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The Ins and Outs of Cyclical Unemployment

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Abstract

A dominant trend in recent modeling of labor market fluctuations is to treat unemployment inflows as acyclical. This trend has been encouraged by influential recent papers that stress the role of longer unemployment spells, rather than more unemployment spells, in accounting for recessionary unemployment. After reviewing an empirical literature going back several decades, we apply a convenient log change decomposition to Current Population Survey data to characterize rising unemployment in each postwar recession. We conclude that a complete understanding of cyclical unemployment requires an explanation of countercyclical inflow rates, especially for job losers (layoffs), as well as procyclical outflow rates.

In principle, the increased unemployment during a recession could arise from an increase in the number of unemployment spells, an increase in the duration of unemployment spells, or both. Equivalently, one can decompose the cyclical variation in unemployment into changes in the rates of inflow to and outflow from unemployment. The title of a 1986 paper by Michael R. Darby, John C. Haltiwanger, and Mark W. Plant (1986) dubbed this subject “The Ins and Outs of Unemployment.” Because Darby et al. claimed that cyclical unemployment variation in the United States stems almost entirely from cyclical variation in the inflow, their paper’s subtitle was “The Ins Win.”

Contrary to that conclusion, one of the strongest trends in recent macroeconomic modeling of the labor market is to treat the inflow to unemployment as acyclical. In some instances, acyclicality of the inflow is assumed; in others, the model is designed to explain the supposed acyclicality of the inflow. Examples include Robert E. Hall (2005a, 2005b), Mark Gertler and Antonella Trigari (2006), Julio J. Rotemberg (2006), Olivier Blanchard and Jordi
Gali (2006), Christian Haefke and Michael Reiter (2006), and Leena Rudanko (2008). Several of these authors motivate their treatment of the inflow as acyclical by referring to papers by Robert Shimer (2005a, 2005b) and Hall (2005b, 2006), which reach a conclusion diametrically opposite to that of Darby et al. For example, the introductory passage in Shimer’s (2005a) paper “Reassessing the Ins and Outs of Unemployment” declares, “Using United States data from 1948 to 2004, I find that there are substantial fluctuations in unemployed workers’ job finding probability at business cycle frequencies, while employed workers’ separation probability is comparatively acyclic.”\(^1\) Similarly, the abstract of Hall’s (2005b) Review of Economic Statistics Lecture says, “In the modern U.S. economy, recessions do not begin with a burst of layoffs. Unemployment rises because jobs are hard to find, not because an unusual number of people are thrown into unemployment.”

By 2006, several new manuscripts, including early drafts of the present paper,\(^2\) reexamined the evidence on unemployment flows and disputed Shimer and Hall’s already-influential conclusion that cyclical inflows are unimportant. Accordingly, the abstract of the 2007 revision of “Reassessing the Ins and Outs of Unemployment” acknowledges that, since 1948, the inflow rate has accounted for one-quarter of the variation in the unemployment rate. The new abstract, however, goes on to declare, “Fluctuations in the employment exit probability are quantitatively irrelevant during the last two decades.”

Viewed in the context of a longer history of unemployment studies, the opposite conclusions of Darby et al. and of Shimer and Hall both seem surprising. Darby et al.’s finding

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\(^1\) Shimer (2005a, 2005b) uses the term “separation probability” to mean the probability of entering unemployment. We do not use this terminology for two reasons. First, we wish to avoid confusion with the more commonly used meaning of “separation” as a quit or layoff from a particular employer, which often involves no unemployment at all (especially in the case of quits). Second, as we will emphasize in section I.D of this paper, many spells of unemployment begin with entry into the labor force, not a separation from employment.

\(^2\) See also Helge Braun et al. (2006), Eran Yashiv (2008), and Shigeru Fujita and Garey Ramey (forthcoming).
that “The Ins Win” and the outs lose appears to be contradicted by a large body of accumulated evidence suggesting that unemployment duration is substantially countercyclical:

- Regularly published statistics on the cross-sectional distribution of unemployment duration from the monthly Current Population Survey (CPS) show a pronounced shift towards longer unemployment spells during recessions. Similarly, sophisticated econometric analyses that have used repeated CPS cross-sectional data on unemployment duration to impute month-to-month hazard rates for exiting unemployment have found these outflow rates to be substantially procyclical (Hal Sider, 1985; Michael Baker, 1992).

- Numerous studies have estimated inflow and outflow rates with the so-called gross flows data, which are based on the two-thirds or so of the CPS sample that can be longitudinally matched from one month to the next. Without exception, these studies have found that the monthly hazard rate for outflow from unemployment is procyclical (George L. Perry, 1972; Stephen T. Marston, 1976; Blanchard and Peter Diamond, 1990; Hoyt Bleakley, Ann E. Ferris, and Jeffrey C. Fuhrer, 1999; Yashiv, 2008; Fujita and Ramey, forthcoming).

- Regularly published statistics on unemployment insurance (UI) claims show that, during recessions, UI claims tend to be of considerably longer duration, and the fraction of claimants that exhaust their entitlement to benefits is considerably higher (Walter Nicholson, 1981; John Kennan, 2006). These facts, of course, are precisely why the federal government usually adopts extended-benefit programs during recessions.

Shimer and Hall’s opposite conclusion that the outs win and the ins lose also appears to be contradicted by a great deal of evidence:
The regularly published CPS statistics on unemployment duration show that the number unemployed less than five weeks (who therefore became unemployed since the previous month’s CPS) tends to be substantially higher during recessions.

The same studies of CPS gross flows data that have found procyclical hazard rates for exiting unemployment also have found substantially countercyclical flows into unemployment. Most recently, for example, Fujita and Ramey (forthcoming) estimate that countercyclical inflows account for 40 to 50 percent of cyclical variation in unemployment.3

Several studies (Darby et al., 1986; Steven J. Davis, 1987; Blanchard and Diamond, 1990; Joseph A. Ritter, 1993) have noted that, although the hazard rate for exiting unemployment is procyclical, the number exiting unemployment is countercyclical. As explained by Blanchard and Diamond (1990, p. 118), “While the flow from unemployment to employment increases in a recession, the hazard rate decreases as the pool of unemployed increases proportionately more than the flow.” Davis (2006) shows that this can occur only if the inflow to unemployment is substantially countercyclical.

Regularly published statistics on initial UI claims show that dramatically more UI claims are initiated during recessions, especially early in recessions (Kennan, 2006). This, of course, is why the Conference Board uses initial UI claims as one of its “leading indicators.”

