tilde{d}_A = 0 \), the centre of gravity comes to lie perpendicular
to the float bottom (\( \omega_{CG} = \pi/2 \)) in order to have a balanced gate at complete opening \( \theta_1 = 0 \). Corriga et al. (1977)
assumed a perfectly calibrated gate, i.e. \( \tilde{d}_A = \tilde{d}_B = 0 \). This corresponds to the ideal case, regulating the water level
without any deviation from \( \tilde{Y}_a \). Given \( \tilde{Y}_1 = \tilde{Y}_a \), the gate is in equilibrium for any position \( \theta_1 \). Under this assumption,
we have \( \omega_{CG} = \pi/2 \), and the mass has to compensate precisely the immersed float \( \tilde{m}_{CG} = (\tilde{\theta}_1^2 - \tilde{R}_1^2)/3 \). Therefore,
the terms \( C_3 \) and \( C_4 \) become zero and the system simplifies.

The information available in (GEC Alsthom 1992) indicates a typical total decrement \( \tilde{d}_A + \tilde{d}_B \) of 0.02 (±). In the
following analysis, we assume \( \tilde{d}_B = 0 \) and \( \tilde{d}_A = 0.02 \).

The typical functioning of the AMIL gate is illustrated by Fig. 5. A free gate, subject to a step-like increasing
input $Q'_i(t)$, is simulated starting at the equilibrium state. Simulation a) shows that with the arrival of the increased discharge the gate opens and the water level rises within the limits defined by the decrement. By opening the gate the increase in water level is mitigated. We can furthermore compare the behaviour of the same gate with different damping coefficients and different level pool lengths (b) and c)). While the strongly damped gate a) follows the equilibrium curve closely, the less damped gate b) oscillates during the transition from one equilibrium point to the other. We can observe that the shorter level pool b) influences the trajectory of these oscillations as the water level rises more quickly. The observed oscillations are possible due to the assumption of a dynamic equilibrium between gate and water level, instead of a static relationship, that would simply follow the equilibrium curve.

Once a gate geometry and size is chosen (i.e. $\alpha, \dot{h}, \dot{b}_F, \dot{Y}_a, \dot{R}, \omega_F, I$) and further constants are defined ($\mu = C_c C_v$), five control parameters $m$ remain to completely define the autonomous system (24). We can recast the function $F$ to use these parameters $m$ as arguments and the system becomes

$$\frac{d}{dt} x = F(x, m) \quad m = \begin{bmatrix} \dot{c}_\omega \\ Q'_i \\ \tilde{d}_A \\ I \\ \dot{Y}_1 \end{bmatrix},$$

which is the form we analyse in the following.

**STABILITY ANALYSIS AND NONLINEAR EFFECTS OF CONTROL PARAMETERS**

**Preliminary Consideration**

We start with investigating the two limit cases, where the level pool dynamics happen on a much faster ($\tilde{I} \ll 1$) or slower scale ($\tilde{I} \gg 1$) than the gate dynamics. Note first that the constants $C_1, C_2$, and $C_4$ are of order $O(1)$, $C_3$ is of order $O(10^{-2})$, and $C_6$ is of order $O(\tilde{l}^{-1})$.

For $\tilde{I} \gg 1$ ($C_6 \to 0$) we infer from equations 21 (or equations 20) that oscillations of $\tilde{Y}_1$ are slow and $\tilde{Y}_1$ can be considered constant. Equation 21a describes the gate movement, during which a constant value for $\tilde{Y}_1$ can be assumed. The eigenfrequency of this subsystem is given by linearising equation 21a around an equilibrium point $x^*$ (i.e. $\tilde{Y}_1^*$ and $\theta^*$) which yields:

$$\omega_0 = \sqrt{C_3 \sin(\theta^*) - C_4 \cos(\theta^*)}$$

$$\omega = \sqrt{\omega_0^2 - \left(\frac{C_1}{2}\right)^2} = \sqrt{\omega_0^2 - \left(\frac{\dot{c}_\omega}{2}\right)^2},$$

for both the undamped ($\omega_0$) and the damped ($\omega$) subsystem. A critical damping $\dot{c}_{\omega, crit}$ separates under- from
overdamped systems, when $\omega_0 < \tilde{c}/2$. Furthermore, note that when the gate is perfectly calibrated, the terms $C_3$ and $C_4$ are zero. In that case if the water level is perturbed, equation 21a doesn’t allow a feedback of $\theta$ and is thus unstable.

