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Citation for published version:

Link:
Link to publication record in Edinburgh Research Explorer

Document Version:
Peer reviewed version

Published In:
Proceedings of the International Conference on Autonomous Agents and Multi-Agent Systems (AAMAS) 2019

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Learning Plans by Acquiring Grounded Linguistic Meanings from Corrections

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ABSTRACT
We motivate and describe a novel task which is modelled on interactions between apprentices and expert teachers. In the task the agent must learn to build towers which are constrained by rules. Whenever the agent performs an action which violates a rule, the teacher provides verbal corrective feedback (e.g. “No, put red blocks on blue blocks”) and answers the learner’s clarification questions. The agent must learn to build rule compliant towers from these corrections and the context in which they were given. The agent starts out unaware of the constraints as well as the domain concepts in which the constraints are expressed. Therefore an agent that takes advantage of the linguistic evidence must learn the denotations of neologisms and adapt its conceptualisation of the planning domain to incorporate those denotations. We show that an agent which does utilise linguistic evidence outperforms a strong baseline which does not.

KEYWORDS
human-robot interaction; interactive learning; knowledge representation and reasoning

ACM Reference Format:

1 INTRODUCTION
In many commercial scenarios, workers face planning problems that consist of goal conditions that are complex and vaguely specified. For example, these problems are created by Standard Operating Procedures (SOPs)—large manuals containing rules and guidelines for workers performing complex routine tasks. In companies such as Amazon or Ocado they may contain rules such as “make sure the box is properly sealed” or “never put frozen items in the same bag as meat products”.

Developing a formally precise representation of such goal constraints in a planning domain, which supports inference about whether a given state complies with the goals or not, remains a major challenge. This is especially true in scenarios where the SOPs and the vast array of contingencies in which they apply are so extensive that it’s untenable for a domain expert to communicate to a software developer all the ways in which the constraints manifest themselves in all possible domain states. Instead, it is more natural for domain experts to communicate their knowledge by reacting to specific situations—for example, by correcting the learner when they make mistakes. The situation where the learner made a mistake may not have come to mind to the teacher beforehand, or may result from a previous misunderstanding of the learner’s capabilities.

A further challenge regarding SOPs is that they may change in unforeseen ways (this is especially true in bespoke manufacturing and in large online retail companies), making previously irrelevant domain level concepts now become relevant. For example, a company that starts to sell batteries must ensure that labels are put to the left rather than the right of the package containing them (this is a SOP in Amazon (Personal Communication)). However, the agent planning how to pack items for safe shipment may not have the domain level concept of “left” as part of its domain model (since the programmer had not initially identified these concepts as relevant).

In this paper we first present a task which is roughly analogous to, but simpler than, SOP compliant packing. In these scenarios packers must follow instructions which refer to attributes such as weight and fragility (“don’t put heavy things above eggs”, “protect the vase with bubble warp because it is fragile”). Our task takes place in a blocks world and we use colour as a proxy for these concepts (e.g. “put red blocks on blue blocks”).

In the task we assume that agents start out ignorant of not only the goal constraints but additionally starts without a vocabulary for the terms in which the constraints are expressed (in our case, colour words), and does not have a domain model which includes these concepts either. That is, agents must learn to recognise colours from RGB values directly, not simply map words onto a symbolic language.

We present a proof of concept agent that learns to solve the task from the teacher’s corrective feedback, which contains neologisms and ambiguities which the agent must resolve to decode the teacher’s intended message. Working in the blocks world allows us to bypass the complex visual task of learning symbol groundings for abstract words like “heavy” and “fragile” and instead focus on how to model the interaction between (dynamic) symbol grounding, decoding the teacher’s message, and updating goals and planning model given those messages.

We present experiments showing that a language aware agent can learn to solve the planning task in a way that outperforms a strong baseline which does not attempt to make use of the verbal content of corrections.

2 RELATED WORK
As with our task, in Interactive Task Learning (ITL), agents start out with both linguistic and operational capabilities and need to learn through interaction with a teacher. A common approach is for
the teacher and learner to engage in an interactive dialogue where the teacher gives instructions, definitions of words, and answers clarifying questions (e.g. [5, 17, 23, 24]).

A prime example of this is She et al [24], whose agent learns new actions from dialogue. In particular, they use a symbolic planner and goal representation to define what a specific new action should achieve. Our work extends this type of dialogue by allowing a different interaction type, namely correction, instead of just instruction and description. Another major difference is that our goal is to learn a higher level task with constraints, rather than how to perform new actions, as in She et al [24].

Other works have also tackled learning language and tasks from interaction. Wang et al. [27] learns to map language to a symbolic action language from interactions. However, the interactions assume that teacher can click through a number of possible interpretations and select the correct one. They also assume that the agent starts out with a perfect conceptualisation of the domain, while in our task, the agent starts out unaware of domain concepts that are critical to successful planning.

