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Anharmonic magnon excitations in noncollinear and charge-ordered RbFe\textsuperscript{2+}Fe\textsuperscript{3+}F\textsubscript{6}

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RbFe\textsuperscript{2+}Fe\textsuperscript{3+}F\textsubscript{6} is an example of a charge ordered antiferromagnet where iron sites, with differing valences, are structurally separated into two interpenetrating sublattices. The low temperature magnetically ordered Fe\textsuperscript{2+} (S=2) and Fe\textsuperscript{3+} (S=5/2) moments form a noncollinear orthogonal structure with the Fe\textsuperscript{3+} site displaying a reduced static ordered moment. Neutron spectroscopy on single crystals finds two distinct spin wave branches with a dominant coupling along b-axis Fe\textsuperscript{3+} chain axis. High resolution spectroscopic measurements find an intense energy and momentum broadened magnetic band of scattering bracketing a momentum-energy region where two magnon processes are kinematically allowed. These anharmonic excitations are enhanced in this non collinear magnet owing to the orthogonal spin arrangement.

Quasiparticles in condensed matter are generally long-lived and non-interacting with a prototypical example being magnon excitations in ordered magnetic lattices. Classically, in the high spin limit, these excitations correspond to transverse small-angle deviations of a spin vector away from the equilibrium direction with the length of the vector remaining fixed. This distortion of the underlying magnetic lattice is harmonic and results in underdamped spin waves. However, the conditions under which these excitations breakdown has become important to understanding low energy properties in a variety of systems including superconductivity \cite{1,2}, frustrated magnets \cite{3–5}, and also quantum liquids \cite{6–8,32}. We demonstrate the breakdown of this quasiparticle notion in a classical magnet with non collinear magnetic order establishing spin geometry as an ingredient establishing quasiparticle stability.

Due to enhanced phase space and also large quantum fluctuations, one-dimensional and low-spin magnets have been at the center of the search for the breakdown of conventional spin-waves into multiparticle states \cite{9–12}. Such composite particles carry fractional quantum numbers and are observed through decay products in scattering experiments \cite{13–16} resulting in a momentum and energy broadened continuum cross section and renormalization \cite{17–19} of the single-magnon dispersion and intensity. In collinear square lattice antiferromagnets, spin wave theory predicts two-magnon processes, which are longitudinally polarized, and correspond to the simultaneous creation of two magnons of opposite signs, reducing the value of the ordered spin moment compared to the full value S \cite{20}. The cross section scales as 1/S \cite{17} and is inherently weak in classical high-spin magnets \cite{21} and such processes have been generally investigated in S = 1/2 magnets where quantum fluctuations are large.

Another means of enhancing this cross section is through a non collinear magnetic structure where longitudinal and transverse excitations are intertwined through geometry of the magnetic lattice \cite{15,16,22}. In this work, we investigate such anomalous spin fluctuations in the charge ordered RbFe\textsuperscript{2+}Fe\textsuperscript{3+}F\textsubscript{6} based on an orthogonal spin geometry.

RbFe\textsuperscript{2+}Fe\textsuperscript{3+}F\textsubscript{6} crystallizes in the Pnma space group (Fig. 1 (a)) with the lattice parameters a =6.9663(4), b =7.4390(5) and c =10.1216(6) Å at T = 4 K. As mentioned in \cite{23}, RbFe\textsuperscript{2+}Fe\textsuperscript{3+}F\textsubscript{6} has a structure related to the α-pyrochlores A\textsubscript{2}B\textsubscript{2}X\textsubscript{6}X' but with a vacancy on one of the two A cations and another on the X' anion site that does not contribute to the BX\textsubscript{6} octahedra. Charge order in this compound originates from two different iron sites which have differing valences. The RbFe\textsuperscript{2+}Fe\textsuperscript{3+}F\textsubscript{6} structure can be described as a chain of corner-shared Fe\textsuperscript{3+}F\textsubscript{6} octahedra running along b and a chain of corner-shared Fe\textsuperscript{2+}F\textsubscript{6} octahedra running along the a-axis. The two chains are connected along the c axis to form a two dimensional network, reminiscent of a Kagome arrangement, in the (1 0 1) plane. While the Fe\textsuperscript{3+}F\textsubscript{6} octahedra are only slightly distorted, a substantial distortion exists on the Fe\textsuperscript{2+}F\textsubscript{6} octahedra likely due to the Jahn-Teller effect given the underlying orbital degeneracy for octahedrally coordinated Fe\textsuperscript{2+}. \cite{24–26}.