For $\tilde{l} \ll 1$ ($C_6 \to \infty$) the evolution of $\tilde{Y}$ becomes very fast compared to the gate. Dividing equation 21a by $C_6$ and taking the limit of $C_6 \to \infty$, results in static relationship $\tilde{Y} = f(\theta)$, which is stable.

To summarise the findings of the limit cases, we conclude that the system is generally stable for both – small and large – values of $\tilde{l}$. The gate and level pool subsystems can thus be regarded as interfering with each other only if their time scales are similar, i.e. in an intermediate range of $\tilde{l}$.

In the following analysis, we consider a base state of the control parameters $m_0$. Varying one parameter at the time, we observe the change in the qualitative behaviour of the solutions. Equilibrium points, their stability (Lyapunov or asymptotic), one-parameter bifurcations points and the corresponding limit cycles (including their stability) are investigated by means of a combination of analytical and numerical methods. For comparison with Corriga et al. [1977] this analysis is based on the same gate. Besides the geometric gate properties mentioned in table 1, we use values based on either (Corriga et al. 1977): $I = 0.0103$, and $\mu = C_c C_v = 0.65$ ($C_c = \mu/0.97$); or from GEC Alsthom 1992: $\alpha = \arctan(1/2)$. The base set of control parameters is given by

$$m_0 = \begin{bmatrix}
\tilde{c}_{\omega,0} \\
Q'_I,0 \\
\tilde{\alpha},0 \\
\tilde{l}_0 \\
\tilde{Y}_A,0
\end{bmatrix} = \begin{bmatrix}
1.0 \\
0.5 \\
0.02 \\
0.253 \\
0.25
\end{bmatrix}.$$ (30)

**Influence of $\tilde{c}_{\omega}$**

Linear stability of equilibrium points for the parameters $m_0$ can be studied with the eigenvalues of the Jacobian ($\frac{\partial F}{\partial x}$) after linearisation (Guckenheimer and Holmes 1993). Due to the complexity of the system, only one equilibrium point is computed numerically. The eigenvalues of the Jacobian, evaluated at the equilibrium point, are shown in Fig. 6 for various values of $\tilde{c}_{\omega}$ for both, free and submerged gate. In both cases, we observe a single real and negative eigenvalue and a pair of complex conjugate eigenvalues. The pair of complex eigenvalues has a positive real part for low values of $\tilde{c}_{\omega}$, but it becomes negative above a certain limiting value. These limiting values $\tilde{c}_{\omega,lim}$ are 1.670 and 1.097 for the free respectively the submerged gate. The equilibrium point is thus unstable at the lower values, but is stabilised at the higher damping. Numerical simulations with the nonlinear system using slightly perturbed initial conditions confirmed this stabilising value of $\tilde{c}_{\omega}$. The eigenvalues remain in the left half-plane, i.e. stable, for further increases in the damping parameter $\tilde{c}_{\omega}$. We note that above another specific value of $\tilde{c}_{\omega}$ the pair of complex conjugate eigenvalues becomes real valued ($\tilde{c}_{\omega,crit} = 42.0$, respectively 14.8). This critical damping value illustrates the effect
of the level pool (equation 21b), which was neglected for $\tilde{c}_{\omega, crit}$ in the preliminary considerations. The qualitative characteristics of this plot of the eigenvalues in Fig. 6 are similar to the plot of the roots of the transfer function shown in (Corriga et al. 1977).

Simultaneous passing of the imaginary axis by two eigenvalues, while no other eigenvalue has zero real part, indicates a Hopf bifurcation at the parameter value of the crossing (Guckenheimer and Holmes 1993). A Hopf bifurcation describes the emergence of limit cycles from an equilibrium point when a parameter is varied (Guckenheimer and Holmes 1993; Ermentrout 2002). We investigate this bifurcation of the nonlinear system at $\tilde{c}_{\omega, lim}$ with the software package XPPAUT (Ermentrout 2002), containing the numerical continuation software AUTO (Doedel and Oldeman 2012).

Fig. 7 shows the one-parameter bifurcation diagrams for various control parameters for the submerged system. These diagrams show the gate position $\theta_1$ in equilibrium position respectively the minimum and maximum values on the limit cycles, as well as the periods $\tilde{T}$ of the limit cycles. We note the emergence of stable limit cycles when the damping is below the limiting value. Having stable limit cycles, the system undergoes a supercritical Hopf bifurcation.

The existence of these periodic solutions is confirmed numerically. Periodic solutions, found using a boundary value approach, are shown in Fig. 8. (The applied procedure is based on (Higgins 2013), which also explicits the derivation of the boundary value problem.)