Knox and Stone [10] address a similar hypothesis to ours. They show with FRAMER, which is a framework for learning from “yes/no” feedback, that using human interaction to help guide an agent can make learning policies faster. This hypothesis is also shared by those attempting to learn from advice [18] which has also been shown to improve the speed of policy learning [4, 13]. However, this work mainly focuses on lower level tasks, such as motor control [10, 13], while we tackle higher level planning: finding which sequence of executable actions to perform.

Another method for learning from interaction is Learning from Demonstration (LfD). The majority of this work also concerns learning to perform new skills. However, a small subset of research has focused on learning plans: i.e. when to perform a particular action, as opposed to how to perform it [13, 16, 21]. A significant example is Niculescu and Matric [22] who, like us, exploit correction. The language they use is unambiguous and contains no neologisms. In contrast, in our task the language’s content is hidden and must be inferred, a general and pervasive feature of natural language communication.

Reinforcement Learning (RL) [25] is another popular method for learning planning problems. The goal descriptions we are attempting to learn could be compared to learning a reward function, which is often addressed in conjunction with RL [1, 6] and approaches to learning this reward function with human interaction as evidence exist [6, 8]. However, RL is most useful for calculating expected utilities when action outcomes are stochastic. At this stage we deal with a fully deterministic domain, so we have elected not to use RL (although we may in the future).

Another significant difference from other tasks is the one mentioned earlier: that learning to ground linguistic terms involves adapting the domain model to include newly discovered and unforeseen concepts, rather than simply mapping terms to already known domain concepts (as in [13, 27]).

A significant part of our system is grounding language to their physical denotations. Our approach falls into a group of approaches which trains explicit classifiers for concepts [19]. Our approach shares similarity with, and was partially inspired by, the G3 framework [11, 12, 26], which builds a graphical model to represent an

![Figure 1: The shades used for blocks within each colour category.](image)

instruction. A significant difference between our work and theirs is that they concern themselves only with description, where the system seeks a correct grounding between the language and world, which we tackle correction, where a mismatch between language and world is expected, and finding what that mismatch is leads to interesting inferences.

### 3 THE TASK

The planning problem consists of a goal description $G$ and a set of initial states $S_0$. Each $s \in S_0$ consists of 10 blocks scattered on the table. $G$ entails that these blocks must be in a single tower, and the agent knows this. However, $G$ also entails further constraints that the agent is ignorant of (see below). The agent experiences a state $s \in S_0$ and attempts to build a tower, receiving verbal corrections whenever it performs an action inconsistent with $G$, continuing in this manner until a goal state is reached. This process is repeated for each $s \in S_0$.

The constraints are rules referencing the colour of blocks. Colours can be referred to in terms of their broad colour category, such as red, green, or pink, or using the specific name of the shade, such as maroon, olive, or hot pink (Figure 1 shows the shades we use, chosen from the set of named shades in CSS3). Each rule takes one of two forms, for a pair of colours $C_1$ and $C_2$:

$$r_{(C_1, C_2)} = \forall x. \neg C_1(x) \rightarrow \exists y. \text{on}(x, y) \land C_2(y)$$

$$r_{(C_1, C_2)} = \forall y. \neg C_2(y) \rightarrow \exists x. \text{on}(x, y) \land C_1(x)$$

The teacher expresses both of these rules as “put $C_1$ blocks on $C_2$ blocks”. Throughout the remainder of this text we will keep a running example of “put red blocks on blue blocks” which would have as potential intended message either $r_{(red, \text{blue})}^\text{1}$ or $r_{(red, \text{blue})}^\text{2}$ (which we abbreviate to $r_{(r, b)}^\text{1}$ and $r_{(r, b)}^\text{2}$).

The difference between the rules is which block is constrained. In $r_{(r, b)}^\text{1}$ red blocks are constrained, and need to be on blue blocks but blue blocks can have any colour placed on them. For $r_{(r, b)}^\text{2}$ the blue block is constrained but not the red. This means that for $r_{(r, b)}^\text{1}$ it is possible to build a tower with more blue blocks than red, but this is not true for $r_{(r, b)}^\text{2}$.
Focal stress in spoken language would disambiguate this intended message [15] (e.g., “put RED blocks on blue blocks corresponds to \( r_1^{(r,b)} \) while “put red blocks on BLUE blocks” corresponds to \( r_2^{(r,b)} \). However, in written form this is left ambiguous (and no current speech recognition system accurately estimates focal placement), so the agent must find other means to disambiguate. It should be noted that in constructing goal constraints no restrictions are made on the combination of rules allowed, so both \( r_1^{(r,b)} \) and \( r_2^{(r,b)} \) can be part of the goal description.