Both magnetic iron sites order antiferromagnetically below T\textsubscript{N}=16 K with the Fe\textsuperscript{2+} and Fe\textsuperscript{3+} magnetic moments oriented 90° with respect to each other forming a noncollinear structure. As illustrated in Fig. 1 (a), the Fe\textsuperscript{3+} moments point along the a-axis and are coupled antiferromagnetically through nearest-neighbor interaction along the b-axis. The Fe\textsuperscript{2+} moments point in the orthogonal direction (b-axis) and are coupled antiferromagnetically through nearest-neighbor interac-
The magnetic moment is equal to the Landé factor. Given that the expected magnetic moment of the Fe$^{3+}$ ions is 2, while the Fe$^{2+}$ displays the full ordered magnetic moment the ordered magnetic moment on the Fe$^{3+}$ is strongly reduced.

We apply neutron spectroscopic measurements to investigate the magnetic dynamics in RbFe$^{2+}$Fe$^{3+}$F$_6$. Single crystals of RbFe$^{2+}$Fe$^{3+}$F$_6$ were made using hydrothermal techniques discussed in the supplementary material. With each crystal weighing less than 1 mg, between three and five thousand were coalesed using hydrogen free Fomblin grease on a series of aluminum plates, using the long chain b-axis as a guide. The estimated total mass was between 0.3 - 0.5 g (Fig. 1 (b)). Neutron spectroscopy was performed using the MERLIN chopper spectrometer (ISIS, UK) and the MACS cold triple-axis (NIST, Gaithersburg). Further details are supplied in the supplementary information. The dynamical structure factor associated with the single magnon excitations was calculated using the SPINWAVE software [27].

We first discuss the dynamics in the low temperature magnetically ordered phase measured with the MERLIN chopper spectrometer. The inelastic spectra in the $b^*$ direction recorded on MERLIN at T = 5 K with two incident energies of $E_i = 25$ meV and $E_i = 10$ meV are shown in Fig. 2 (a) and 2 (c) respectively. Given the low dimensional nature of the structure (further confirmed by the magnetic dynamics discussed in the supplementary information) we have integrated along the a* and c* directions. Figure 2 (a) displays a spin wave dispersion stemming from $k=1$, reaching a maximum top of the band at $\sim 12$ meV. Higher resolution data taken with $E_i = 10$ meV displays an energy gap at the zone center of $\sim 2$ meV, indicating an easy-axis anisotropy. Moreover, at $k=1$, the spin wave dispersion separates into two branches with a mode at 2 meV and a second one around 4 meV. The lower mode reaches a flat maximum at $\sim 3.5$ meV while the higher mode disperses up to the 12 meV maximum observed on the $E_i = 25$ meV data. This separation is illustrated in the constant-Q cut $k=1$ displayed in Fig. 2 (e) (blue circles). In Fig. 2 (f), a constant-Q cut at $k=1.5$ shows the additional flat modes located near the magnetic zone boundary.

To understand the microscopic origin of these two modes and the dispersion, we have performed linear spin wave calculations based upon Heisenberg exchange and easy-axis anisotropy. As reported in the Cs counter-part [25], the nearest-neighbour interactions are dominated by super-exchange interactions, mediated by the F ions and are sensitive to distances and angles. Therefore, four different magnetic couplings are considered in this compound. The full spin Hamiltonian is written out in the supplementary information considering Fe-Fe nearest neighbour interactions mediated through Fe-F-Fe bonds. The four couplings constants considered are shown in Fig. 1 (a) and correspond to two intrachain couplings $J_{ch1}$ and $J_{ch2}$, associated to Fe$^{3+}$-Fe$^{3+}$ and Fe$^{2+}$-Fe$^{2+}$ interactions, respectively, and two interchain couplings $J_{int1}$ and $J_{int2}$ associated to Fe$^{3+}$-Fe$^{3+}$ interactions.