All these indications of countercyclical inflows into unemployment dovetail with well-established facts about labor turnover, including the recent employer-based evidence on

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3 Although Shimer (2007) emphasizes the evidence from repeated cross-sections of the CPS, section 2 of his paper also analyzes the gross flows data. The results in his table 2 suggest that countercyclical inflows account for about one-third of cyclical unemployment variation over the 1967-2007 period and about 20 percent over 1987-2007. These findings, however, are not reflected in Shimer’s abstract, introduction, or conclusion.
countercyclical job destruction as well as a long history of evidence that layoffs are strongly countercyclical (Peter S. Barth, 1971; Davis, R. Jason Faberman, and Haltiwanger, 2006).4

Reacting to the apparent discrepancy between these patterns and Shimer and Hall’s influential conclusion, in this paper we reexamine the evidence from repeated cross-sections of the CPS. Yashiv (2008) and Fujita and Ramey (forthcoming) have recently reexamined the evidence from the CPS gross flows data, but published time series data from CPS cross-sections are the basis for the evidence that Shimer (2005a, 2005b, 2007) emphasizes and describes as his “preferred measures” (2007, p. 1). One advantage of using that publicly available information, as Shimer (2007, pp. 2-3) says, is “making it easy for others to verify my results, extend them as more data becomes available, and examine their consistency both within the United States and across countries.” In addition, the gross flows data are subject to a number of drawbacks, including the systematic exclusion of individuals who change residence and the many spurious transitions generated by misclassification of labor force status in either of the months used in the longitudinal match (National Commission on Employment and Unemployment Statistics, 1979, pp. 214-17; Anthony J. Barkume and Francis W. Horvath, 1995). We therefore consider it worthwhile to examine both types of evidence. As it turns out, our findings and those of gross flows studies like Yashiv (2008) and Fujita and Ramey (forthcoming) are qualitatively similar. It is useful and reassuring to find that both slices of the CPS data yield similar answers.

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4 As noted by Hall (2006), the countercyclicality of layoffs is no greater than the procyclicality of quits. This point was previously documented by Sumner H. Slichter (1919), W. S. Woytinsky (1942), George A. Akerlof, Andrew K. Rose, and Janet L. Yellen (1988), Patricia M. Anderson and Bruce D. Meyer (1994), and others. Despite the well-known ambiguities in the measurement and interpretation of layoffs versus quits, the two types of separations display large systematic differences in their cyclicality and in the associated incidence of unemployment and changes in earnings. Davis (2006) gives a detailed explanation of why distinguishing layoffs from quits is important for understanding cyclical fluctuations in the labor market.
Section I of our paper takes Shimer’s analysis of the published CPS series as our point of departure. In section I.A, we describe a remarkably simple but useful way of decomposing unemployment variation into parts associated with logarithmic changes in the hazard rates for flowing into and out of unemployment.\(^5\) In section I.B, we apply that decomposition to the CPS time series data. Like many previous researchers, we find that much or most of cyclical unemployment variation can be attributed to cyclicality in the outflow hazard, but we also find an important role for inflows, especially in the most severe recessions. In section I.C, we propose and implement modifications of Shimer’s methods of correcting for the 1994 CPS redesign and time aggregation bias. These refinements reconfirm our finding of substantial cyclicality in both inflow and outflow rates.

In section I.D, we consider heterogeneity in flow rates across job losers, job leavers, and labor force entrants. This exercise reveals stark differences in the cyclical properties of the three inflow hazards. The job loser inflow to unemployment is clearly countercyclical, displaying prominent upward spikes in all recessions. By contrast, the job leaver inflow rate is prominently procyclical and the inflow from non-participation is comparatively acyclical.

In light of these findings, in section II we caution against the recent tendency of macroeconomic theorists to overlook the cyclicality of unemployment inflows. A complete understanding of cyclical unemployment requires an explanation of countercyclical

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5 The basic idea dates back to Hyman Kaitz’s (1970) seminal work on unemployment duration. He notes that “small percentage changes in the unemployment rate from one period to another are approximately equal to the sum of the percent changes in the number of new spells and in the length of the average spell” (p. 14). To our knowledge, the 2006 draft of our paper was the first attempt to use the log change decomposition for systematic analysis of the contributions of the flow hazard rates to cyclical unemployment. This decomposition has subsequently been adopted by Fujita and Ramey (forthcoming), who use our equation (3) formulation, and Christopher A. Pissarides (2007), who uses our equation (4) version. Pissarides appears to have been aware of the result at an earlier date. Page 505 of his 1986 *Economic Policy* paper on unemployment and vacancies in Britain says, “The two series for the flow rates are plotted in Figure 1 on a logarithmic scale: what matters for changes in the unemployment rate are proportional changes in the flow rates.” More recently, Dale T. Mortensen and Eva Nagypal (2005) use the result to explore the theoretical implications of exogenous shocks to job destruction in the context of the search model.
unemployment inflow rates (especially for job losers) as well as procyclical outflow rates. We also pose the question of what can be learned about the economics of the business cycle from performing purely mechanical decompositions of cyclical unemployment variation into inflow and outflow components. We explain why some of the cyclical variation in the outflow hazard may be caused by cyclical changes in the size and composition of the inflow, and we suggest more generally that the choice and interpretation of decomposition methods ultimately must depend on the economic models being considered.

I. An Analysis of Published Time Series from the Current Population Survey

A. Some Useful Identities

Shimer (2007) and Hall (2005b) start with the following description of the evolution over time of the number unemployed:

\[ \frac{du}{dt} = s_t (l_t - u_t) - f_t u_t = -(s_t + f_t)(u_t - u^*_t) \]

where \( l_t \) and \( u_t \) are the labor force and unemployment stocks respectively, \( u^*_t \) is steady state unemployment, and \( s_t \) and \( f_t \) are the unemployment inflow and outflow hazard rates. It should be mentioned at the outset that equation (1) accurately describes the evolution of unemployment only if all inflows into unemployment originate from employment. In fact, however, around 40 percent of the stock of unemployed workers report that their unemployment originated from non-participation in the labor force. We will address this issue in detail in section I.D, but for now we maintain Shimer and Hall’s simplifying assumption.