The evolution of the gate position and water level during a cycle and the trajectory in the state space are shown for the free gate (left) and the submerged gate (right) for $m_0$. Both systems are shown for the same damping ratios $\tilde{c}_{\omega}/\tilde{c}_{\omega, lim}$ and $Q'_i$ is chosen for each system separately to yield similar equilibrium positions in $\theta_1$. The trajectories are in agreement with the values shown by Fig. 7. We observe a phase shift in the trajectories between gate position $\theta_1$ and water level $\tilde{Y}_1$. The periods and Floquet multipliers of these periodic solutions are shown in table 2. With only one Floquet multiplier of magnitude 1 or higher, the limit cycles are stable.

**Influence of $Q'_i$**

To assess the influence of the parameter $Q'_i$ we first look at the linear stability of the equilibrium point for the base parameters $m_0$. The eigenvalues of the Jacobian are shown in Fig. 9 for various values of $Q'_i$ for the submerged gate. The free gate is not shown, behaving qualitatively similar. As the equilibrium point depends on the value of $Q'_i$, the Jacobian needs to be re-evaluated at each (numerically found) equilibrium point. Again, there exists a limiting value $Q'_{i, lim}$ of 0.5638 (respectively 0.8217 for the free gate) stabilising the system. Again, numerical simulations with perturbed initial conditions confirmed these limiting values.

The evolution of the eigenvalues in the complex plane for varying $Q'_i$ is similar to the evolution for varying $\tilde{c}_{\omega}$. A supercritical Hopf bifurcation for the parameter $Q'_i$ is expected and confirmed by the second bifurcation diagram in Fig. 7.
The resulting periodic solutions for values below $Q'_{i, \text{lim}}$ are qualitatively similar to the ones shown in Fig. 8 for variations in $\tilde{c}_\omega$. The magnitude of the oscillations increase with decreasing $Q'$, an observation that can readily be inferred from the bifurcation diagram.

The response to the step-like input $Q'_i(t)$ shown in Fig. 5 illustrates the change in stability due to $Q'$. Fig. 10 compares the response to such a step-like input for the free and submerged gate using the same damping ratio $\tilde{c}_\omega/\tilde{c}_{\text{oa,lim}} = 0.61$, based on $\tilde{c}_{\text{oa,lim}}$ for the initial value of $Q'$. The input $Q'_i(t)$ increases from 0.2 to 0.7. Both gates are unstable at the initial value of $Q'$ and start to oscillate. The systems stabilise with increasing discharge as they are stable at the final value of $Q'$. The damping $\tilde{c}_\omega$ of the submerged gate used for the simulation is lower compared to the free gate (1.80 vs. 1.17).

**Influence of $\tilde{d}_A$ and $\tilde{Y}_3$**

The relationship between $Q'$ and $\tilde{c}_{\text{oa,lim}}$ is illustrated by Fig. 11. It shows the free gate system using various values for $\tilde{d}_A$ in a), while the submerged gate system uses $\tilde{d}_A = 0.02$ but various submergence depths $\tilde{Y}_3$ in b). Generally, the limiting values $\tilde{c}_{\text{oa,lim}}$ decrease with increasing discharge (i.e. larger gate openings), illustrating again the stabilising effect of large $Q'$. A shift in the $x$-axis can be observed between the plots showing the limiting values for the same system, but either using $Q'_i$ or $\theta_{eq}$ (compare for example subplots b) and d)). These shifts depend on the value of $\tilde{d}_A$ or $\tilde{Y}_3$. This is caused by the influence of these parameters on the equilibrium position $\theta_{eq}$ for the same $Q'$.

An increase in the decrement $\tilde{d}_A$ might have a stabilising or destabilising effect on the system, i.e. requiring a lower/higher damping, depending on the $Q'$ considered. However, the destabilising effect seems to be explained through the change in the equilibrium position $\theta_{eq}$ for different decrements. Indeed judging only by the free gate plot against $\theta_{eq}$ in c), an increase in the decrement decreases the $\tilde{c}_{\text{oa,lim}}$ for almost all equilibrium positions.

For the submerged gate, an increase in the downstream depth $\tilde{Y}_3$ stabilises the gate. It is likely that this is caused by the reduced sensitivity of the gate discharge $Q_g$ to the gate position $\theta_1$ (i.e. a smaller $\partial Q_g/\partial \theta_1$). This can be observed for the various values of $\tilde{Y}_3$ in Fig. 11 (subplots b) and d)).