The task is implemented in a virtual environment where each scenario is defined in the Planning Domain Definition Language (PDDL) [20]. The agent can interact with the world through the action \( put(x,y) \), which simply places object \( x \) on \( y \). Further the agent only partially observes the current state: it can identify the blocks, their spatial relation on and clear, and it can determine the RGB-values of each block \( x \) (which we denote \( F(x) \)). But the agent is ignorant of how the various RGB values partition into colour concepts, as shown in Figure 1; it also starts out unaware of the available vocabulary of colour terms and must learn these from the teacher.

### 3.1 The Teacher’s Correction Strategy

To succeed in this task our agent exploits evidence supplied by the teacher’s corrective feedback. To do so the agent reasons about the world through the action \( put(x,y) \), which simply places object \( x \) on \( y \). Further the agent only partially observes the current state: it can identify the blocks, their spatial relation on and clear, and it can determine the RGB-values of each block \( x \) (which we denote \( F(x) \)). But the agent is ignorant of how the various RGB values partition into colour concepts, as shown in Figure 1; it also starts out unaware of the available vocabulary of colour terms and must learn these from the teacher.

The two components of the correction strategy are timing (when is a correction given?) and content (what does the teacher say?). The teacher corrects action \( a \) if \( a \) results in state \( s \) such that no sequence of actions consisting of only adding blocks to the tower would satisfy the goal \( G \). The action \( a \) may create such a state \( s \) in two ways, as shown in Figure 2 where the rule being violated is \( r_1^{(r,b)} \); either \( a \) creates a tower where the top two blocks make this rule false (state \( s_1 \) in Figure 2), or there is a block on the table which cannot be placed on the existing tower while satisfying the rule (state \( s_2 \))—in essence, there are no further blue blocks that you can add to the tower so as to put the red block on it. If we consider \( r_2^{(r,b)} \) \( s_2 \) directly violates the rule while in \( s_1 \) there is no place to place the remaining blue block. This means knowing the context and the utterance is not enough to disambiguate between the intended messages.

We assume a corrective strategy where the form of the feedback discriminates whether the situation is like \( s_1 \) or like \( s_2 \) (direct violation or impossibility to place a remaining block). The verbal component of the move is the same regardless (i.e., the verbal utterance \( u \) is “No, put red blocks on blue blocks”, which, as we explained before, is ambiguous between \( r_1^{(r,b)} \) vs. \( r_2^{(r,b)} \). When the tower directly violates the rule the teacher’s multimodal move \( u_1 \) will be uttering \( u \) and pointing to the tower. If a block on the table can no longer be placed in the tower the move, \( u_2 \), is uttering \( u \) and pointing to the block (or one of the blocks) which can no longer be placed.

The agent must use the teacher’s signal \( (u_1 \) or \( u_2) \) to learn to solve the planning problem. We do this by inferring the teacher’s intended message \( M \), given \( u_1 \) (or \( u_2) \) and the knowledge that it corrects action \( a \). If we assume the agent knows the colours of the relevant objects, it would be able to infer with certainty whether \( M = r_1^{(r,b)} \) or \( M = r_2^{(r,b)} \). To see this, consider \( s_1 \) in Figure 2 again and suppose the teacher says \( u_1 \); then by the semantics of correction [3]—i.e., the content of the corrective move \( u_1 \) must be inconsistent with what it corrects— given that you know the top block \( b_1 \) is red and the one beneath it \( b_2 \) is blue, then the message \( M \) that’s meant by \( u_1 \) must be \( r_1^{(r,b)} \) since \( s_1 \) makes \( r_1^{(r,b)} \) false but satisfies \( r_2^{(r,b)} \). This interaction between the context, the signal, and its meaning, given the semantics of correction, is regimented as follows:

\[
\text{Corr}(a, u_1) \leftrightarrow \text{on}(o_1, o_2) \land (M = r_1^{(r,b)} \land \text{red}(o_1) \land \neg \text{blue}(o_2)) \\
\lor (M = r_2^{(r,b)} \land \neg \text{red}(o_1) \land \text{blue}(o_2)) \tag{3}
\]

In a similar fashion, if the speaker uses the multimodal move \( u_2 \), then the semantics of correction constrains the combination of the message \( M \) and the colours of the blocks \( o_1 \) and \( o_2 \) in the tower and the block \( o_3 \) on the table that the speaker points at:

\[
\text{Corr}(a, u_2) \leftrightarrow \text{on}(o_1, o_2) \land (r_1 \land \neg \text{red}(o_1) \land \text{blue}(o_2) \land \text{red}(o_3)) \\
\lor (r_2 \land \text{red}(o_1) \land \neg \text{blue}(o_2) \land \text{blue}(o_3)) \tag{4}
\]

Since our agent starts the learning process unable to classify the colour of any objects, it uses the above constraints (i.e., the mutually known conditions under which a corrective move is coherent) to constrain inference during learning (see Section 4.1).