The focus of interest, then, is on the two flow rates \( s_t \) and \( f_t \). As many previous studies have shown, and as we will confirm, since \( (s_t + f_t) \) is typically close to 0.5 on a monthly basis, the half life of a deviation from steady state unemployment is close to one month. In other words,
the evolution of the actual unemployment rate, which we denote $\tilde{u}$, is closely approximated by
the steady state unemployment rate:

$$
\tilde{u}_t \equiv \frac{u_t}{l_t} \approx \frac{u^*_t}{l_t} = \frac{s_t}{s_t + f_t}
$$

In what follows, a recurring theme will be the decomposition of changes in the observed
unemployment rate into a contribution due to changes in the inflow rate and a contribution due to
changes in the outflow rate. It turns out that equation (2) provides us with a remarkably simple
decomposition. In particular, log differentiating of (2) yields

$$
d \log \tilde{u}_t \approx (1 - \tilde{u}_t) \left[ d \log s_t - d \log f_t \right]
$$

Equivalently, multiplying (3) through by $\tilde{u}_t$ yields

$$
d \tilde{u}_t \approx \tilde{u}_t (1 - \tilde{u}_t) \left[ d \log s_t - d \log f_t \right]
$$

Expressed in either way, the equation provides a decomposition in which the
contributions of the inflow and outflow rates are separable and may be compared on an equal
footing with respect to their impact on the unemployment rate. To obtain a transparent view of
the relative contributions of the inflow and outflow rates, all one need do is compare the log
variation in the two rates.6

B. Evidence from CPS Time Series Data

As noted by Shimer, a significant virtue of his methodology is the ease of its replication.
In this spirit, we use the same, publicly available, seasonally adjusted CPS data on the number

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6 Of course, equations (3) and (4) hold as equalities only for infinitesimal changes. For discrete changes, they are
only approximations. Fujita and Ramey’s (forthcoming) regression-based estimation of our log change
decomposition verifies that it works well for discrete changes, in the sense that the estimated components come
remarkably close to summing to 1.
employed, the number unemployed, and the number unemployed less than five weeks (henceforth “short-term unemployment”) for each month from 1948 through 2004.\footnote{These data are readily obtained from the Bureau of Labor Statistics website, www.bls.gov.}

Shimer’s analysis involves two corrections to these time series. First, as discussed by Anne E. Polivka and Stephen M. Miller (1998) and Katherine G. Abraham and Shimer (2001), the 1994 redesign of the CPS changed the way the survey measures unemployment duration for all of the survey’s eight “rotation groups” except the first and fifth.\footnote{In the CPS sample design, an address selected into the sample remains in the sample for four consecutive months, is temporarily rotated out of the sample for eight months, and then is rotated back in for four more months before being permanently retired from the sample. The first and fifth rotation groups are respectively the addresses in the survey for the first time and those reentering after the eight-month hiatus. The crucial change in the 1994 redesign was that, in all rotation groups except the first and fifth, unemployed individuals who also were unemployed as of the previous month’s interview were no longer asked about their unemployment duration. Instead, their unemployment duration was measured as the previous month’s value incremented by the number of weeks between the two monthly interviews.} The resulting reduction in the number counted as short-term unemployed induced a discontinuity in the series. Shimer’s main method of correcting for the discontinuity is, in each month from 1994 on, to inflate the official count of short-term unemployment by that month’s ratio of the short-term share of unemployment in the first and fifth rotation groups (obtained from the CPS microdata) to the short-term share for the full sample. Equivalently, he multiplies the official count of all unemployment by the short-term share in only the first and fifth rotation groups. This treats the discontinuity because, even since 1994, the first and fifth rotation groups’ unemployment duration has been measured in the same way as the full sample’s was before 1994. In this section’s replication, we use Shimer’s correction method, but in section I.C we will implement a variation of the method that we believe is even better.

Second, instead of just using the monthly time series to calculate monthly transition rates, Shimer devises an ingenious way of inferring continuous-time inflow and outflow hazard rates, $s_t$ and $f_t$. Inferring the outflow hazard rate is relatively straightforward. First calculate the
probability that a typical unemployed worker leaves unemployment in the month between consecutive CPS surveys, \( F_t \), using the identity

\[
(5) \quad \Delta u_{t+1} = u_{t+1}^* - F_t u_t
\]

where \( \Delta u_{t+1} \) is the monthly change in the number unemployed between month \( t \) and month \( t + 1 \), and \( u_{t+1}^* \) is the number unemployed less than five weeks in month \( t + 1 \). Thus, the monthly outflow probability is given by

\[
(6) \quad F_t = 1 - \left[ \frac{(u_{t+1} - u_{t+1}^*)}{u_t} \right].
\]

This can then be mapped into the outflow hazard, \( f_t = -\log(1 - F_t) \).

Inferring the inflow hazard is more difficult. The reason is that some workers who flow into the unemployment pool after one month’s CPS also exit unemployment before the next month’s survey. As a result, the measured stock of short-term unemployed workers in any CPS is in fact an underestimate of the number of workers who flowed into the unemployment pool over the course of the preceding month. The latter is what Shimer refers to as time aggregation bias.\(^9\)

To correct for time aggregation bias, Shimer solves (1), the differential equation for the evolution of the unemployment rate, forward one month under the assumptions that the flows, \( s_t \) and \( f_t \), and the labor force, \( l_t \), are constant between surveys:

\[
(6) \quad u_{t+1} = u_t^* + (u_t - u_t^*) \exp[-(s_t + f_t)]
\]

Since we obtain a measure of the outflow rate \( f_t \) from the method above, and since we observe \( u_t \) and \( u_{t+1} \), the unemployment rates at the beginning and end of the month, we can solve (6) for the inflow hazard \( s_t \).

---

\(^9\) Note that there is no analogous time aggregation problem in the measurement of unemployment outflows due to unemployed workers leaving unemployment and re-entering between CPS surveys. The reason is that the CPS in theory picks up all such workers, as they will be measured as unemployed less than five weeks.
Following this method provides us with measures of the inflow and outflow rates for each month from 1948 through 2004. As a final step, to obtain what Shimer refers to as his preferred measures of unemployment inflow and outflow rates, we take quarterly averages of these monthly series to obtain smoother series.

In our figure 1 we replicate Shimer’s figure 1 and display the quarterly time series of the probabilities of flowing in or out of unemployment over the course of a month. To the untrained eye, figure 1 might give the impression that the cyclical variation in the inflow to unemployment is dwarfed by the variation in the outflow from unemployment. However, a key lesson from equations (3) and (4) in our section I.A is that a more apt comparison is between the variation in the logarithms of the inflow and outflow hazard rates. Figure 2 displays these log flows. Note that, since the range of the vertical axes measuring these two log flows is the same, equal-sized variation in either plot will have an equal-sized impact on the unemployment rate.

Inspection of figure 2 reveals substantial variation in log inflow rates in all recessions except the two most recent (the relatively mild 1990 and 2001 recessions). Thus it is by no means clear that the inflow rate into unemployment is, in Shimer’s words, “comparatively acyclic” relative to the outflow rate, except in these recent recessions.