**Influence of $\tilde{I}$**

Already highlighted by the preliminary considerations, the system is generally stable in the limits $\tilde{I} \ll 1$ and $\tilde{I} \gg 1$, unless the total decrement is set to zero, where stability occurs only in the lower limit $\tilde{I} \ll 1$. These observations are confirmed by Fig. 12 showing the real part of the second eigenvalue of the linearised system as a function of $\tilde{I}$. The bifurcation diagram for $\tilde{I}$ in Fig. 7 identifies two supercritical bifurcations. The period of the limit cycle, shown in the same figure, differs strongly.

Fig. 13 shows the identified limiting damping parameter $\tilde{c}_{\text{oa,lim}}$ as a function of $\tilde{I}$. We notice that the value of $\tilde{I}$ resulting in the highest $\tilde{c}_{\text{oa,lim}}$ depends on the value of $\tilde{d}_A$.
PRACTICAL CALIBRATION OF MODEL PARAMETER $\tilde{l}$ TO MEASURED DYNAMICS

We recall that the level surface is a simplifying assumption, using a model-related – not problem-related – parameter $\tilde{l}$. In the following, we calibrate this parameter $\tilde{l}$ to observed wave interactions with a canal. We performed video measurements of the dynamical behaviour of the experimental gate at EPFL. Two distinct dynamic regimes have been recorded. Videos of the two behaviours are available as electronic supplementary material (S2 and S3). The gate position during the two dynamic responses is shown in Fig. 14.

In behaviour A), the upper end of the canal reach upstream of the gate, situated at a distance $L$, acts as a reflecting boundary for incoming waves. A periodic solution develops as the waves in the canal and the gate synchronise. The periodic solution corresponds to a standing wave in the canal with the gate oscillating at the same frequency.

Behaviour B) corresponds to a transient response, describing the gate rising, after being initially locked in closed position. Over the short period of time we consider, the reflecting upstream boundary has no effect on the gate, as the perturbations generated by the gate travel with a finite speed.

Both measurements were taken under free flowing conditions. The gate setup at EPFL is described by the following measured quantities: $D = 0.81$m, $R = 0.63$m, $r = 0.685$m, $Y_a = 0.367$m, $b = 0.46$m, $b_F = 0.36$m, $\omega_F = 0.173$m/$R$, $\alpha = \arctan(1/2)$, $\omega_{CG} = 1.61$rad, $m_{CG} = 8.13$kgm, and the estimated dynamic properties: $I = 7.67$Nm$^2$/rad, and $c_{sw} = 69.0$Nms/rad. The canal reach ends at a distance $L = 4.17$m upstream of the gate leaf in a boundary, where the inflow enters the canal reach through the bottom part.

The length of the level pool volume can be calibrated to reproduce the observed behaviour. While situation A) is representative of a short canal reach under the influence of an upstream reflecting boundary, situation B) can describe an infinitely long canal reach, where the generated perturbations are not reflected upstream. These two situations can be characterised by two different values of $\tilde{l}$.

For behaviour A), we can describe the standing wave in the canal with standing wave theory (SWT). We recall the sensitivity of the frequency of the gate to the model parameter $\tilde{l}$, observed in the bifurcation diagram (Fig. 7). This allows us to estimate $\tilde{l}$ for a given frequency. We combine both of these approaches to estimate the parameter $\tilde{l}$ for AMIL gates with canals of various lengths $L$ showing standing wave behaviour.

In the observed case, the ratio of the flow velocity to the wave celerity is small ($U_0/c \ll 1$). Therefore, we apply classic SWT using a constant celerity in both directions. SWT allows us to determine the frequency of a specific mode for a canal of a given length $L$. Based on that the parameter $\tilde{l}$ can be determined by adjusting the frequency of the gate to the standing wave in the canal. In behaviour A) both ends of the canal were antinodes, i.e. the amplitude of the oscillations is at its maximum. This can be translated to boundary conditions prescribing the gradient of the water level to be zero. The frequency of the modes is then given by $f_n = nc/(2L)$, where the wave celerity is related to the equilibrium water level by $c = \sqrt{gY_1^*}$. The observed behaviour A) corresponds to the mode with $n = 4$, giving us a theoretical frequency by wave theory of $f_{4,SWT} = 0.93$Hz or $\omega_{4,SWT} = 5.85$rad/s (using $Y_1^* = 0.385$m for both). The
level pool length required to obtain the same frequency of gate oscillations is \( \tilde{l}_{SWT} = 0.043 \).