### 4 METHOD

Our agent solves its task by jointly learning the goal constraints and learning to ground the colour terms referenced in those constraints. Figure 3 gives an overview of the agent. There are two main components: the action selection component senses the world by grounding colour terms and makes use of search and a symbolic planner to find a plan consistent with the agents current estimate of the goal description \( G \). Correction Handling tackles learning from the teacher’s corrective move by making probabilistic inferences to identify the most likely goal constraints and learn to recognise colour terms from RGB values.
Learning from Correction

In the event of a correction the agent generates a probabilistic model capturing the semantics of correction (Equation (3) or (4)). The variables and dependencies in the graphical model represent the relevant logical dependencies of correction semantics and therefore depend on the type of correction (i.e., is it of type $u_1$ or $u_2$?). The models, for $u_1$ and $u_2$ respectively, are shown in Figure 4.

The node $\text{Corr}(a, u_1)$ represents whether the teacher should say $u_1$ given the colour of relevant objects and given the message. Thus

$$P(\text{Corr}(a, u_1) = \text{True} | \text{Red}(o_1), \text{Blue}(o_2), M) = 1$$

(5)

if the right hand side of Equation (3) evaluates to True. Equivalently,

$$P(\text{Corr}(a, u_2) = \text{True} | \text{Red}(o_1), \text{Blue}(o_2), \text{Red}(o_3) \lor \text{Blue}(o_3), M) = 1$$

(6)

if the right hand side of Equation (4) is True. The conditioning set are the variables that appear on the right hand side of these equations. $M$ represents the teacher’s potential intended messages: $\text{i}(r, b)$ or $\text{r}_1(r, b)$. The colour variables $\text{Red}(x)$ and $\text{Blue}(y)$ are binary variables indicating that an object is of that colour (e.g. $\text{red}(o_3)$) or not ($\neg\text{red}(o_3)$). The node $P(\text{Red}(o_3) \lor \text{Blue}(o_3))$ represents the fact that in Equation (4) $o_3$ is either red or blue. The remaining

\[\text{variables, } F(o_1), \text{ represent the visual features of the objects—i.e. the RGB values of the blocks, used since the true colour of blocks is not directly observable.}\]

4.1.1 Correction model. The factored probability distribution the model for $u_1$ in Figure 4 would be:

$$P(\text{Corr}(a, u_1), \text{Red}(o_1), \text{Blue}(o_2), F(o_1), F(o_2), M) = P(\text{Corr}(a, u_1) | \text{Red}(o_1), M, \text{Blue}(o_2))$$

$$P(\text{Red}(o_1) | F(o_1))P(\text{Blue}(o_2) | F(o_2))P(M)P(F(o_1))P(F(o_2))$$

(7)

$P(M)$ and $P(F(o_1))$ are set to be constant which means they will cancel out in the conditional calculations required for updating the goal (Section 4.1.3) and the grounding models (Section 4.1.5).

$P(\text{Red}(x) | F(x))$ and $P(\text{Blue}(x) | F(x))$ are called the grounding models and are learned from the evidence given by the correction (Section 4.1.5).

4.1.2 Grounding. Grounding a particular colour term means accurately predicting $P(\text{Colour}(x) | F(x))$. We estimate this probability using Bayes Rule:

$$P(\text{Colour}(x) | F(x)) = \eta P(F(x) | \text{Colour}(x)) P(\text{Colour}(x))$$

(8)

where

$$\eta = \sum_{i \in \{0, 1\}} P(F(x) | \text{Colour}(x) = i)P(\text{Colour}(x) = i)$$

(9)

We set the prior $P(\text{Colour}(x))$ to 0.5 since the agent has no knowledge about how likely any block is to be, for example, red or not.

We have chosen to estimate $P(F(x) | \text{Colour}(x))$ with weighted Kernel Density Estimation (KDE) (we experimented with Gaussian distributions but found them to perform poorly). Section 4.1.5 shows how this model is updated.

The factor $P(\text{Red}(o_3) \lor \text{Blue}(o_3) | F(o_3))$ is a simple extension of the grounding model, defined in terms of the estimates for $\text{Red}(x)$.
and Blue(x), as shown in (10):

\[ P(\text{Red}(o_3) \lor \text{Blue}(o_3) = \text{red}|F(o_3)) = \frac{P(F(o_3)|\text{Red}(o_3))P(\text{Red}(o_3))}{P(F(o_3)|\text{Red}(o_3))P(\text{Red}(o_3)) + P(F(o_3)|\text{Blue}(o_3))P(\text{Blue}(o_3))} \]  

(10) (sharing likelihood function, P(F(x)|\text{Red}(x)), with P(F(x)|\text{Red}(x)).

4.1.3 Inferring the Goal Constraints. Given the corrections received by the teacher the agent wishes to find the most likely goal description. To begin with the agent only knows that rule constraints exist and the shape they take, further, since it does not know the colours it does not know the full space of possible rules. As the agent learns more colour terms, its hypothesis space of possible rules expands.