A natural question at this point is what fraction of the increase in unemployment during a recession is due to increases in the inflow rate into unemployment, and what fraction is due to declines in the outflow rate? Thanks to the decomposition presented in section I.A, such a question is straightforward to answer. We first identified start and end dates for the unemployment ramp-up in each recession from 1948 on.\textsuperscript{10} We then calculated the difference in

\textsuperscript{10} In practice, the start dates were determined by the most recent minimum quarterly unemployment rate preceding each NBER recession start date, and the end dates by the highest quarterly unemployment rate following each NBER recession end date. The NBER recession dates were not used as their focus is not on recessionary
the log inflow rate and log outflow rate relative to their start-of-recession values for each recession in turn. Figure 3 plots the change in the log inflow rate and the negative of the change in the log outflow rate for each quarter of each recession since 1948. As indicated in equation (3), these two quantities multiplied by 1 minus the unemployment rate give an approximate accounting for the change in the log of the unemployment rate.

Figure 3 reveals a number of insights. First, consistent with the results of Shimer and many others, we observe that the outflow rate from unemployment fell in most recessions by about 30 to 50 log points. Thus, variation in the outflow rate from unemployment is a crucial aspect of cyclical unemployment. And it is true that the outflow rate explains the majority of the cumulative peak-to-trough rise in unemployment over the cycle, with a greater relative impact later on in a recession.

However, figure 3 confirms that inflow rates also have played a substantial role in generating cyclical unemployment historically. In particular, we observe that the inflow into unemployment typically rose by around 20 to 40 log points from peak to trough, except in the last two recessions. We also observe that the effects of inflows tend to be strongest at the start of recessions, in contrast to the effects of the outflow rate. Thus, graphed in an appropriate metric, the data show that, until the two recent recessions, there was something like a 35:65 inflow/outflow split of the overall increase in unemployment, with relatively more weight on inflows earlier on and outflows later on in a recession. Thus, Shimer’s (2005b, p. 493) influential published claim that the inflow rate is “nearly acyclical” is an overstatement at best.

unemployment, but rather principally on GDP growth, and they thereby miss a large portion of the cyclical ramp-up in unemployment. Figure 0 displays these dates along with the time series for the unemployment rate.

11 For both outflows and inflows, the changes in log points appear small in the major recession period of the early 1980s because we break the period into two separate recessions.
Figure 3 also highlights the difference in unemployment patterns between the last two recessions and the many prior recessions. In the last two recessions, especially the one of the early 1990s, aggregate inflows into unemployment moved comparatively little. These weak aggregate inflow effects appear to be a feature of these last two recessions rather than a stylized fact of recessionary unemployment as a whole. In any case, in the next two sections, we shall see reasons to question figure 3’s depiction of the most recent recessions. In section I.C, we shall see that the apparent weakness of inflow effects in the 2000/01 recession varies with the method of correcting for the CPS redesign. And our disaggregate analysis in section I.D will reveal that the aggregate picture presented in figure 3 masks some important heterogeneity in the effects of different inflow rates for different sub-groups of the unemployed. In the end, the inflow effects in the last recession will not look so different from those in prior recessions.

C. Alternative Corrections for the CPS Redesign and Time Aggregation Bias

To this point, we have followed Shimer’s methods of correcting the published CPS data for the effects of the CPS redesign and time aggregation. We agree that corrections are called, but we think the methods can be improved on. In this section, we propose refinements of the correction methods and present the results from applying them.

As mentioned above, to treat the discontinuity in the short-term unemployment series induced by the 1994 CPS redesign, Shimer multiplies the official unemployment count in each month from 1994 on by the month’s short-term share of unemployment for only the first and fifth rotation groups, whose unemployment duration measurement was unaffected by the redesign. As Shimer acknowledges in his appendix, a drawback of this approach is that it bases each month’s estimated short-term share on only about one-quarter of the unemployed in the
CPS sample and therefore multiplies the sampling variance of the estimate by about four. The resulting noise in the corrected series can make it more difficult to discern the true cyclical variation in unemployment flows since 1994. This noise from sampling error would get worse still in our section I.D, when we disaggregate the unemployed into job losers, job leavers, and labor force entrants.

An alternative approach that can yield a more stable corrected series for short-term unemployment over the post-redesign era is to multiply the official short-term unemployment series by the era’s average of the ratio of the short-term share for the first and fifth rotation groups to the full sample’s short-term share. Our analysis of CPS microdata from February 1994 (the first month that unemployment duration was measured in the new way for all rotation groups except the first and fifth) through January 2005 finds an average ratio of 1.1549. We therefore produce a less noisy post-redesign series by simply multiplying the official short-term unemployment by 1.1549 in each month from February 1994 on.\(^\text{12}\)

To get a sense of the practical difference between Shimer’s and our methods of correcting for the CPS redesign, figure 4 plots the month-by-month scaling factor used by Shimer, together with our scaling factor. It can be seen that the month-by-month correction factor displays considerable volatility and little obvious systematic trend around our correction factor of 1.1549.

Figure 5 displays the effects of our alternative redesign correction on the decomposition of cyclical unemployment in the last recession, along with the previous five recessions by way of comparison. It can be seen that our less noisy correction for the 1994 redesign reveals a substantially more pronounced effect of the inflow rate in the 2001 recession. In particular, the

\(^{12}\) In footnote 27 of his appendix, Shimer (2007) mentions an analysis in which he multiplied the post-redesign short-term unemployment by a constant factor of 1.10, but he does not explain his choice of 1.10. Statistics he reports in his appendix seem to indicate that 44.2/37.9=1.166 would be a more appropriate choice. Based on different information from the CPS “parallel survey,” Polivka and Miller (1998) suggest an even higher correction factor of 1/.830 = 1.205.
inflow contribution in the last recession no longer looks so different from the inflow contributions in some of the earlier recessions.

The second correction to the CPS data seeks to avoid the time aggregation bias that would result from missing unemployment spells that begin after one month’s CPS and end before the next month’s survey. As explained in our section I.B, Shimer’s approach is to impute continuous-time hazard rates for the unemployment inflow. An alternative approach, pioneered by Kaitz (1970) and Perry (1972), is to impute discrete weekly hazard rates. One advantage of the latter approach is that, unlike the continuous-time method, it is consistent with the discrete weekly nature of the CPS labor force definitions. Each month’s CPS interviews take place during the week containing the 19th of the month, and the labor force questions pertain to the “reference week” containing the 12th. Someone who works at any time during the reference week is counted as employed. Thus, contrary to the assumptions of the continuous-time correction method, a worker who loses her job partway through the reference week would not be counted as unemployed in the CPS data.