However, the frequency of the observed behaviour does not exactly coincide with the one predicted by standing wave theory. Further studies including nonlinear effects may explain such differences. The measured frequency was \( f_{meas} = 0.81 \text{Hz} \) or \( \omega_{meas} = 5.09 \text{rad/s} \). The level pool length corresponding to this frequency is \( \tilde{l}_{meas,A} = 0.05 \).

We consider behaviour B) over roughly two oscillation cycles, corresponding to the time before the perturbations return. (The inflow \( Q_i \) was adapted to compensate the flow above the gate that occurred during the measurement.) A parameter \( \tilde{l}_{meas,B} = 0.14 \) was calibrated for this behaviour. Transient effects from the reflection of the waves remain after the two oscillations cycles, but eventually the gate stabilises.

The model simulation for the parameters \( \tilde{l}_{meas,A} \) and \( \tilde{l}_{meas,B} \) and two different inflow discharges are superimposed onto Fig. [14]. Note that using the value of \( \tilde{l} = 0.253 \) from [Corriga et al. 1977] would result in too low frequencies to reproduce either behaviour A) nor B).

In conclusion the choice of \( \tilde{l} \) thus depends on the type of dynamic one wants to reproduce.

**CONCLUSION AND OUTLOOK**

In this article a mathematical model was developed based on [Corriga et al. 1977] [Ramirez-Luna 1997] and investigated with respect to various control parameters. The model was used to reproduce two kinds of dynamic behaviour of an experimental gate. For the calibration of the counterweights, we presented an analytical formula permitting to impose a specified decrement. The stability analysis allowed to determine limiting values for the damping parameter \( \tilde{c}_{\omega,lim} \). We’ve shown a change in behaviour at these limiting values from stable equilibria to stable periodic solutions – a supercritical Hopf bifurcation. The periodic solutions are not desired in irrigation canals, leading to fluctuations of discharges in the main canal and lateral off-takes. The constant inflow parameter \( Q_i' \) exhibits similar influence on the system as \( \tilde{c}_{\omega,lim} \).

The identified limiting values depend on the model parameter \( \tilde{l} \). It is therefore important to use a representative level pool length \( \tilde{l} \) or to simply select the most conservative damping \( \tilde{c}_{\omega,lim} \) among the estimates obtained with a wide range of \( \tilde{l} \).

In view of the typically slow canal dynamics in irrigation canal networks [Corriga et al. 1980] [Ramirez-Luna 1997], the dynamic interactions between the water level and the gate are considered negligible by other authors and the simplification of a static gate appropriate. On the other hand, the model based on a level pool, used throughout this work, allows to consider the dynamic interaction between the local water level and the AMIL gate. This dynamic interplay might become more important under circumstances where faster water level dynamics are present (e.g. irrigations canals exhibiting resonance behaviour or situations outside of irrigation canals). Refraining from the static gate simplification, by using the level pool model, seems more appropriate in those circumstances.

To complement existing studies (e.g. [Ramirez-Luna 1997]), the model developed here can suggest a different
approach to study interaction of AMIL gates installed in series. In canals exhibiting strong resonance behaviour and weak wave attenuation, waves generated by a non-static gate-water level relationship – possible to model with the derived system – might reach and influence other AMIL gates up- or downstream.

To operate run-of-the-river hydropower plants, non-proportional water distribution from rivers is an efficient alternative to fixed-percentage (proportional) releases of the incoming flow [Razurel et al. 2015; Gorla and Perona 2013; Perona et al. 2013]. AMIL gates might constitute a possible, energy-free means for this repartitioning. We envision that the combination of a weir in the river and an AMIL gate with an adapted float form in the derived canal might allow to implement non-proportional dynamic environmental flows, hence the importance of similar studies that address stability conditions.