When the agent is corrected it uses this evidence to update the possible values of G as well as its (probabilistic) belief about which possibility is most likely. First, it extracts the possible messages M, for example, if the verbal component of the corrective move is u = “no, put red blocks on blue blocks”, then the agent knows that M is $r_1^{(r,b)}$ or $r_2^{(r,b)}$. Further, whichever one the teacher did intend will certainly be part of G.

To keep track of the agent’s belief about which of these rules are in the goal we introduce $R^{(r,b)}$ which represents the four possibilities of whether these rules are in the goal or not:

\[
\begin{align*}
R_1^{(r,b)} &\in G \land R_2^{(r,b)} \in G \\
R_1^{(r,b)} &\in G \land R_2^{(r,b)} \notin G \\
R_2^{(r,b)} &\in G \land R_1^{(r,b)} \notin G \\
R_1^{(r,b)} \notin G \land R_2^{(r,b)} \notin G
\end{align*}
\]  

(11a) (11b) (11c) (11d)

This variable is added when the agent encounters a correction where the possible messages have not been observed previously. That is, the first time the agent encounters u it adds this variable. The agent then keeps track of which goal constraints it believes most likely through $P(R_n^{(r,b)})$ where $n$ represents the number of corrections received with evidence relevant to $R_n^{(r,b)}$ (i.e., corrections where the possible message is $R_1^{(r,b)}$ or $R_2^{(r,b)}$).

When the teacher utters u in response to action a the observed evidence is that $\text{Corr}(a,u) = \text{True}$ and the values of $F(o_1), F(o_2)$, and, optionally, $F(o_3)$ (if the teacher pointed at block o3 on the table). For brevity we define $X = \{F(o_1), F(o_2), \ldots\}$ to be the observed features relevant to the correction at hand.

The agent updates its belief about $R_n^{(r,b)}$ given these observations and its previous belief $R_{n-1}^{(r,b)}$:

\[ P(R_n^{(r,b)}|R_{n-1}^{(r,b)}, \text{Corr}(a,u) = \text{True}, X) \]  

(12)

The main evidence that is relevant to this belief update is the intended message. Since this is not directly observable we marginalise over the possible messages $M = \{R_1^{(r,b)}, R_2^{(r,b)}\}$:

\[
\begin{align*}
P(R_n^{(r,b)}|R_{n-1}^{(r,b)}, X, \text{Corr}(a,u)) &= \sum_{m \in M} P(R_n^{(r,b)}, m|R_{n-1}^{(r,b)}, X, \text{Corr}(a,u)) \\
&= \sum_{m \in M} P(R_n^{(r,b)}|R_{n-1}^{(r,b)}, m) P(m|X, \text{Corr}(a,u))
\end{align*}
\]  

(13a) (13b) (13c)

To calculate $P(M = m|X, \text{Corr}(a,u))$ we use the correction model (Section 4.1.1) marginalising over the colour terms.

To calculate $P(R_n^{(r,b)}|R_{n-1}^{(r,b)}, M)$ we assume conditional independence between the two rules being in the goal given the message:

\[
P(R_n^{(r,b)}|R_{n-1}^{(r,b)}, m) = P(R_1^{(r,b)}|R_{n-1}^{(r,b)}, m) P(R_2^{(r,b)}|R_{n-1}^{(r,b)}, m)
\]  

(14a) (14b)

This independence stems from the overall assumption that there is no restriction on what rules appear together. So, if $R_1^{(r,b)} \in G$ it does not change our belief about if $R_2(r,b) \in G$. The affect of m on the posterior likelihoods of the goal are encapsulated in equations (15) and (16):

\[
P(R_1^{(r,b)} \in G|R_{n-1}^{(r,b)}, m \neq R_1^{(r,b)}) = P(R_1^{(r,b)} \in G|R_{n-1}^{(r,b)})
\]  

(15)

\[P(R_1^{(r,b)} \in G|R_{n-1}^{(r,b)}, m = R_1^{(r,b)}) = 1 \]  

(16)

To calculate $P(R_1^{(r,b)} \in G|R_{n-1}^{(r,b)}, m)$ in Equation (15) we marginalise over the states of $R_{n-1}^{(r,b)}$ where $R_1^{(r,b)} \in G$, i.e., (11a) and (11b):

\[P(R_1^{(r,b)} \in G|R_{n-1}^{(r,b)}) = \sum_{s \in R_{n-1}^{(r,b)}} P(R_n^{(r,b)} = s) \delta(R_1^{(r,b)} = s) \]  

(17)

where $\delta(R_1^{(r,b)} = s) = 1$ if $R_1^{(r,b)} \in s$ is true and 0 otherwise.