More fundamentally, it is not clear whether the process governing transitions into and out of unemployment should be viewed even theoretically as a purely continuous-time process. If a particular worker surveyed in the CPS were to quit one job effective 5:00 pm. on Wednesday of the reference week and start a new job at 9:00 a.m. the next day, a continuous-time approach would regard that worker as unemployed every instant between those two times. Not only would the official CPS classification scheme judge otherwise; we suspect that most readers would as well. This is not to say that the official definition or, for that matter, any other specific classification scheme is clearly correct. What if the worker who quit at 5:00 on Wednesday chose not to start her new job till Friday or Monday? Would she be unemployed while between
the two jobs? The official definition (and, we suspect, at least some readers) would say no. Other readers might say yes.13

Our reaction to the inescapable ambiguity is to check what happens to the results based on the continuous-time correction if instead we use discrete weekly hazard rates. The details of our approach are in our appendix. Similarly to Shimer’s correction, ours boils down to the solution to a non-linear equation in the weekly inflow probability $s^w_t$, and the weekly outflow probability, $f^w_t$:

\[
U_{t+1} = U^w_t + (U_t - U^w_t)(1 - s^w_t - f^w_t)^4
\]

where $U^w_t$ is the steady-state weekly unemployment stock.

Figure 6 illustrates both the discrete-time and continuous-time corrected log inflow hazard rates, along with the uncorrected inflow rate for comparison.14 As expected, both aggregation bias corrections raise the level of estimated inflow rates, since they seek to add back on inflows that subsequently exited unemployment between survey dates. In particular, the continuous-time correction increases the level of the measured inflow rate by about 30 log points, while the discrete-time correction does so by around 23 log points. Thus, the continuous-time correction arguably over-corrects for time aggregation bias in the sense that it imputes short unemployment spells that the official statistics would not recognize as unemployment spells even if the CPS took place every single week.

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13 The latter readers might prefer a hybrid correction method that views the flow process as a purely continuous-time process, but recognizes that the CPS statistics are based on definitions using a weekly interval. Developing and implementing such a correction would be a worthy project for future research, but we have not pursued it here because it turns out that our discrete-time correction does not dramatically alter the conclusions about the contributions of inflow and outflow rates.

14 To isolate the effects of the alternative corrections for time aggregation bias, all the series plotted in figure 6 use our correction for the 1994 redesign.
In addition, figure 6 reveals that, since the aggregation bias corrections raise the level of estimated inflow rates, they reduce the log change in the inflow rate over the cycle. Simple least squares regressions of corrected log inflow rates on the uncorrected log inflow rate reveal coefficients of 0.78 for the continuous-time correction and 0.85 for the discrete-time correction, consistent with the notion that correcting for aggregation bias limits the capacity for inflows to explain cyclical unemployment. The latter also reveals that, because the weekly correction affects the inflow level to a lesser extent than the continuous-time correction, it also preserves more of the log variation in inflow rates over time, and thereby in theory affords greater potential for inflows to explain cyclical unemployment.

Figure 7 compares the inflow contributions implied by the two alternative corrections for aggregation bias, as well as the contributions based on no correction at all. The starkest finding is that failing to correct for time aggregation bias does indeed apportion a greater role to the inflow rate, and therefore correcting for that bias is important. It is also true that the weekly correction places marginally greater emphasis on inflows than the continuous-time correction, but quantitatively the effects are small. Thus, the results based on the discrete-time aggregation correction methods are broadly similar to those obtained in the aggregate analysis of section I.B.

D. **Disaggregation by Reason for Unemployment**

Until now, we have been concentrating on aggregate unemployment flows based on Shimer’s approach to the published CPS time series. As noted at the beginning of section I.A,  

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15 Strictly speaking, this occurs for a slightly different reason from that highlighted by Shimer, who argues that “ignoring time aggregation will bias a researcher towards finding a countercyclical separation probability, because when the job finding probability falls, a worker who loses her job is more likely to experience a measured spell of unemployment.” In fact, we find that the aggregation bias corrections have little effect on the countercyclicality of the level of the inflow rate. But, by raising the overall level of the inflow rate, they reduce the countercyclicality of the log inflow rate, which is what matters for the statistical decomposition of cyclical variation in unemployment.

16 For all three of these approaches to time aggregation bias, this figure’s contributions for the most recent recession are based on our correction for the 1994 CPS redesign.
however, this approach ignores that almost half of unemployment comes from non-participation in the labor force, not employment. In this section, we extend the analysis to incorporate flows from non-participation. At the same time, we also distinguish employment-to-unemployment flows stemming from job loss and from job leaving, as these two flows have very different cyclical properties.

The disaggregated analysis in this section uses data on the number unemployed by reason, the number unemployed for less than five weeks by reason, and aggregate series for employment and non-participation. Our disaggregation of unemployment by reason uses three categories: job losers, job leavers, and labor force entrants.\(^{17}\) The complete requisite series for short-term unemployment by reason are not available on the BLS website, so we have based this section’s analysis on data from the monthly BLS Employment and Earnings publications. Even those data for short-term unemployment by reason extend back only to May 1968 and are not seasonally adjusted. For internal consistency, we start with the seasonally unadjusted Employment and Earnings data for all the series used in this section. As in section I.C, we treat the 1994 discontinuity in the short-term unemployment series by multiplying each published short-term unemployment number from February 1994 on by an average ratio of the short-term share of unemployment in the first and fifth rotation groups to the corresponding short-term share for the full sample. In particular, based on the CPS microdata from February 1994 through January 2005, we calculate correction factors of 1.0948 for job losers, 1.1644 for job leavers, and 1.2221 for labor force entrants. Finally, we seasonally adjust all the series with Eviews’ implementation of the Census Bureau’s X-12 procedure.

\(^{17}\) We do not further disaggregate job losers into temporary layoffs and permanent job losers for two reasons. First, the temporary layoff information is available only back to 1976. Second, as explained in Polivka and Miller (1998), the 1994 CPS redesign caused a discontinuity in the way the two types of job losers are distinguished. Similarly, we do not disaggregate labor force entrants into new entrants and re-entrants because the 1994 redesign instituted a major change in the way the two types of entrants are distinguished.
Given the resulting data, it is again straightforward to calculate monthly outflow probabilities for each reason for unemployment. Specifically, for each reason we can calculate

\[ F_{rt} = 1 - \left[ \left( u_{r,t+1} - u_{r,t+1}^* \right) / u_{rt} \right], \]

where a subscript \( r \) denotes reason. And, as in the aggregate case, we can calculate the associated outflow hazards by reason, \( f_{rt} = -\log(1 - F_{rt}) \). As detailed in our appendix, we treat time aggregation bias with an extension of our discrete-time correction, which produces a corrected inflow hazard \( s_{rt} \) for each type of unemployment.