The calculations are illustrated in Figs. 2 (b) and 2 (d). Panel (b) illustrates a spin wave calculation where interchain interactions $J_{int1}=J_{int2}$=0 and panel (d) shows a calculation with both inter and intra chain interactions non zero. The band observed in the data for $E_i = 25$ meV (Fig. 2 (a)) corresponds to the dispersion along the Fe$^{3+}$-b-axis chain as illustrated in panel (b) which was used to adjust the $J_{ch2}$ intrachain coupling (indicated by the white arrows) and the easy-axis anisotropy associated with this site. The other terms of the spin Hamiltonian could be refined from the lower energy $E_i=10$ meV.
The strongest coupling $J_{ch2}$ is hence found along the Fe$^{3+}$-Fe$^{3+}$ chain where the Fe-F-Fe angle is the closest to 180°. Describing the system as two interacting spin chains allows an understanding of the low-energy data: without the interchain interactions, the data in the $k$ direction would only appear as a single mode stemming from $Q=(0\ 0\ 0)$ accounting for the dispersion of the Fe$^{3+}$ chain (Fig. 2 (b)). Because of the interaction with the Fe$^{2+}$ chain, the coupling between the two chains leads to the separation of the low-energy dispersion into two modes (Fig. 2 (d)), thus setting up two energy scales in the spin dynamics: one higher energy scale associated with the Fe$^{3+}$ chain and a lower one tied to Fe$^{2+}$ chain and the interchain interactions. As shown in the supplementary information, this lower energy mode is weakly dispersive for directions perpendicular to $b$. This is further confirmed by the temperature evolution of the spectra shown in Fig. 3. The interchain interaction was found to be of the order of 0.75 to 1.4 meV, which corresponds roughly to 8 to 15 K. Interestingly, near $T_N = 15$ K, the low energy data shows a collapse of the two modes, giving a single branch. Hence the interchain interactions are phased out by thermal fluctuations, and the only dominant energy scale remaining is the intra-chain coupling between the Fe$^{3+}$ ions. The inelastic signal also still shows a damped “dispersion” up to $2T_N \sim 30$ K, indicating the persistence of short range spin correlations, a behavior characteristic of low dimensional systems [28, 29]. The persistence of short range correlations is consistent with the derived $J_{ch2} = 1.9$ meV~22 K coupling between Fe$^{3+}$ spins. The changes in the spin wave dispersion with temperature supports the energy scales derived from the low-temperature spin wave analysis. The temperature dependence also illustrates the underlying one dimensional nature of RbFe$_2$FeF$_6$.

The noncollinear magnetic structure (illustrated in Fig. 1) brings the possibility for multi magnon states to be observable. In magnets with noncollinear spin structure, cubic anharmonic terms arise in the spin wave Hamiltonian due to the coupling of the transverse and the longitudinal fluctuations associated with deviations of the spin direction perpendicular and parallel to the ordered moment direction. These cubic terms have no analog in collinear magnets and describe the possibility of multi magnon states. Therefore it is likely that the excitations are multi magnon states.

(Fig. 2 (c)) data. As displayed in Fig. 2 (d), the white arrows indicate how the energy position of the different modes allowed the refinement of the anisotropy term for Fe$^{2+}$ and the three remaining exchange parameters. Notably, the anisotropy term affects the position of the higher mode and the slope of this branch is also affected by $J_{ch1}$. As for the flat modes near the zone boundary, their energy position is controlled by the interchain interactions $J_{int1}$ and $J_{int2}$. Figures 2 (e) and (f) show a fit of the spin wave modes with chosen constant $Q$ cuts at the zone center and near the zone boundary, respectively. The best solution found for the anisotropy terms is: $D_α = 0.075$ meV (for the Fe$^{3+}$ site) and $D_β = 0.6$ meV (for the Fe$^{2+}$ site) in agreement with the difference in distortion between the Fe$^{3+}$F$_6$ and Fe$^{2+}$F$_6$ octahedra. The exchange couplings extracted from the fit are $J_{ch1} = 1.40(5)$ meV (Fe$^{2+}$ chain), $J_{ch2} = 1.90(2)$ meV (Fe$^{3+}$ chain), $J_{int1} = 1.40(5)$ meV and $J_{int2} = 0.75(10)$ meV.

![Graphical representation](image-url)
FIG. 3. Inelastic neutron scattering data of RbFe$_2$F$_6$ measured on MERLIN with incident energies of $E_i = 10$ meV (left) and $E_i = 25$ meV (right) along $k$ at 15 K (top), 30 K (middle) and 100 K (bottom).