On expanding the hypothesis space with a new random variable (which happens at step i, say), we set the prior as in (18) and (19):

\[P(R_1^{(r,b)} \in G|R_{n-1}^{(r,b)}) = 0.01 \]  

(18)

\[P(R_1^{(r,b)} \notin G|R_{n-1}^{(r,b)}) = 1 - P(R_1^{(r,b)} \in G|R_{n-1}^{(r,b)}) \]  

(19)

One consequence of these equations is that given a correction $P(R_1^{(r,b)} \notin G \land R_2^{(r,b)} \notin G \land \text{Corr}(a,u)) = 0$  

which is exactly what is desired, since we know that one of the two messages must be part of the goal.

4.1.4 Updating The Goal. After a correction is given the agent updates what rule constraints are in it’s goal description. Since a correction will only change the belief about rules which are potential messages of that correction this goal update can be made locally. The goal is updated using the most likely state of $R^{(r,b)}$:

\[ G_n = G_{n-1} + \arg \max P(R_n^{(r,b)}) \]  

(21)

where $G \ast e$ represents AGM belief revision [2]. For us, this means that when $\text{argmax} P(R_n^{(r,b)}) = (11b)$ then $R_1^{(r,b)}$ is added to the goal and if $R_2^{(r,b)}$ was previously part of the goal it is removed.

4.1.5 Updating the Grounding Models. To update the likelihood function $P(F(x)|\text{Colour}(x))$ there is no direct labelled data available; rather the agent must exploit predictions from the correction model to estimate how likely it is that an object is a particular colour:

\[ w = P(\text{Red}(o_1) = \text{True}|\text{Corr}(a, u_1), F(o_1), F(o_2)) \]  

(22)

we use w as a label for o1 being red or not, thus creating a new data point $(w, F(o_1))$ for the distribution $P(F(x)|\text{Red}(x)) = \text{True}$. This probability density is estimated using a weighted KDE.
KDE is a non-parametric model which places a kernel around every known data point and calculates the probability of a point by summing over the values at that point. To take into account the weights the sum is weighted by each \( w \) and normalised by the sum of weights. For \( m \) data points \((w_1, x_1), ..., (w_m, x_m)\) this becomes

\[
P(F(x)|\text{Red}(x) = \text{True}) = \frac{1}{m} \sum_{i=1}^{m} w_i \cdot \phi(F(x) - F(x_i))
\]

(23)

Where we use a diagonal Gaussian distribution for the kernel \( \phi \).

### 4.2 Action Selection

To select actions we treat the task as a symbolic planning problem because the scenarios are restricted such that the agent has the requisite motor skills to perform all actions, and the outcome of an action is deterministic. We use what is learned from the steps in Section 4.1 to build the necessary symbolic description. We use the FF planner [9], a PDDL planner which requires a goal and current state description to plan.

The goal is updated as described in Section 4.1.4 and begins as

\[
\forall x. \text{in-tower}(x)
\]

(24)

i.e., the agent defaults to assuming no constraints on towers.

The agent can observe \( \text{on} \) relations and \( \text{clear} \) (required in the preconditions of the put action) so the only part of the state description the agent must estimate probabilistically is the colour of each block.

We predict the probability that each object is a particular colour using the Grounding Models introduced in Section 4.1.2. We define \( S^* \) to be the most likely belief state (over the colours):

\[
S^* = \arg\max_{i \in (0,1)} \sum_{x} \sum_{c} P(C(x) = i|F(x))
\]

(25)

So if we had \( P(\text{red}(o_1) = 1|F(o_1)) = 0.6 \) and \( P(\text{red}(o_2) = 1|F(o_2)) = 0.3 \) \( S^* \) would contain \( o_1 \) as red and \( o_2 \) as not red. If we also had \( P(\text{blue}(o_1) = 1|F(o_1)) = 0.7 \) then \( S^* \) would contain \( o_1 \) as both red and blue, which is acceptable under our framework (this would be an incorrect inference for red and blue but it could be correct if the colours were red and maroon).

Since \( S^* \) is simply a specific belief state and since the grounding models may be incorrect it may be the case that it is impossible to build a rule compliant tower given \( S^* \) and the agent’s current estimate of \( G \). For example, if the rule \( r^{(r,b)}_1 \) is in the goal and there are more red blocks than blue then the planner would not be able to find a plan, since there are not enough blue blocks to place red blocks on. The agent assumes it is possible to build a tower in every scenario, so any inconsistency must be due to errors in the agents estimates.

To ensure that we do find a plan in every situation the agent performs a search over belief states, starting at \( S^* \). The search attempts to find the most likely belief state for which there is a valid plan, maximising:

\[
P(S) = \sum_{c} \sum_{x} P(C(x) = i|F(x))
\]

(26)

where \( C(x) = 1 \) if \( C(x) \in S \) and 0 otherwise.