Figure 8 displays the time series for each of these inflow rates. It reveals stark heterogeneity in the cyclical properties of the three inflow hazards. The job loser inflow is clearly countercyclical, displaying prominent upward spikes in all recessions. By contrast, the job leaver inflow rate is prominently procyclical (which is not so surprising given the procyclicality of quit rates noted above in footnote 4). Finally, the inflow from non-participation is comparatively acyclical.

The latter three observations have an important implication with respect to the literature’s usual approach of considering only the aggregated inflow. Concentrating on the aggregate inflow rate conflates loser and leaver inflows that move in opposite directions over the cycle, and in addition it averages them with a broadly acyclical inflow of entrants. Looking only at an aggregate inflow has the effect of masking the individual contributions of each of these inflow rates that move in different cyclical directions.

Figure 9 displays the analogous results for outflow rates by type. This figure exhibits two types of heterogeneity. First, job losers show considerably lower outflow rates (and hence longer unemployment spells) than do leavers and entrants. This fact combined with the countercyclicality of losers’ share of the inflow constitutes the kernel of truth in the argument by Darby, Haltiwanger, and Plant (1986): One reason the aggregate outflow rate declines in a
recession is the increased inflow share of job losers, whose outflow rates are relatively low. As shown by Baker (1992) (and reaffirmed in section 3 of Shimer, 2007), however, this composition effect is not nearly strong enough to justify Darby, Haltiwanger, and Plant’s conclusion that “The Ins Win.”\(^\text{18}\) Interpreted in the framework of our equation (3), the estimates in Baker’s tables 1 and 3 indicate that adjusting for this composition effect decreases the share of cyclical unemployment due to cyclicality in outflow rates from 57 percent to 49 percent. Thus, Baker’s results are altogether consistent with our conclusion that both the ins and outs of unemployment are empirically important.

Second, figure 9 shows that the outflow rate is especially procyclical for job losers. Because the outflow rate also is quite procyclical for the other two types of unemployed, though, aggregating the various outflow rates is much less problematic than aggregation of the inflows.

To get a sense of the individual contributions of each of the inflow and outflow rates by reason, we again seek to decompose the change in the log unemployment rate into components due to each of the flows. To this end, note first that we can split the aggregate unemployment rate into the sum of the unemployment rates for each reason, \(\tilde{u} = \tilde{u}_\lambda + \tilde{u}_q + \tilde{u}_e\), where subscripts \(\lambda\), \(q\), and \(e\) refer to job losers, job leavers (quits), and labor force entrants respectively. Log differentiation of the latter reveals that the change in the log unemployment rate is equal to the share-weighted sum of the log changes in the constituent sub unemployment rates:

\[
(8) \quad d \log \tilde{u} = \omega_\lambda d \log \tilde{u}_\lambda + \omega_q d \log \tilde{u}_q + \omega_e d \log \tilde{u}_e
\]

where \(\omega_r\) is the unemployment share of reason \(r\). In steady state, the three sub unemployment rates are given by

\(^{18}\) Baker and Shimer also explore composition changes with respect to observable demographic characteristics and conclude that these can explain very little of the cyclicality in outflow rates. Of course, this does not rule out the possibility of important composition changes with respect to unobserved characteristics.
where \( e \) and \( i \) denote employment and non-participation as a fraction of the labor force. It turns out that the log variation in both \( e \) and \( i \) over time is minuscule relative to the cyclical variation in log unemployment (see figure 10). Thus, a very good approximation over the few quarters represented by a recessionary ramp-up in unemployment is that \( d \log e \approx 0 \approx d \log i \).\(^{19}\) This yields the following very simple approximate decomposition:

\[
\begin{align*}
\tilde{u}_\lambda &= s_\lambda e / f_\lambda \quad \Rightarrow \quad d \log \tilde{u}_\lambda = d \log s_\lambda - d \log f_\lambda + d \log e \\
\tilde{u}_\psi &= s_\psi e / f_\psi \quad \Rightarrow \quad d \log \tilde{u}_\psi = d \log s_\psi - d \log f_\psi + d \log e \\
\tilde{u}_c &= s_c i / f_c \quad \Rightarrow \quad d \log \tilde{u}_c = d \log s_c - d \log f_c + d \log i
\end{align*}
\]

Figure 11 displays the results of this decomposition. Specifically, it plots the contribution of each unemployment flow, for each reason, for each recession since 1969. The contribution of each flow is measured, in accordance with equation (10), by multiplying the difference in the log flow relative to its start of recession value by the initial share in unemployment of that flow at the start of the recession.

The results of this exercise reveal that there is a great deal of richer detail underlying the aggregate analyses performed by Shimer, ourselves, and others. First and foremost, the decomposition indicates that the most important flow in all but the last two recessions was the job loser inflow rate. In addition, the job loser inflow contributed to a non-trivial degree in the 1990 recession, and was very prominent in the first five quarters of the 2001 unemployment

\(^{19}\) Of course, although the cyclical variation in \( \log e \) and \( \log i \) is far smaller than the cyclical variation in \( \log u \), it is not really zero. That is why we do not use this approximation in the previous analyses of sections I.A, B, and C, where we do not need the approximation to derive a tractable decomposition method.
Thus, recent claims such as “In the modern U.S. economy, recessions do not begin with a burst of layoffs” (Hall, 2005b, p. 397) are not supported by the CPS data.\textsuperscript{21}

Moreover, figure 11 confirms that the aggregate picture presented in figure 3 masks important heterogeneity in the cyclical effects of each individual inflow rate. Specifically, it can be seen that the contribution to recession unemployment due to job leavers is systematically negative because the leaver inflow rate is procyclical. This serves to offset part of the increase in unemployment due to increased job loss.

Figure 11 also provides some insight into why the aggregate inflow rate performs relatively poorly in explaining the increase in unemployment in recent recessions. The contribution of the inflow rate from non-participation declined from a positive effect in the 1969, 1973, and 1979 recessions, to mildly positive in the 1981 and 1990 recessions, to negative in the 2001 recession. This is important to emphasize as, from a theoretical perspective, macroeconomists are typically most interested in unemployment inflows that originate from employment rather than non-participation. Indeed, Shimer’s (2005a, 2005b) practice of referring to the unemployment inflow rate as the “separation rate” reflects this focus.