FIG. 4. (a) Inelastic neutron scattering data of RbFe$_2$F$_6$ measured on MACS with final energy of $E_f = 3.7$ meV along $k$ at 1.5 K. The grey ellipses show the evolution of the resolution ellipsoid as a function of energy along the $k = 1$ cut, calculated with the Reslib library [30]. (b) Two-magnon kinematic conditions calculated in the (E,Q) space (grey dots). The black circles are fits to the experimental data. (c−d) Constant $k = 1$ and $k = 1.5$ cuts; the solid red line and blue dashed line show a fit to the data as described in the text. The grey area shows the energy resolution. (e) Constant E cuts recorded on MERLIN with $E_i = 25$ meV at 5 K.

measured on MACS with the peak of the dispersion illustrated by the solid points in Fig. 4 (b). The grey region in Fig. 4 (b) is the region where the Fe$^{3+}$ spins are kinematically allowed to decay, conserving both momentum and energy, given the constraints of the low-energy branch. Fig. 4 (c−d) show constant -Q scans through the MACS data at the magnetic zone center ($k=1$) and the zone boundary ($k=1.5$). The sharp and intense single magnon excitations are seen at low energies but also an energy broadened component with comparable integrated spectral weight is observed up to high energies of $\sim 9$ meV. This component is also extended in momentum as illustrated in panel (e) and is not associated with sharp single magnon excitations which are resolution limited in energy and momentum. The energy and momentum broadened cross section is not expected based on our single magnon analysis discussed above and the energy and momentum broadened nature indicates a shortened lifetime. The region in momentum and energy that this second component of scattering is observed does coincide with the expected energy and momentum region expected based on two magnons and the lower branch. Based on the broadened cross section and the comparison with calculations discussed above, we therefore conclude that this additional momentum and energy broadened component corresponds to the decay of Fe$^{3+}$ excitations into multiparticle states.

This interpretation of a decay or leakage of Fe$^{3+}$ excitations into a multiparticle continuum is also supported by magnetic diffraction data probing the magnetic structure. Given constraints of the total moment sum rule [33] of neutron scattering, the additional spectral weight appearing in the multiparticle continuum must draw from somewhere else in momentum and energy. As shown in classical, and collinear, Rb$_2$MnF$_4$ [21] and quantum CFTD [20, 34], this spectral weight draws from the elastic channel in localized magnetic systems and this is consistent with the fact that neutron diffraction data reports a strongly reduced ordered moment for the Fe$^{3+}$ site while not for the Fe$^{2+}$. As illustrated in Fig 4 (b) and given the kinematic conditions, the gap and energy range of the lower excitation mode provide favorable conditions to observe the decay of the higher energy Fe$^{3+}$ excita-
tions.

Similar momentum and energy broadened continuum have been reported in quantum \( (S = \frac{1}{2}) \) [35, 36], itinerant magnets [37], and triangular systems [38, 39]. However, the observation of such a strong continuous and decay processes in a classical high spin magnet is unusual given predictions that such cross sections should scale as \( \sim 1/S \) [17]. \( \text{RbFe}^{2+}\text{Fe}^{3+}\text{F}_6 \) is thus a unique case where charge ordering allows the coupling of non-collinear spins oriented 90° to each other and demonstrates that this multi magnon phenomenon is not constrained to purely charge ordered \( \text{RbFe}^{2+}\text{Fe}^{3+}\text{Rb} \) and spin degrees of freedom in \( \text{RbFe}^{2+}\text{Fe}^{3+}\text{Rb} \) nets where similar “orthogonal” or noncollinear spin arrangements exist and may include the oxyselenides and oxysulfides [40–42]. The spin and charge degrees of freedom in \( \text{RbFe}^{2+}\text{Fe}^{3+}\text{F}_6 \) are well separated in terms of iron sites and also energy scales of branches. The multiparticle excitations may provide a means of coupling charge and spin degrees of freedom in \( \text{RbFe}^{2+}\text{Fe}^{3+}\text{F}_6 \) and similar coupling processes have been suggested in BiFeO\(_3\) [43, 44] and low dimensional cuprates [45].

In summary, we report the magnetic fluctuations in charge ordered \( \text{RbFe}^{2+}\text{Fe}^{3+}\text{F}_6 \). The separation of different \( \text{Fe}^{3+} \) and \( \text{Fe}^{3+} \) chains results in an orthogonal spin arrangement on the two different magnetic sites and separate spin-wave branches. We observe multi magnon processes in this magnet and show that such processes can occur in classical magnets with a noncollinear spin arrangement.

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