<table>
<thead>
<tr>
<th>Name</th>
<th>Rules</th>
</tr>
</thead>
<tbody>
<tr>
<td>One Rule</td>
<td>( r_1^{(\text{red,blue})} )</td>
</tr>
<tr>
<td>Maroon</td>
<td>( r_1^{(\text{red,blue})} \ \land \ r_2^{(\text{green,maroon})} )</td>
</tr>
<tr>
<td>Three Red</td>
<td>( r_1^{(\text{red,blue})} \ \land \ r_2^{(\text{pink,red})} \ \land \ r_3^{(\text{purple,red})} )</td>
</tr>
<tr>
<td>Three Rules</td>
<td>( r_1^{(\text{red,blue})} \ \land \ r_2^{(\text{green,yellow})} \ \land \ r_3^{(\text{purple,orange})} )</td>
</tr>
</tbody>
</table>

Table 1: The four planning problems our agents tackled. Each problem varies in the number and identity of rules constraining the goal.

The search begins at \( S^* \) and proceeds to adjacent states by flipping the value of a prediction, for example from \( \text{Red}(x) = 1 \) to \( \text{Red}(x) = 0 \). A priority queue is kept such that the search always explores states with higher scores first.

However, to reduce the size of the search problem we use what we know about the goal constraints to only add adjacent states that move us towards states where it would be possible to find a plan. For example, if we have \( r^{(r,b)}_1 \) then the number of red blocks must be less or equal to the number of blue blocks. Thus, if a state has more red than blue blocks then it will be impossible to find a plan and the relative number must be changed by either increasing the number of blue or decreasing the number of red. The search method adds the highest scoring adjacent states, where one of these changes has been made. In the case where all constraints are satisfied but no plan was found the agent considers random adjacent states.

The search continues until a plan is found or a fixed number of states have been explored. In the latter case, the agent defaults to finding a random plan which builds a tower out of the remaining blocks (ensuring the agent always takes some action).

The actions in the plan are executed in sequence until either the tower is built or a correction is given by the teacher. If the teacher gives a correction the agent performs the steps in correction handling. After this the teacher resets the world state to the state which appeared before the corrected action occurred. This ensure the world is always in a state where it is possible to build a rule compliant tower without removing any blocks from the tower.

### 5 EXPERIMENTS

The purpose of our experiments is to test our Language Agent against a strong baseline which does not make use of language. We wish to show that disambiguating the message and grounding the colour terms is worth it, by showing that this agent learns faster against a strong baseline which does not make use of language. We run the agent through four different planning problems each consisting of 50 scenarios: i.e., 50 distinct initial states. The planning problems vary by what rules are in the goal constraints, Table 1 details what planning problems were used. We report the regret accumulated over these scenarios.
Between each scenario the agent retains all knowledge it has learned so far, specifically, it retains its estimate of $P(R_n | C_i, C_j)$ for all relevant $C_i$ and $C_j$ as well as the grounding models, $P(C_i | F(x))$.

### 5.1 Baselines

We compare our Language Agent to two other agents. The **Naive Agent** is an agent that does not attempt any learning between scenarios. It acts as a lowerbound on how badly an agent could perform. The Naive agent only ensures no corrected action is repeated, for example, if $\text{put}(o_1, o_2)$ was corrected the agent will not perform this action again. Otherwise the agent acts randomly. It retains no knowledge between scenarios.

The **No Language Agent**, the second baseline, attempts to learn the task without making use of the language content of the correction. It only makes use of the teacher’s “no” and the pointing they do. This changes what inferences are available to the agent and therefore what it can learn from correction. Action selection stays largely the same.

Given the correction “no” + *point at tower* for action $\text{put}(o_1, o_2)$ the agent cannot infer enough to create anything resembling the rules in Equations (1) and (2) because the message does not convey which colour terms $C_1$ and $C_2$ are a part of the goal description (since the correction does not convey a positive example of both colours, only one). The only inference the agent can make is that blocks with similar RGB values to $o_1$ cannot be placed on blocks with similar RGB values to $o_2$:

$$\neg \exists x, y, C_{o_1}(x) \land C_{o_2}(y) \land \text{on}(x, y)$$

(27)

The agent adds this rule to its goal state. To identify $P(C_{o_1}(x) | F(x))$ the agent creates a grounding model with a single data point for $P(F(x) | C_{o_1} = 1)$, namely $F(o_1)$.

When the teacher points at $o_2$ the agent does have enough information to construct a rule along the lines of Equations (1) and (2). By pointing at $o_3$ the teacher is saying the block is constrained and cannot be placed any longer. This must mean it is on the left hand side of a rule and that it either must go on $o_2$ or $o_1$ most go on it. In logical form this would be:

$$r_1 = \forall x, C_{o_1}(x) \rightarrow \exists y, C_{o_2}(y) \land \text{on}(x, y)$$

(28)

$$r_2 = \forall y, C_{o_2}(y) \rightarrow \exists x, C_{o_1}(x) \land \text{on}(x, y)$$

(29)

From the available evidence the agent cannot make a decision about which rule is correct. To make an informed decision the agent will attempt to break one of the rules and observe how the teacher reacts. The agent attempts to break (28) by finding the object $o_4$ most dissimilar to $o_3$ and place it on $o_2$. If the teacher corrects this action then (28) is most likely the rule, otherwise it is (29).