Turning to outflows, we can see from figure 11 that the reason aggregate outflows explain so much of the variation in unemployment is because all of the constituent outflows by reason cause unemployment to move in the same direction – that is, up in a recession. In addition, we see that the most important outflow is the outflow rate for job losers. This is to be expected, as job losers represent a substantial fraction of the unemployment pool. That aside,

\textsuperscript{20} Note that our choice to weight by \textit{pre}-recession unemployment shares errs on the side of \textit{under}stating the importance of the job loser inflow.

\textsuperscript{21} Hall’s conclusion is based partly on the Job Openings and Labor Turnover Survey (JOLTS). Because JOLTS began in December 2000, it missed part of the ramp-up to the most recent recession. Furthermore, the JOLTS data for that recession seem to be at odds with information from other surveys, including our evidence from the CPS. A careful comparison of what multiple sources of labor market data have to say about the last recession would be a very worthwhile research project.
however, the losers outflow rate is conspicuously dominant in the 1990 recession, again suggesting that this recession was especially different from the others in the sample period.

A question that arises at this point is the extent to which the disaggregated analysis is important. Surely, one might argue, it nevertheless aggregates to the same story mentioned in section I.B? Our view, however, is that the disaggregated analysis culminating in figure 11 affords a more nuanced and illuminating view of unemployment flows, especially with regard to the inflows. It is not clear what economic hypothesis is being assessed when one observes the cyclicality of the aggregate inflow rate, which is a weighted average of a number of sub-inflow rates. However, the economics becomes clearer, and very intuitive, when one looks at inflows by reason. The job leaver inflow into unemployment falls in all recessions for the same reason that the quit rate does – presumably because workers find it harder then to find attractive new jobs. The job loser inflow rate rises in all recessions for the same reason that the layoff rate does – because firms want to employ fewer workers in a recession; they are unable (especially in the more severe recessions) to achieve the intended employment reductions merely by allowing workers to quit; and they therefore lay off more workers, many of whom then experience unemployment.

II. Summary and Discussion

Our reanalysis of repeated cross-section data from the Current Population Survey has confirmed the finding of previous studies that procyclicality of the hazard rate for exiting unemployment plays an important role in cyclical unemployment. Contrary to Shimer and Hall’s conclusions, however, we have shown that even Shimer’s own methods and data indicate an important role for countercyclical inflows into unemployment. This finding is further
strengthened by our refinements of Shimer’s methods of correcting the official CPS labor force series for the 1994 redesign of the CPS and for time aggregation bias. In addition, we have conducted a disaggregated analysis that recognizes the large unemployment inflows from non-participation in the labor force and also distinguishes employment-to-unemployment inflows stemming from job losing and job leaving. The disaggregated results highlight the particularly important role of job loss inflows to unemployment in accounting for increased unemployment in most recessions. Thus, in contrast to both Darby et al.’s pronouncement that “The Ins Win” and Shimer and Hall’s opposite conclusion that the outs win, we find that everyone’s a winner.

At a basic level, then, our paper suggests that a complete understanding of cyclical unemployment requires an explanation of countercyclical unemployment inflow rates as well as procyclical outflow rates. Accordingly, the many recent analyses cited in our second paragraph that overlook cyclical inflows may be ill-advised. By the same token, earlier efforts to explain why unemployment inflows rise in a recession (e.g., Mortensen and Pissarides, 1994) remain potentially relevant.

In the remainder of this section, however, we want to emphasize that the precise economic interpretation of statistical decompositions such as equation (3) is not as clear as it might seem. Up until now, we have followed the literature in interpreting the decompositions as answering the question “how much of the increase in unemployment in a recession is due to changes in inflows and outflows.” In what follows, we show that such an interpretation is not the only possible reading of decompositions based on (3), and that different models of the labor market imply different interpretations.

We motivate this point with the following metaphor. Imagine a traffic intersection at which a queue of automobiles awaits a green light. The light stays green long enough in each
cycle to allow an outflow of five cars to leave the queue before the light turns red again. Ordinarily, only a moderate number of cars is backed up at the light. But suppose some event—say, construction on an alternate route—ramps up the inflow of cars to this intersection. If nothing happens to keep the green light on longer, then the queue gets longer, and each car’s wait to get through the intersection becomes longer.

Now just for the moment, think of the queue of backed-up cars as unemployment, and think of the five cars going through each green light as the outflow from unemployment. When the inflow increased, the stock of unemployment increased, and so did the average duration of unemployment. If an analysis such as ours or Shimer’s were applied here, it would attribute much of the increased unemployment to a decreased exit rate even though nothing actually changed in the outflow process. The proximate cause of both the increased unemployment level and the increased duration was the increased inflow.22

Thus, the traffic metaphor illustrates a possibility worth considering when reacting to statistical decompositions of the ins and outs of unemployment. Although such analyses attempt to separate the contributions of inflows and outflows, the inflows and outflows may be inherently inseparable. It could be, for example, that congestion from increased inflows causes outflow hazard rates to become lower.23

This latter possibility has received little attention in the previous literature on unemployment flows, perhaps because of the literature’s focus on search and matching models of the aggregate labor market (Pissarides, 1985; Mortensen and Pissarides, 1994). In these models,

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22 Note also that, just as the wait until going through the green light would increase for all cars regardless of whether they had arrived from the usual route or from the obstructed alternate route, unemployment duration would increase for all the unemployed—job losers, job leavers, and labor force entrants—just as found in the analyses by Baker (1992), Shimer, and ourselves.

23 Another example of interaction between inflows and outflows, discussed above in section I.D, is that cyclical changes in the composition of the inflow to unemployment (such as the increased share of permanent job losers) may cause a reduction in the outflow rate.
the number flowing out of unemployment is increasing in the number of unemployed workers, as well as in the number of job vacancies. The matching function that describes this relationship is meant to capture frictions that prevent firms and workers from quickly finding (suitable) partners for an employment relationship. Under the typical specification of this matching function, a greater number of unemployed workers (the denominator of the outflow hazard) will raise the number flowing out of unemployment (the numerator of the outflow hazard) so that the outflow rate will not itself depend on the number unemployed. Put in the language of the traffic metaphor, the green light stays on longer when more cars are waiting at the intersection. According to these models, then, changes in the outflow hazard will be driven only by exogenous variables, notably labor productivity.24 In this theoretical framework, the mechanism encapsulated in the traffic metaphor does not arise.