APPENDIX I. CONSTANTS

Constants for Dimensional System

\[ c_1 = \frac{C_\omega \omega}{I} \] \hspace{1cm} \text{[s}^{-1}] \hspace{1cm} (31a)
\[ c_2 = -\frac{b_F \rho g r^2 - R^2}{I} \] \hspace{1cm} \text{[rad/(s}^2 \text{m}]} \hspace{1cm} (31b)
\[ c_3 = -\frac{b_F \rho g mr_{CG}}{I} \frac{\rho_r CG \cos(\omega_{CG})}{b_F \rho} \] \hspace{1cm} \text{[rad/s}^2]\hspace{1cm} (31c)
\[ c_4 = -\frac{b_F \rho g}{I} \left( \frac{r^3}{3} - \frac{R^3}{3} - \frac{mr_{CG}}{b_F \rho} \sin(\omega_{CG}) \right) \] \hspace{1cm} \text{[rad/s}^2]\hspace{1cm} (31d)
\[ c_6 = \frac{1}{l} \] \hspace{1cm} \text{[m}^{-1}] \hspace{1cm} (31e)

Constants for Dimensionless System

\[ C_1 = c_1 \tau = \tilde{c}_\omega = \frac{C_\omega \omega}{I} \sqrt{\Lambda} \frac{\sqrt{A}}{g} \] \hspace{1cm} [-] \hspace{1cm} (32a)
\[ C_2 = c_2 \tau^2 \Lambda = -\frac{1}{l} \frac{\rho^2 - R^2}{2} \] \hspace{1cm} \text{[rad]} \hspace{1cm} (32b)
\[ C_3 = c_3 \tau^2 = -\frac{1}{I} \tilde{m}r_{CG} \cos(\omega_{CG}) \] \hspace{1cm} \text{[rad]} \hspace{1cm} (32c)
\[ C_4 = c_4 \tau^2 = -\frac{1}{l} \left( \frac{\rho^3}{3} - \frac{R^3}{3} - \tilde{m} r_{CG} \sin(\omega_{CG}) \right) \] \hspace{1cm} \text{[rad]} \hspace{1cm} (32d)
\[ C_6 = \frac{\tau}{\Lambda} = \frac{c_6}{\Lambda} = \frac{1}{\sqrt{A}} \frac{1}{\sqrt{gA^{5/2}}} \] \hspace{1cm} \text{[s/m}^3] \hspace{1cm} (32e)
\[ \tilde{c}_\omega = \frac{c_\omega}{T} \sqrt{\frac{\Lambda}{g}} \quad [-] \quad (33a) \]

\[ \tilde{I} = \frac{I}{\rho b_F \Lambda^3} \quad [\text{rad}^{-1}] \quad (33b) \]

\[ \tilde{m} r_{CG} = \frac{mr_{CG}}{b_F \rho \Lambda^4} \quad [-] \quad (33c) \]

**APPENDIX II. ACKNOWLEDGMENTS**

The Swiss National Science Foundation is greatly acknowledged for funding the projects REMEDY (Grant No. PP00P2153028/1). Paolo Perona wishes to thank the Climatology Research Group at the Institute of Geography of the University of Bern for hosting him as academic guest.

**APPENDIX III. SUPPLEMENTAL DATA**

Fig. S1 and Videos S2-S3 with the corresponding Data S2-S3 are available online in the ASCE Library (ascelibrary.org).

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<thead>
<tr>
<th>Group</th>
<th># of gates</th>
<th>$\tilde{Y}_a$</th>
<th>$\tilde{b}$</th>
<th>$\tilde{R}$</th>
<th>$\tilde{r}$</th>
<th>$\omega_F$ (rad)</th>
<th>$\theta_c$ (rad)</th>
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<td>0.448</td>
<td>0.565</td>
<td>0.565</td>
<td>0.665</td>
<td>0.401</td>
<td>0.517</td>
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<tr>
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<td>8</td>
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<td>0.733</td>
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<tr>
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<td>3</td>
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<td>0.806</td>
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<tr>
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<td>0.788</td>
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<td>0.192</td>
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<tr>
<td>(Corriga et al. 1977)</td>
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<td>0.633</td>
<td>0.658</td>
<td>0.314</td>
<td>0.434</td>
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</table>

**TABLE I.** Mean values of the dimensionless gate parameters for the four groups and the values used in (Corriga et al. 1977).
<table>
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<tr>
<th>$\frac{c_{re}}{c_{ao/1cm}}$</th>
<th>Period</th>
<th>Floquet 1</th>
<th>Floquet 2</th>
<th>Floquet 3</th>
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<td>1.000</td>
<td>0.996</td>
<td>$2.877 \times 10^{-7}$</td>
</tr>
<tr>
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<td>0.992</td>
<td>$2.902 \times 10^{-7}$</td>
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<tr>
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<td>0.985</td>
<td>$2.955 \times 10^{-7}$</td>
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<tr>
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<td>1.000</td>
<td>0.996</td>
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<tr>
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<td>1.000</td>
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<tr>
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<td>$1.559 \times 10^{-6}$</td>
</tr>
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</table>
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