Making use of these inferences allows the agent to build up a goal which will solve the task without disambiguating the language or performing language grounding. Between scenarios the agent retains its current estimated goal description and the distributions $P(F(x) | C_{o_1}(x))$.

### 5.2 Results

Figures 5–8 show the cumulative regret for each planning problem. Our Language agent outperforms the two baselines in all cases. The No Language agent performs much better than the Naive agent, showing that outperforming it is meaningful. In most problems our Language Agent has learned to act near perfectly (indicated by the the reward curve eventually going flat), while the No Language agent has only achieved this in the simplest, One Rule, planning problem. This seems to support our belief that benefiting from generalisations expressed in language outweigh the cost incurred by having to disambiguate the that language and ground the colour terms.

Further, we would expect the generalisations that language can express to be especially valuable if there is an overlap between the rules; that is, if there is a colour which is used several times in different rules, since the Language agent would be able to more quickly generalise by using the overlapping colour. We test this by comparing the Three Rules to the Three Red problem. In the Three Red problem all three rules contain “red” as one of the relevant colours. Given this, we would expect the linguistic agent to be able to more quickly learn as it does not need to learn as many colours, while the No Language agent has no way of detecting the overlap.

In Figure 7, where three different rules contain the word “red”, we do indeed see that there is a significant difference between the speed in which the Language agent has learned. This is especially clear when comparing to the Three Rules problem, in Figure 8. Here we see that the Language agent is having much more trouble learning the problem and is much closer to the No language agent in performance.
However, speedier learning is not the only benefit we get from the Language agent. The resulting domain model the agent has learned is highly interpretable. The goal description is human readable, for example, inspecting the learned goal for the One Rule problem we found that the agent has in fact learned \( r_1(r, b) \in \mathcal{G} \). This is not true for the No Language agent where the goal consists of 25 different rules referencing meaningless terms such as \( C_{15} \) (which could only be made more meaningful by inspecting the data points in its grounding model). Further, since the Language agent learns colour terms these could be used for other types of communication with humans. For example, the agent could easily interpret the command “pick up a red block”, given sufficient knowledge of the other words in the sentence. Therefore this would fit well with an ITL system which attempts to learn further tasks and actions.

6 CONCLUSION

In this paper we presented a novel task, where an agent learns a set of constraints from a teacher who verbally corrects the agent when it performs actions that violate the constraints. Additionally, we present an agent that exploits the semantics of correction to learn the previously unknown constraints and how to ground colour terms in RGB values. Our agent consistently out-performs baseline systems which do not make use of language.

The results are encouraging, showing that using coherence relations can be a useful tool for joint task and language learning. That being said, this work represents a proof-of-concept as we make several simplifying assumptions in the domain, which makes the current approach unsuitable to be tested “in the wild”.

We will discuss two main directions that must be addressed when extending to a more general setting. The world the agent inhabits and the interactions with the teacher would need to be made richer. Dealing with a richer world would require more sophisticated visual processing and reasoning about uncertain outcomes. Dealing with richer interactions requires more sophisticated ways of computing possible messages from language, a wider coverage over different types of interaction, and reasoning over ambiguity and uncertainty in the teacher’s messages and strategy. To interact with real humans we would also have to be conscious of the patience of the teacher, as long wait times between interactions or the need for many repetitions would cause them to become fed up.

In the current system the main bottle-neck as far as speed of learning is learning to ground the colour terms. If we move to closer to a real world domain this is likely to be compounded as we are limited by the current state-of-the-art in visual processing, which requires models that require in the order of thousands of examples to learn. The most promising solutions to this would be to use pre-trained models and adapt them through one-shot or few-shot learning methods [7, 14], perhaps by using linguistic definitions as in [23]. We believe the method we are using to update the parameters of the grounding models is flexible enough to be integrated with a large class of visual processing systems. For this reason we are less concerned with dealing with more complex visual scenes, as we don’t aim to extend the state-of-the-art in visual processing.

We are more interested in exploring richer interactions with the teacher. In our future work we plan on relaxing assumptions made on the strategy of the teacher, extend the set of constraints the agent learns, and expand the way in which the agent and teacher interact.

ACKNOWLEDGMENTS

We would like to thank EPSRC for funding Mattias Appelgren, Ram Ramamoorthy and Yordan Hristov for helpful advice and discussions, and three anonymous reviewers for very helpful feedback. All errors that remain are our own.

REFERENCES