That particular theoretical perspective, however, is not the only conceivable economic interpretation of cyclical flows in the labor market. Consider, for example, an alternative model in which firms face no friction in hiring unemployed workers; that is, firms may hire as many unemployed workers as they wish without incurring important search costs.25 Then, given labor productivity, firms will choose directly the number of workers to hire out of the unemployment pool. In the language of the traffic metaphor, how long the green light stays on is not determined by the number of cars waiting at the intersection. Then, as in the traffic metaphor, increased unemployment due to increased inflows can mechanically reduce outflow hazard rates during recessions.

24 Indeed, Shimer (2007, p. 20) makes this point to justify his emphasis on flow hazard rates, rather than the levels of the unemployment flows.
25 Such an assumption may not be an entirely ludicrous approximation, as the average duration of a vacancy is consistently less than one month in the Bureau of Labor Statistics’ JOLTS dataset.
Viewed through this lens, a more appropriate decomposition of unemployment flows might focus on changes in the level of the outflow, since these are independent of the number unemployed in the latter model. It turns out that simple algebraic manipulation of equation (3), our framework for decomposing cyclical unemployment variation into inflows and outflows, provides such a decomposition:

\[
\text{(11)} \\
d \log \tilde{\mu}_t \approx \frac{1-\tilde{\mu}_t}{\tilde{\mu}_t} \left[ d \log s_t - d \log (f_t \tilde{\mu}_t) \right]
\]

This re-expression of equation (3) decomposes cyclical variation in log unemployment into an inflow component plus an outflow component involving the log change in the number flowing out of unemployment, \(f_t \tilde{\mu}_t\) (instead of the hazard rate for the outflow, \(f_t\)). The monthly version of the latter is plotted in figure 12, which reiterates a fact mentioned in this paper’s introduction: Even though the hazard rate for exiting unemployment goes down in recessions, the number exiting unemployment goes up.

Given the countercyclicality of the number exiting unemployment, if one viewed unemployment flows solely in terms of the model motivating equation (11), one would conclude that more than the entirety of the cyclical variation in unemployment is accounted for by countercyclical inflows. That is, one would declare that “The Ins Win” after all. Our point, however, is not to deny the importance of reduced outflow hazard rates in recessions. Our point is that, in order to assess the roles of inflows and outflows in cyclical unemployment, one must understand the economic determinants of both the ins and the outs. The challenge to future theoretical work is to develop coherent and plausible models that can account for the full range of relevant empirical evidence. In terms of the particular facts we hope to have clarified in this paper, theoretical analyses should explain why job-loss-induced inflows to unemployment
increase at the beginning of a recession and why outflows do not increase enough to keep unemployment duration from rising.\textsuperscript{26}

\begin{quote}
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\end{quote}

\textsuperscript{26} Of course, theoretical work also should endeavor to explain the cyclical features of other salient variables such as employment, hours of work, wage rates, vacancies, productivity, capital utilization, etc.
Appendix

Discrete-Time Correction for Time Aggregation Bias in Aggregate Inflows

We use an analogous method to Shimer's in discrete time. That is, we essentially use one difference equation, that for the total stock of unemployment:

\[ u_{t+\tau+1/4} = u_{t+\tau} + s_t^w e_{t+\tau} - f_t^w u_{t+\tau} \]  

(A.1)

where \( s_t^w \) and \( f_t^w \) are the weekly inflow and outflow probabilities and are assumed constant between interview dates, and where \( \tau \in \left\{0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}\right\} \) indexes the intervening weeks. Like Shimer, we then make the further assumption that the labor force, \( l_t \equiv e_t + u_t \), is also constant within the interval. This implies that we can rewrite (A.1) as:

\[ u_{t+\tau+1/4} = s_t^w l_t + \left(1 - s_t^w - f_t^w\right) u_{t+\tau} \]  

(A.2)

Solving this equation forward four weeks yields the following non-linear equation:

\[ u_{t+1} = s_t^w l_t \sum_{n=0}^{3} \left(1 - s_t^w - f_t^w\right)^n + \left(1 - s_t^w - f_t^w\right)^4 u_t \]  

(A.3)

Noting that the steady-state weekly unemployment stock in this model is given by \( u_t^w = s_t^w / (s_t^w + f_t^w) \) yields equation (7) in the main text.

Discrete-Time Correction for Time Aggregation Bias in Inflows by Reason

The correction for inflows by reason is a simple extension to the above. Now there are three difference equations to solve out – one for unemployment by each reason:

\[ u_{\lambda,t+\tau+1/4} = u_{\lambda,t+\tau} + s_{\lambda,t}^w e_{t+\tau} - f_{\lambda,t}^w u_{\lambda,t+\tau} \]  

(A.4)

\[ u_{q,t+\tau+1/4} = u_{q,t+\tau} + s_{q,t}^w e_{t+\tau} - f_{q,t}^w u_{q,t+\tau} \]

\[ u_{e,t+\tau+1/4} = u_{e,t+\tau} + s_{e,t}^w e_{t+\tau} - f_{e,t}^w u_{e,t+\tau} \]

where \( i \) is the stock of non-participation. We then again assume, like Shimer, that the labor force is constant in the month between CPS interviews. It should be noted that this has the implication that the non-participation stock is also constant between months. Since the unemployment system implicit in the above is a closed one (all flows among unemployment, employment, and non-participation originate from one of these three categories), the population (the sum of unemployment, employment, and non-participation) is implicitly constant.
Given this, equation (A.4) is just a non-linear system, which can be solved using conventional programs such as MATLAB.
Figure 0: Unemployment Rate and Recessionary Unemployment Dates Used
Figure 1: Replication of Shimer’s Figure 1
Figure 2: Log Inflow and Outflow Hazard Rates Using Replication of Shimer’s Data
Figure 3: Changes in Log Inflow and Outflow Rates by Recession, 1948–2004
Figure 4: Month-by-Month Ratio of Short-Term Share of Unemployment in Incoming Rotation Groups to Full Sample

Mean post Feb 1994 = 1.1549
Figure 5: Effect of Our Alternative Redesign Correction on the 2000-2001 Recession
Figure 6: Effects of Different Aggregation Bias Corrections on Measured Log Inflow Rates
Figure 7: Effects of Aggregation Bias Corrections on Decomposition
Figure 8: Log Inflow Rates by Reason for Unemployment
Figure 9: Log Outflow Rates by Reason for Unemployment

![Log Outflow Rates by Reason for Unemployment](image-url)
Figure 10: Logs of Employment, Non-Participation, and Unemployment as Fractions of the Labor Force
Figure 11: Decomposition of Increase in Unemployment into Effects of Flows by Reason for Unemployment
Figure 12: Level of Monthly Outflow from Unemployment (Quarterly Average)
References


Blanchard, Olivier and Jordi Gali. 2006. “A New Keynesian Model with Unemployment.” MIT and CREI.


